

JAM19: strange quark suppression from a simultaneous global fit of PDFs and FFs

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[arXiv:1905.03788 \[hep-ph\]](https://arxiv.org/abs/1905.03788)



JAM19

What is JAM19?

First **simultaneous** analysis of **unpolarized** PDFs and FFs

Why JAM19?

To study the **strange** quark distribution

Motivation

- Knowing the limits in x and Q^2 of collinear factorization
- Testing the universality of PDFs ,FFs...
- All the data must be studied using the **same** theoretical framework
- First step: (first) **simultaneous** analysis of **unpolarized PDFs** and
FFs $\longrightarrow$ **Strange** quark distribution

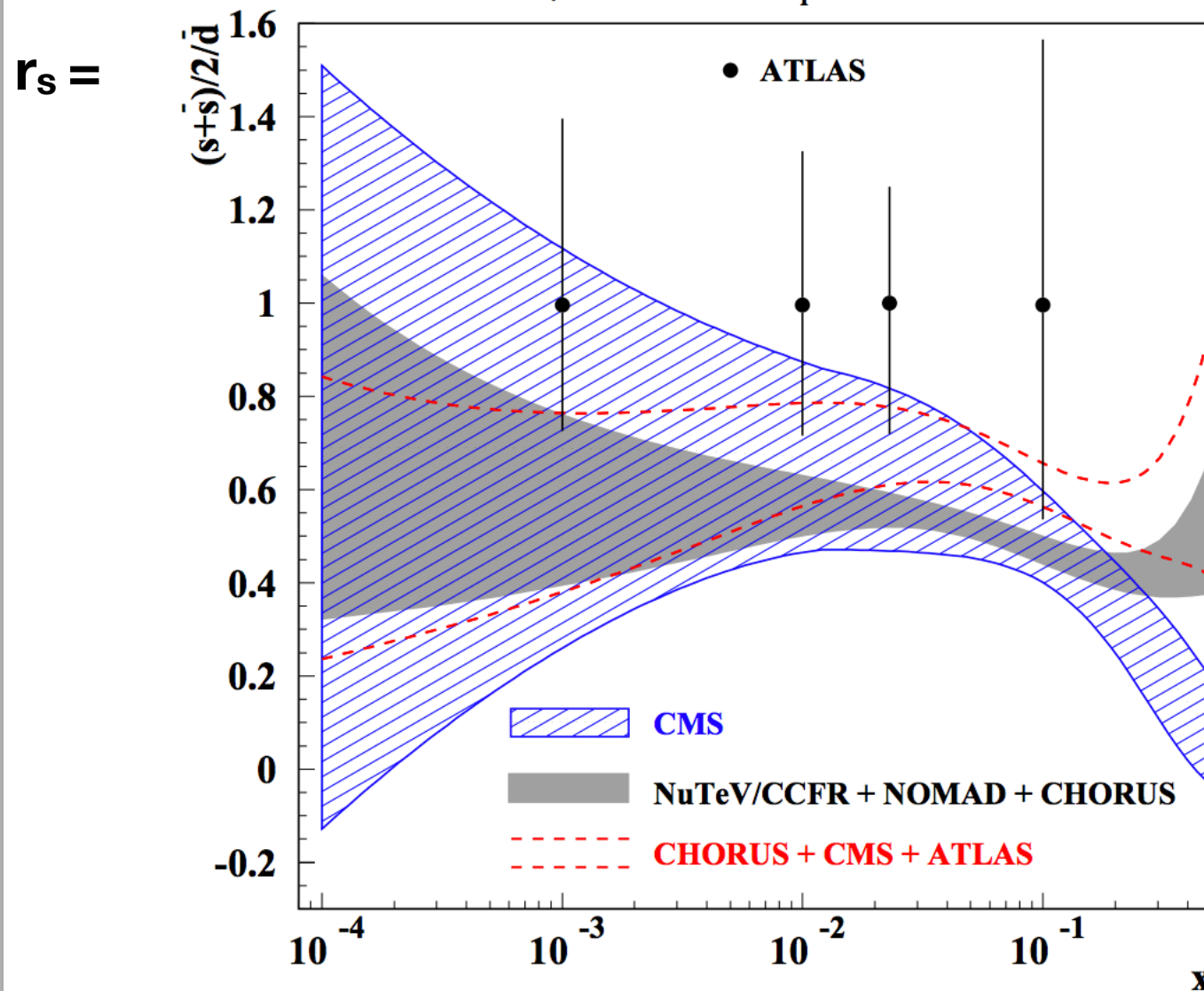
Motivation II

- The strange PDF is **less known** than the non-strange light flavors
- Traditionally: **neutrino**-(heavy) **nucleus** DIS data used to extract the strange PDF.
 - Drawbacks: nuclear effects on PDFs.
- **W** and **Z** inclusive production in **p-p** collisions also sensitive to flavor separation
 - Drawbacks: tension between CMS and ATLAS results?

Motivation II

Alhekin et al. [arXiv:1404.6469](https://arxiv.org/abs/1404.6469) [hep-ph]

$\mu^2 = 1.9 \text{ GeV}^2, n_f = 3$



Why don't we use
SIDIS?

Setup: data

$$\text{DIS} : l + (p, d) \rightarrow l' + X$$

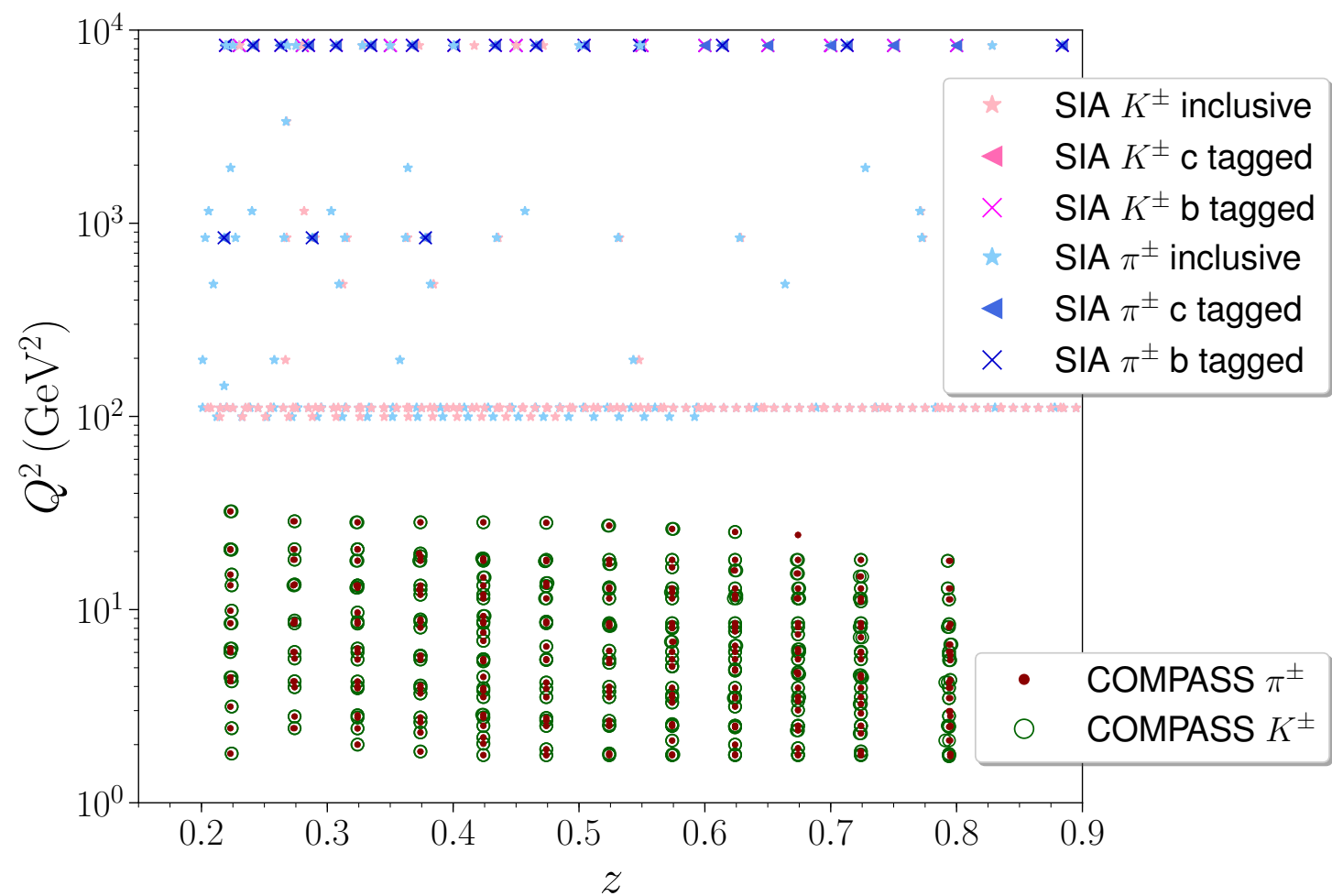
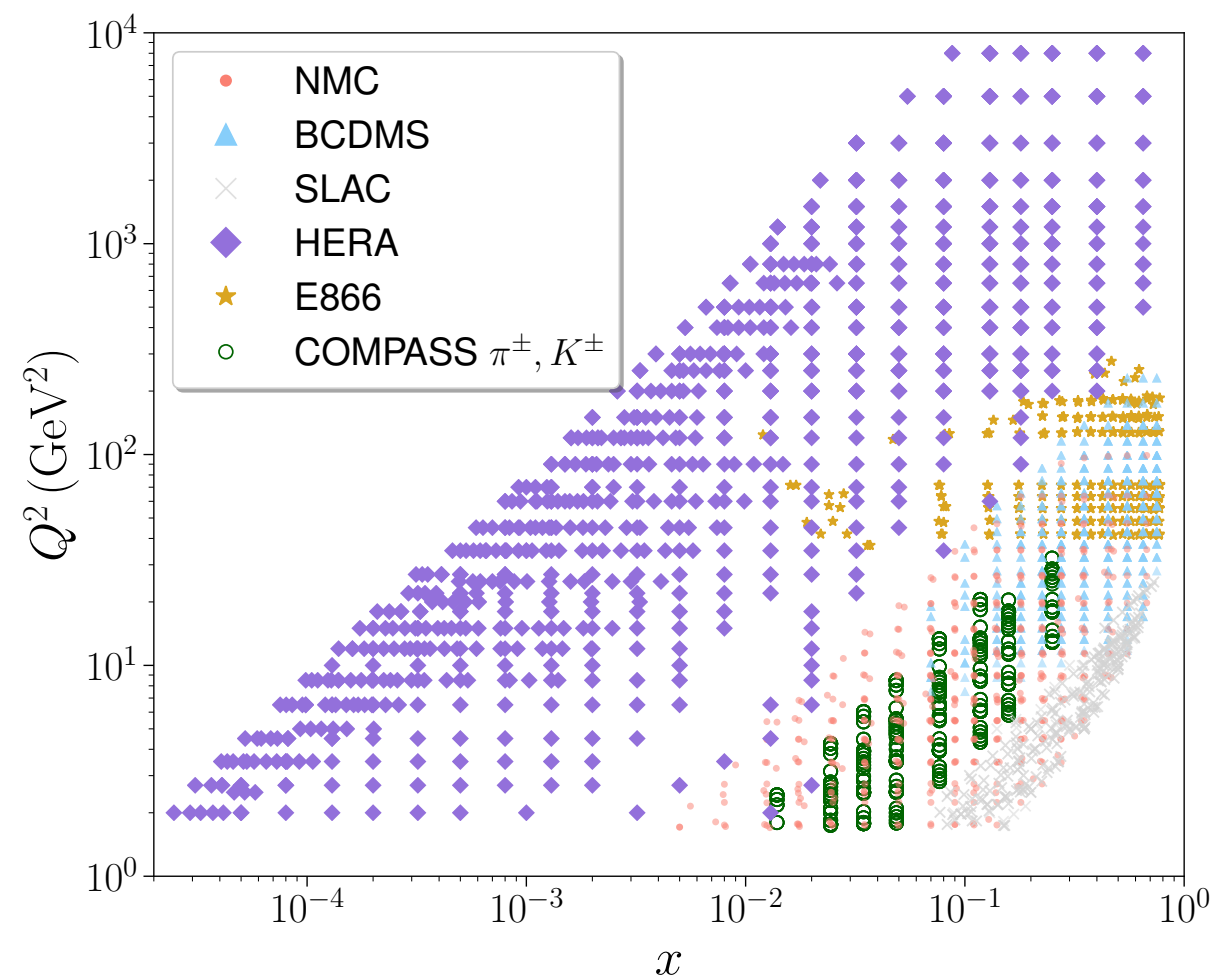
$$\text{DY} : l + (p, d) \rightarrow l\bar{l} + X$$

$$\text{SIDIS} : l + d \rightarrow l' + h + X$$

$$W^2 > 10 \text{ GeV}^2$$

$$Q^2 > m_c^2$$

$$\text{SIA} : e^+ + e^- \rightarrow h + X$$



Setup: theory

- All observables computed at NLO in pQCD
- DGLAP truncated evolution at order α_s in Mellin space
- DIS/SIDIS/SIA cross sections computed at leading twist
- Nuclear smearing for deuterium DIS
- Heavy quark treatment : ZM-VFN
- Fitting methodology:
 - MC (multi-steps), k-means clustering, extended reduced χ^2

Why MC?

- Typical PDF parametrization:

$$x\Delta f(x) = Nx^a(1-x)^b(1+c\sqrt{x}+dx)$$

$$\chi^2 = \sum_e^{N_{exp}} \sum_i^{N_{data}} \frac{(D_i^e - T_i)^2}{(\sigma_i^e)^2}$$

- Perform single χ^2 -fit: $\longrightarrow$ Multiple local minima!

Parameters difficult to constrain

Hessian method for uncertainties $\longrightarrow$ Introduces tolerance criteria

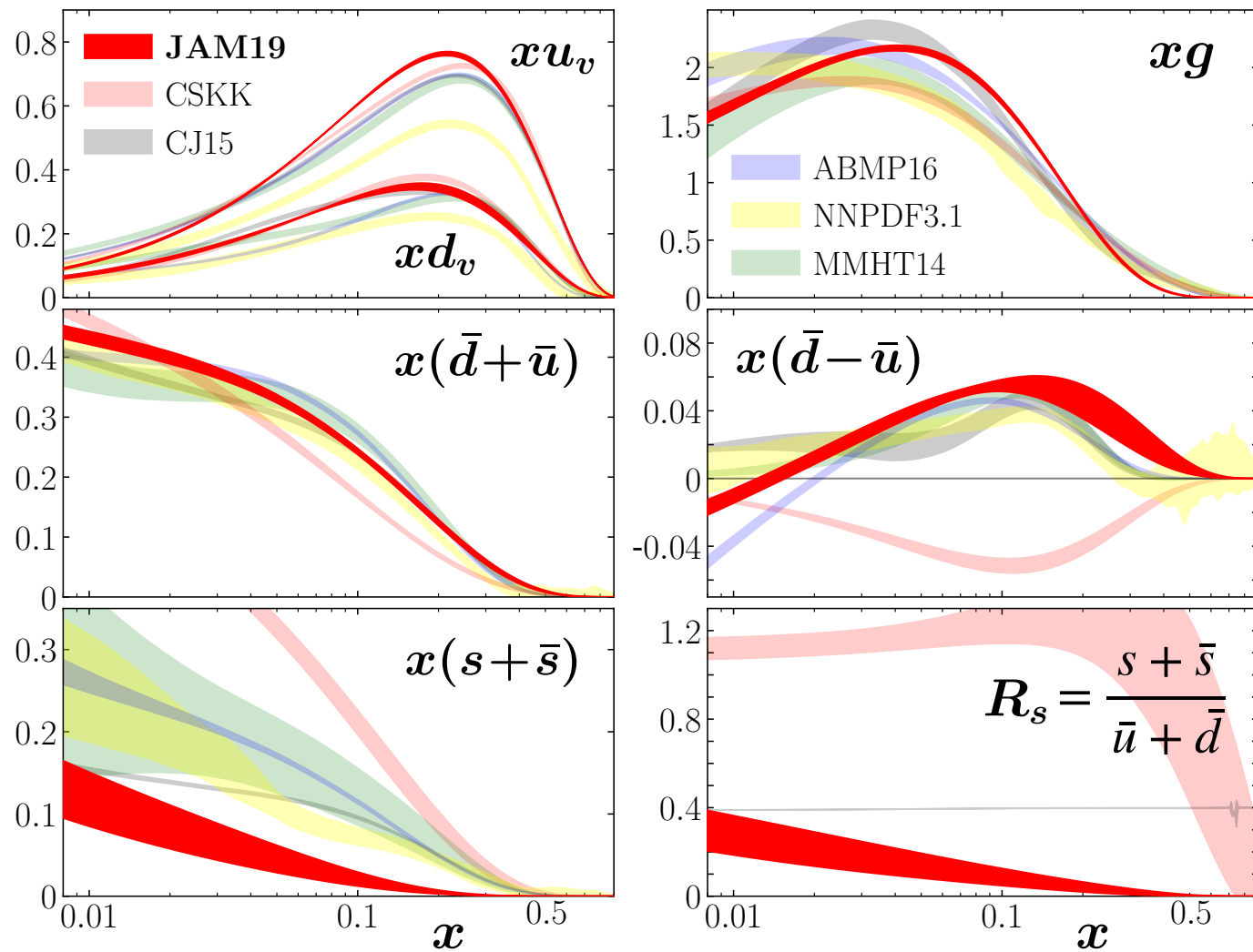
Unsuitable for simultaneous analysis of collinear distributions

- Monte Carlo methods:
 - Allows efficient exploration of the parameter space
 - Uncertainties directly obtained from MC replicas

PDF results

JAM19 PDFs

arXiv:1905.03788 [hep-ph]

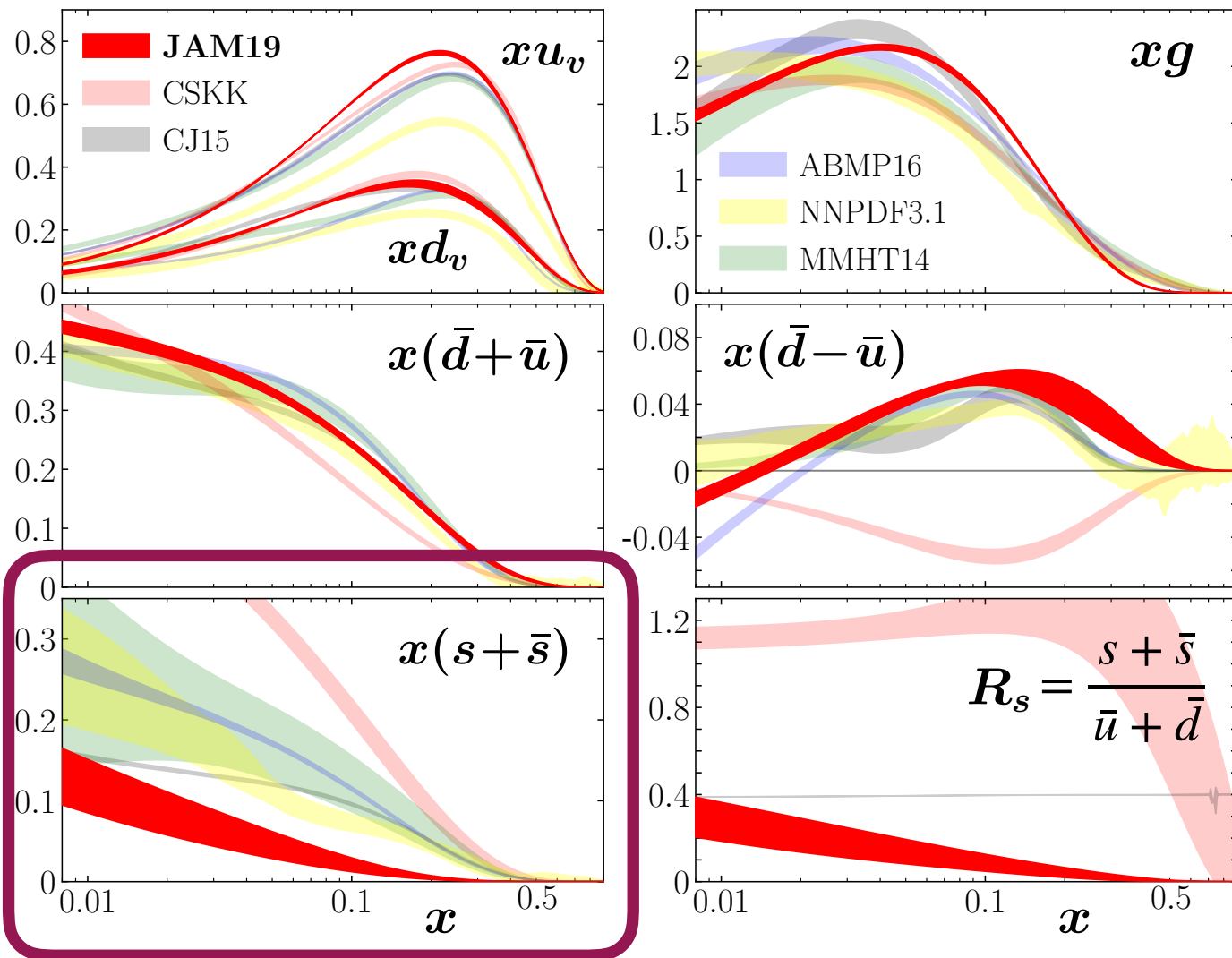


$Q = m_c$

DIS(p, d)
 DY(pp, pd)
 SIA($\pi^\pm, K^\pm$)
 SIDIS($\pi^\pm, K^\pm$)

JAM19 PDFs

arXiv:1905.03788 [hep-ph]



$Q = m_c$

DIS(p, d)

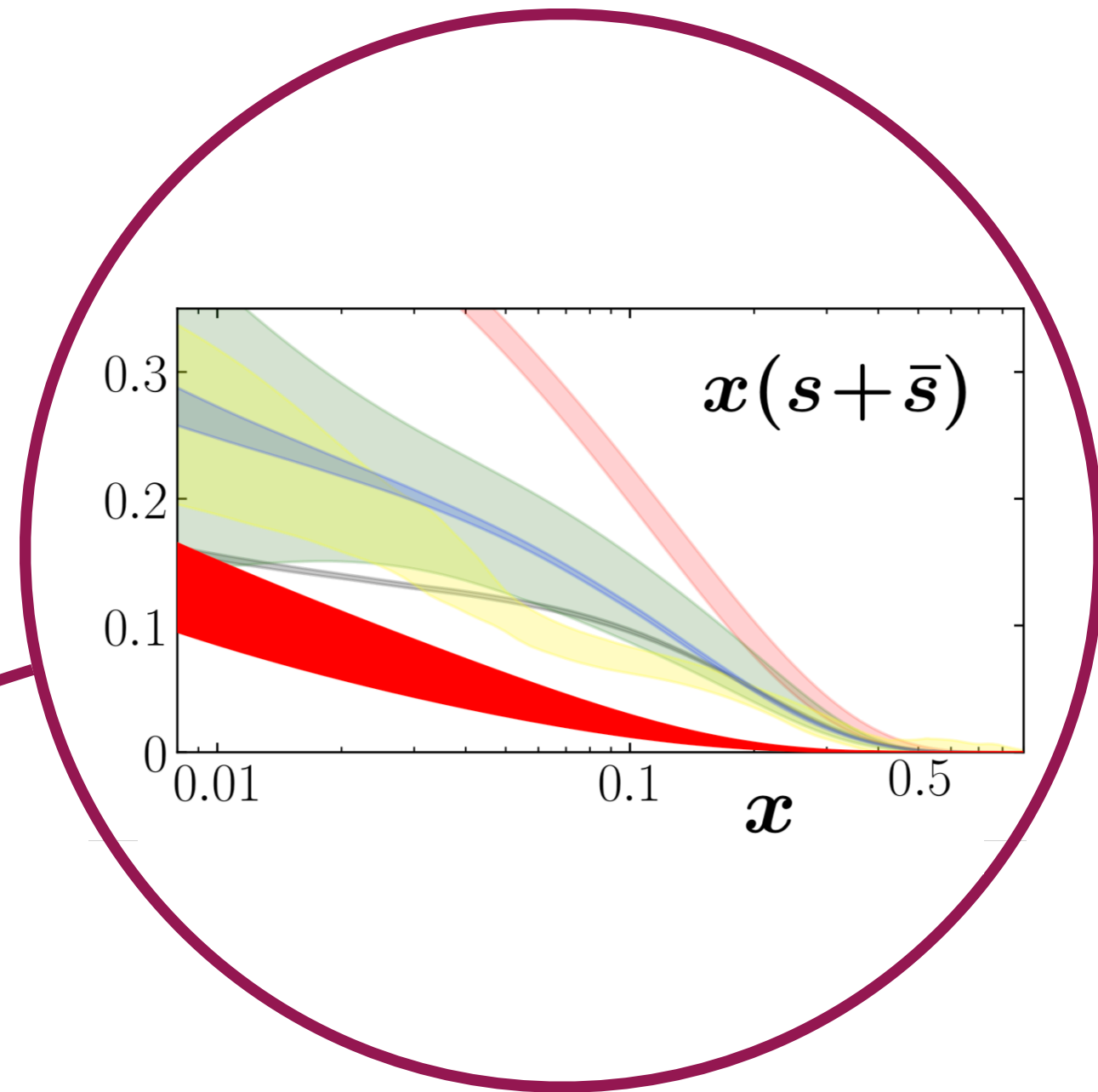
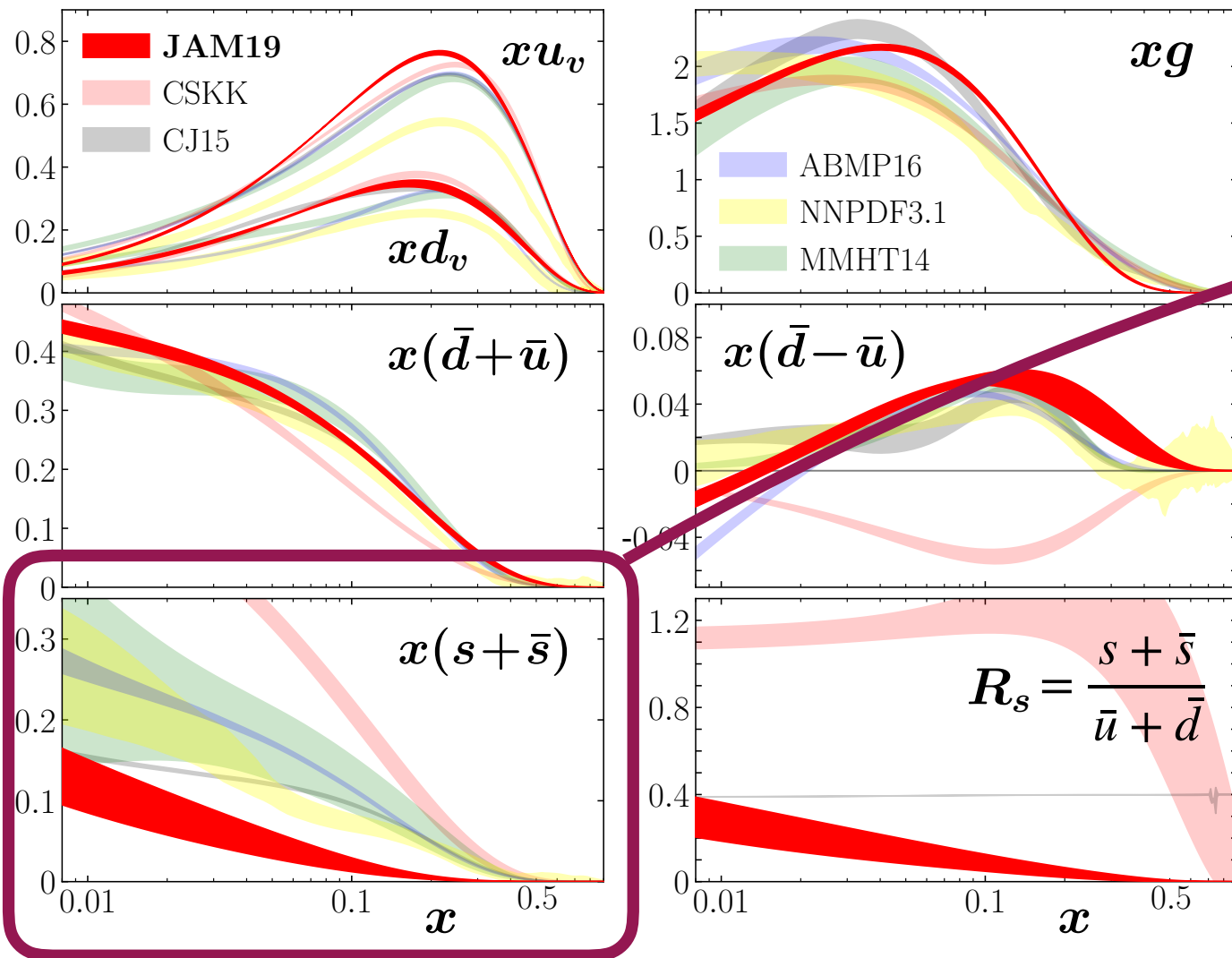
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SIA($\pi^\pm, K^\pm$)

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JAM19 PDFs

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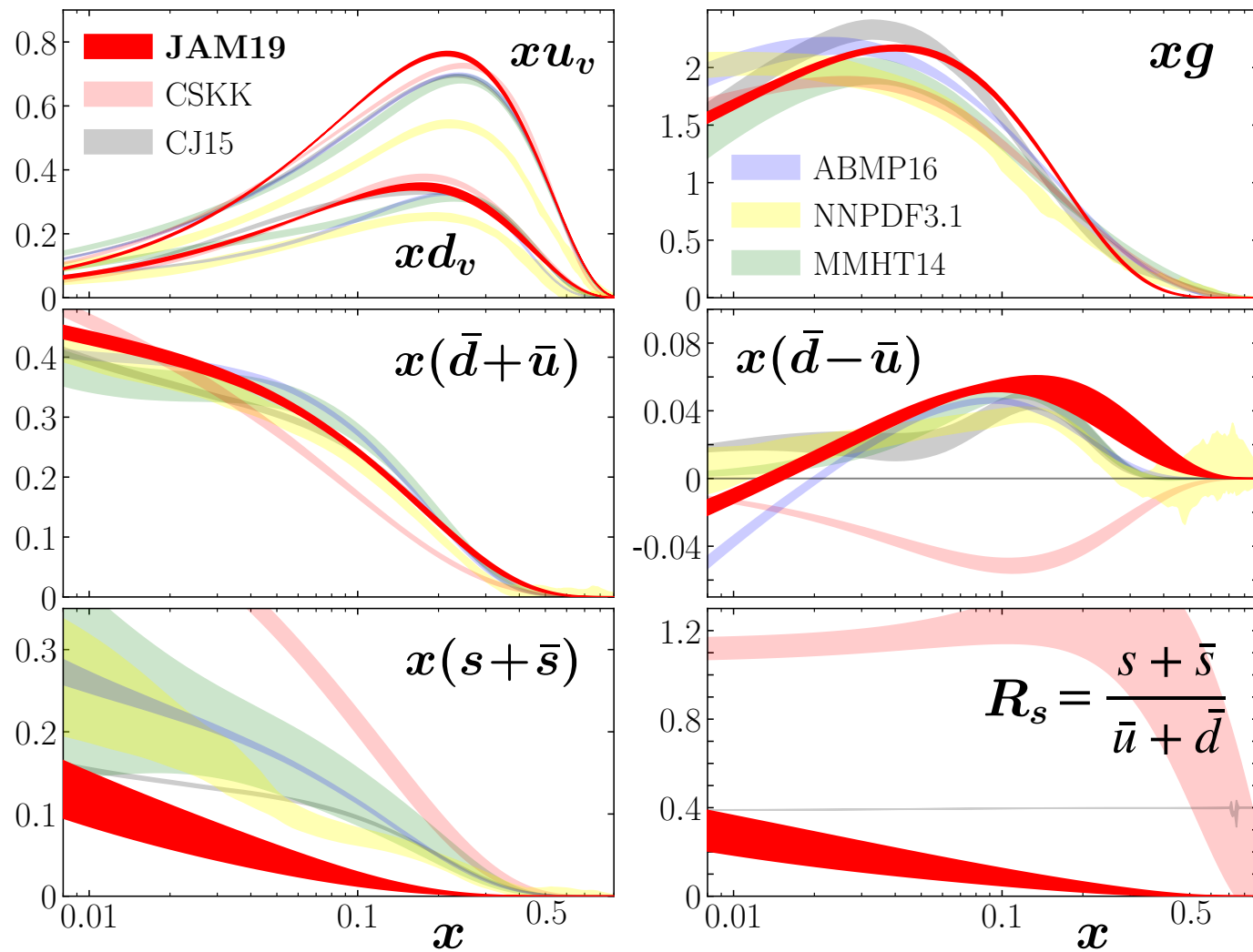
Strong strange suppression

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JAM19 PDFs

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$Q = m_c$

DIS(p, d)

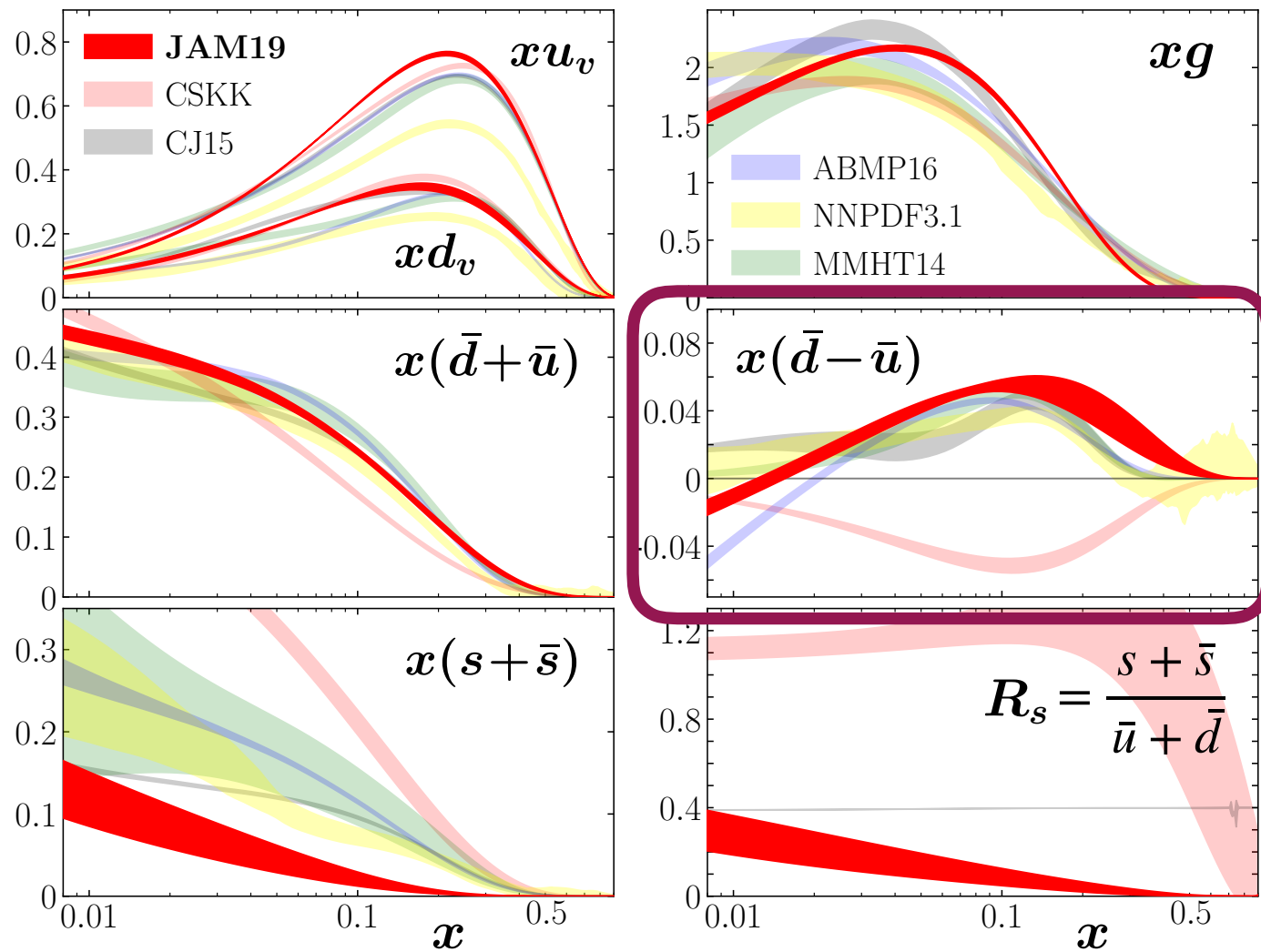
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JAM19 PDFs

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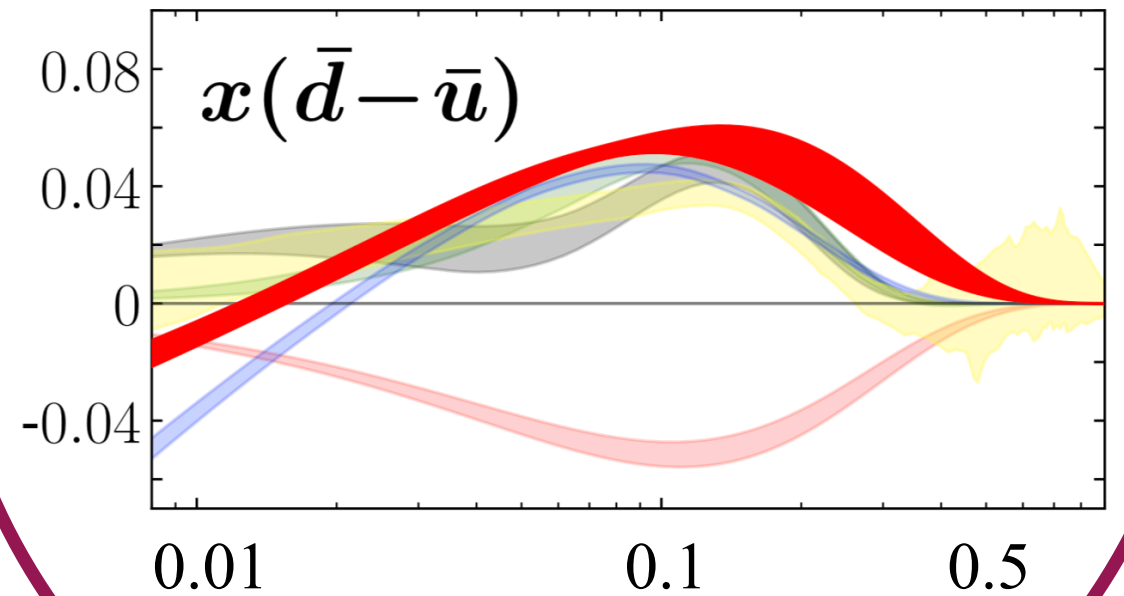
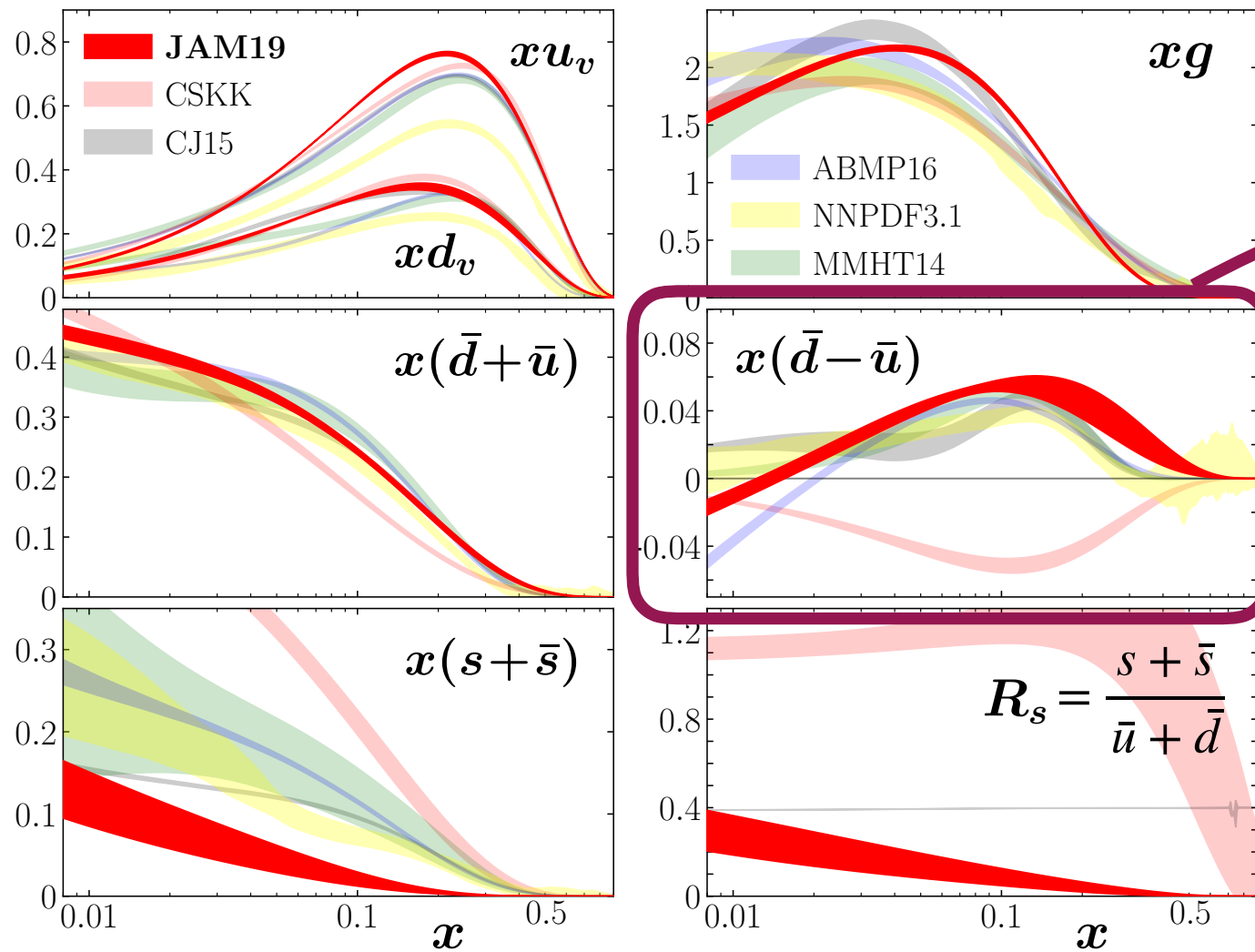


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JAM19 PDFs

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$\bar{d} - \bar{u} > 0$ at $x \sim 0.1 - 0.2$

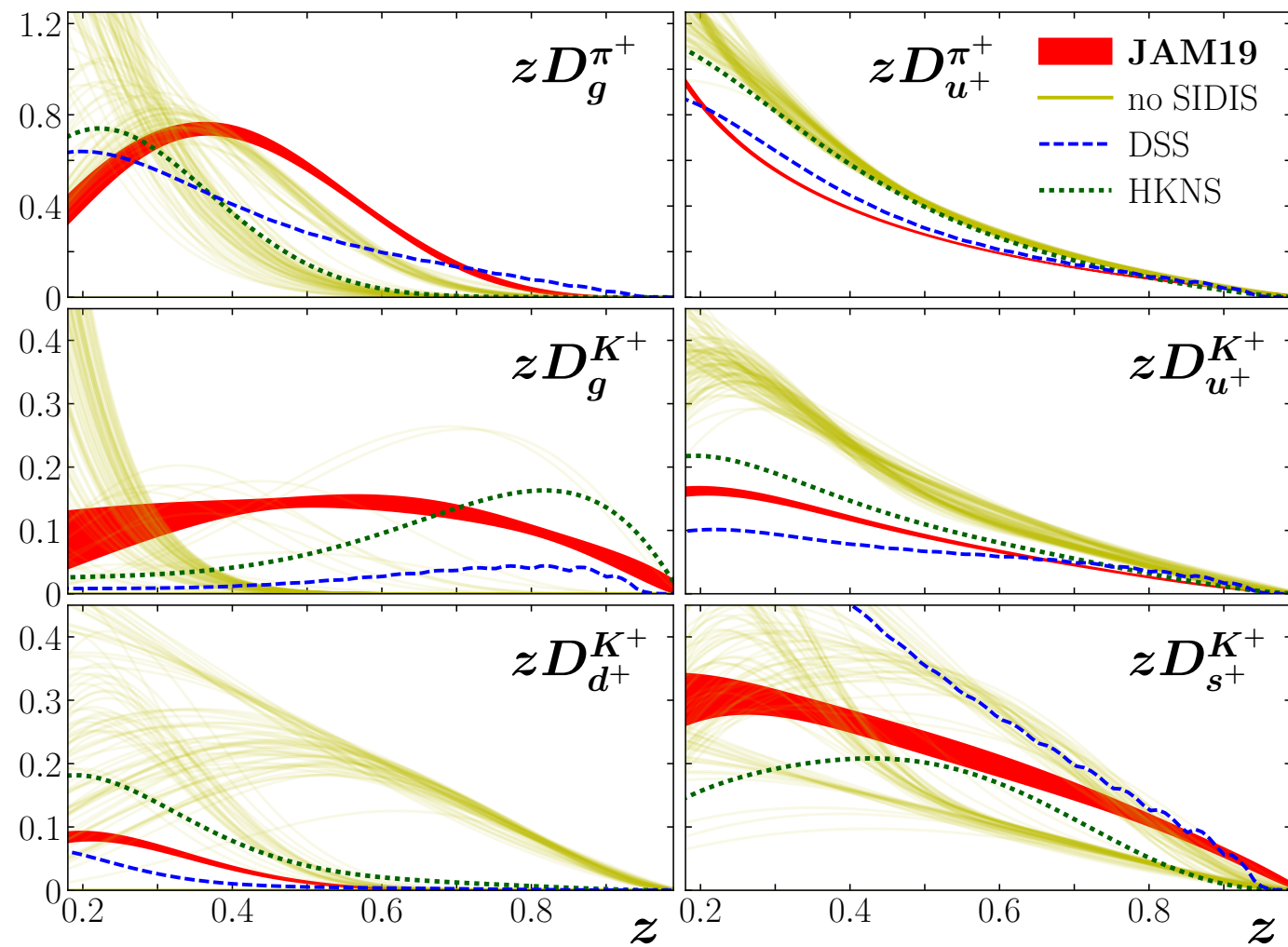
$Q = m_c$

DIS(p, d)
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FF results

JAM19: FF

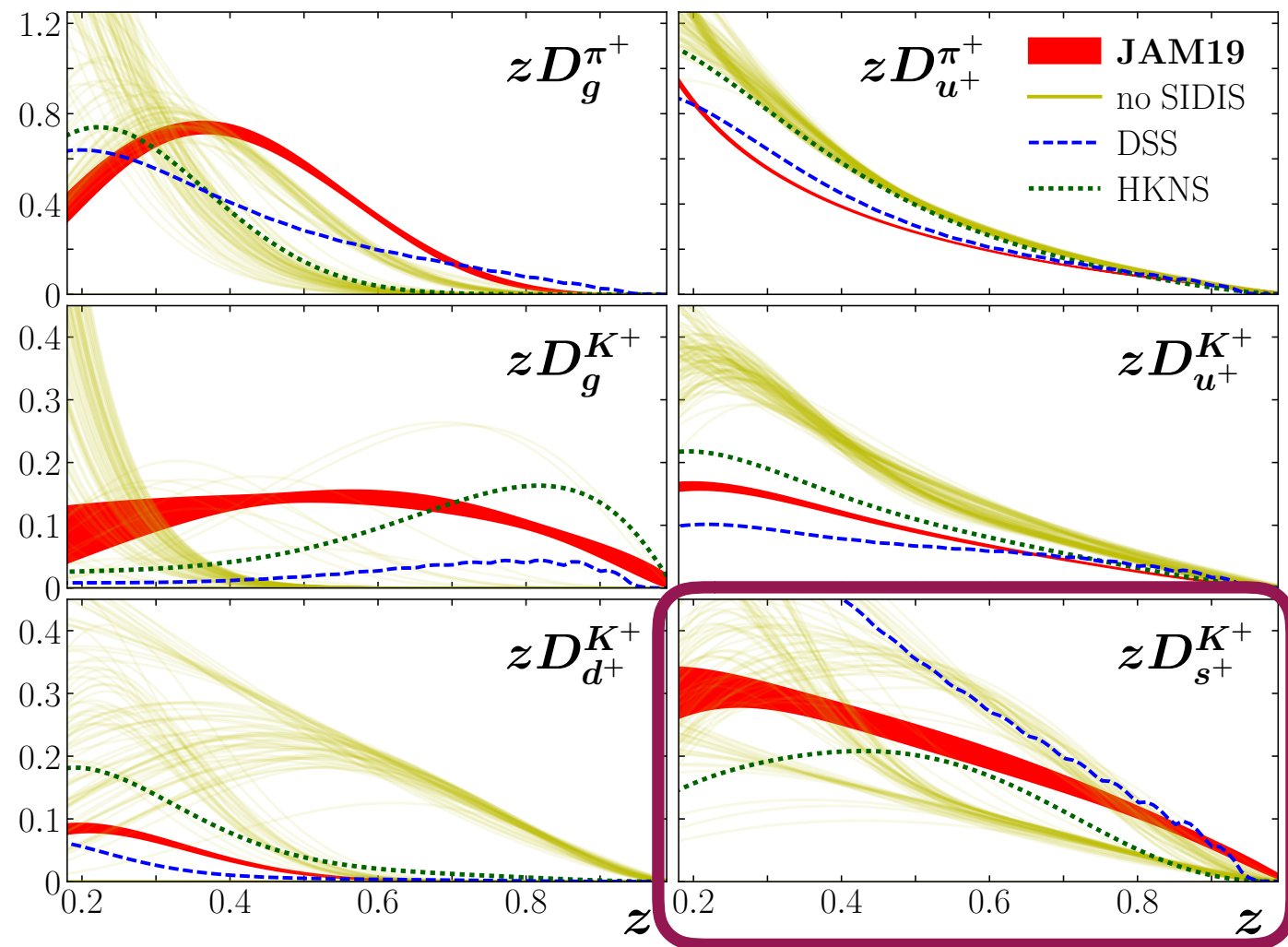
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JAM19: FF

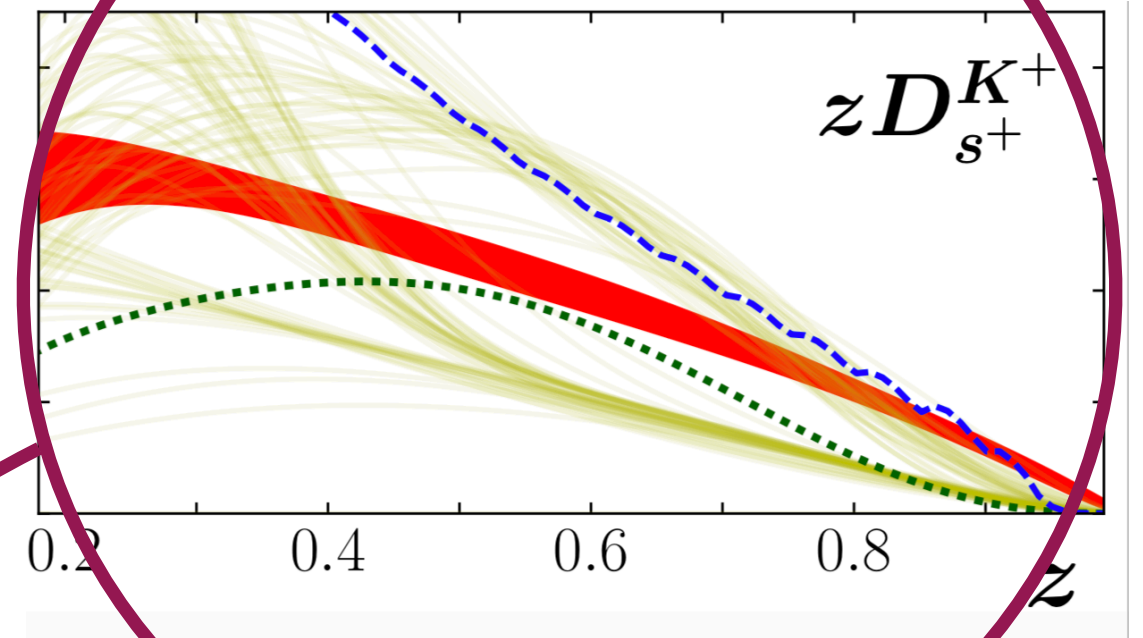
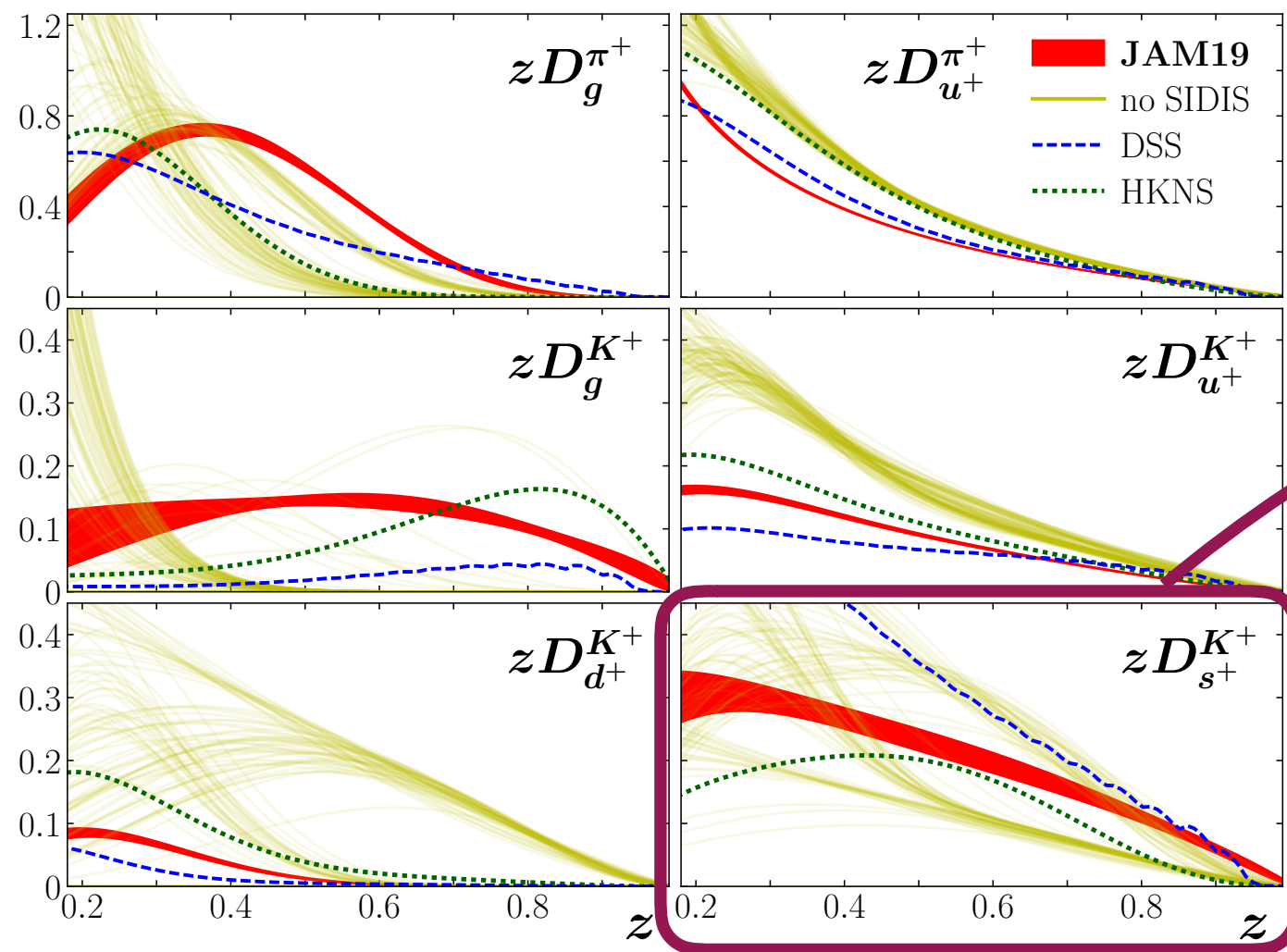
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$$Q = m_c$$

JAM19: FF

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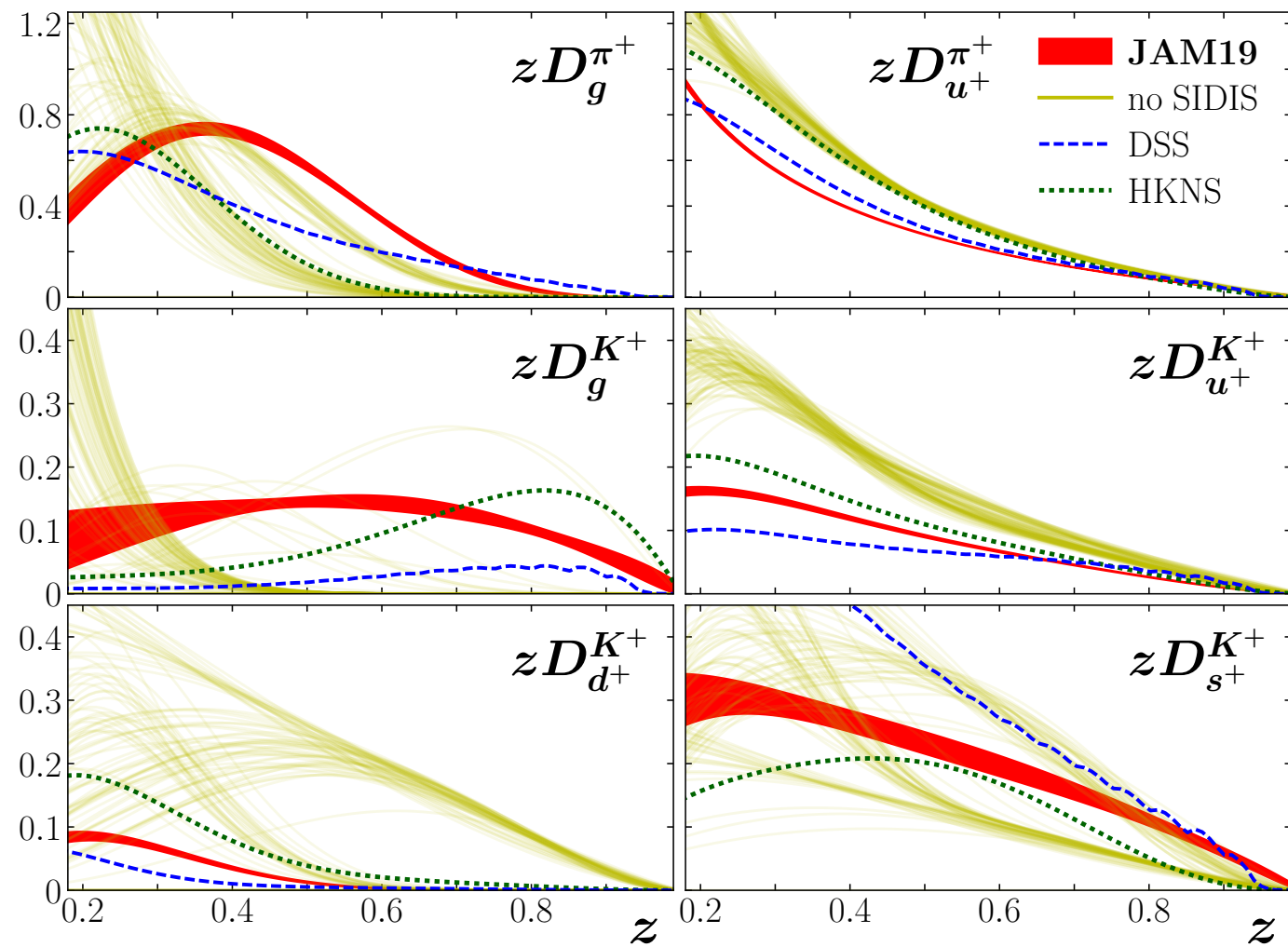


Large $\bar{s} \rightarrow K^+$

$Q = m_c$

JAM19: FF

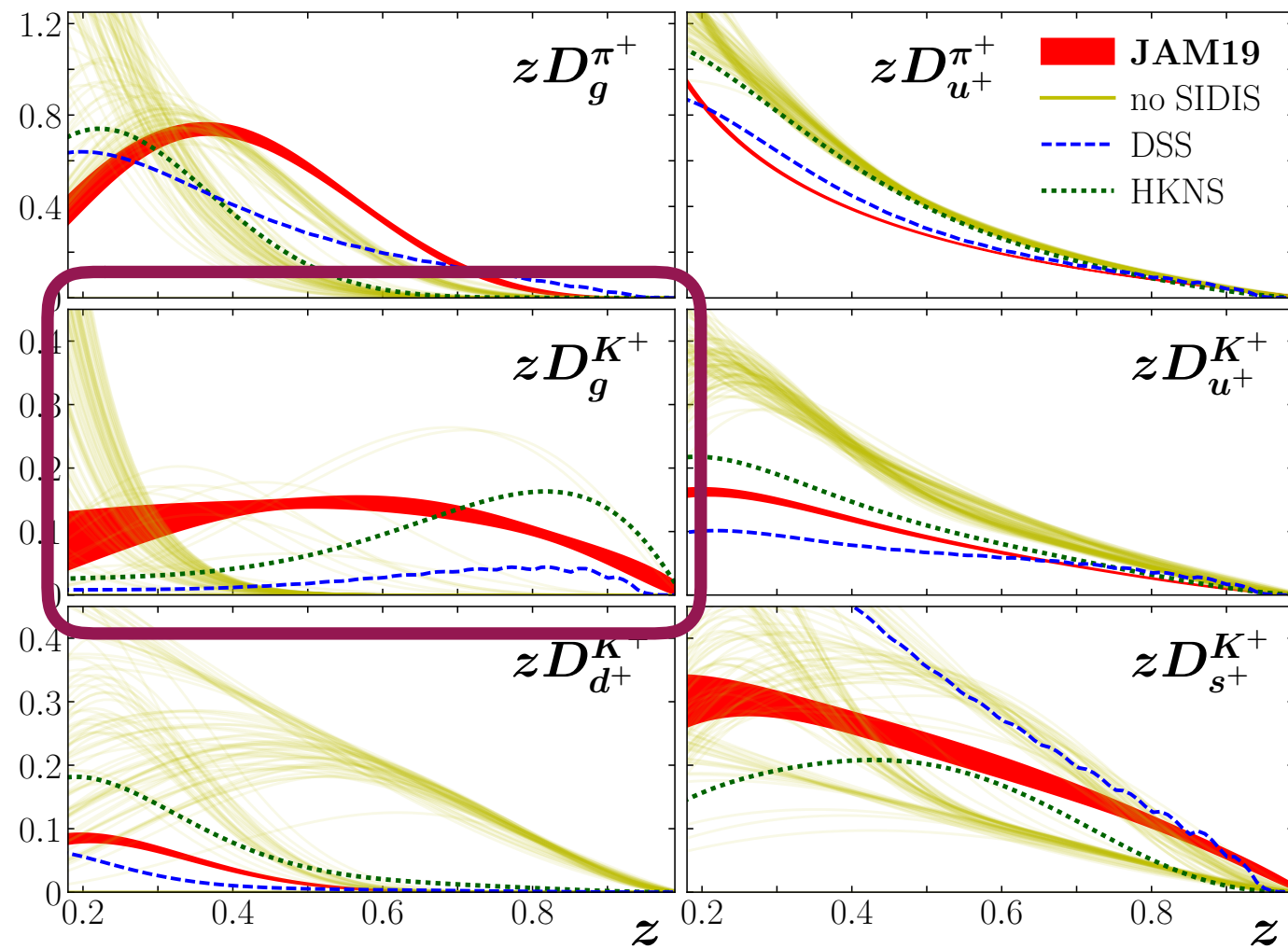
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$$Q = m_c$$

JAM19: FF

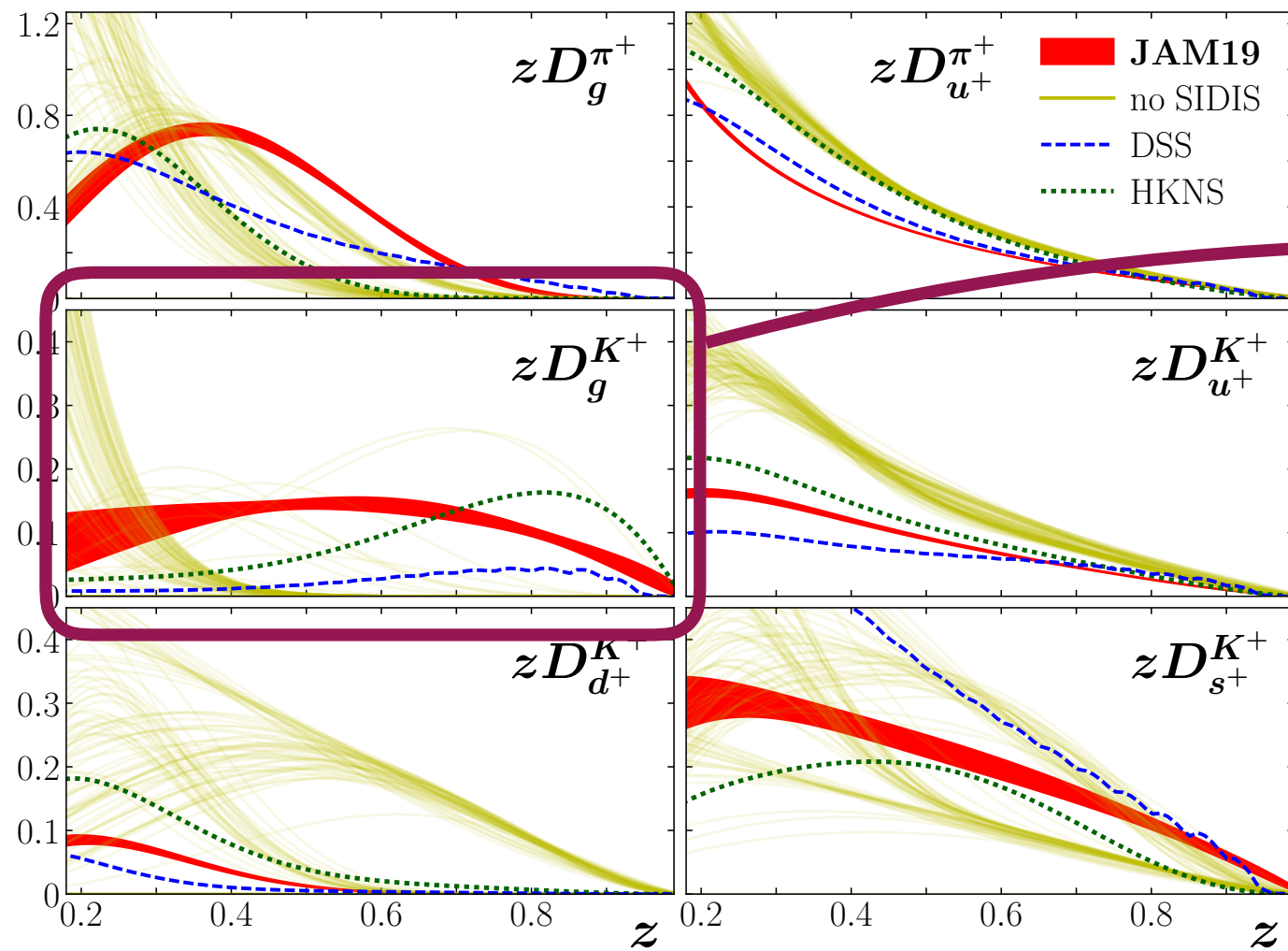
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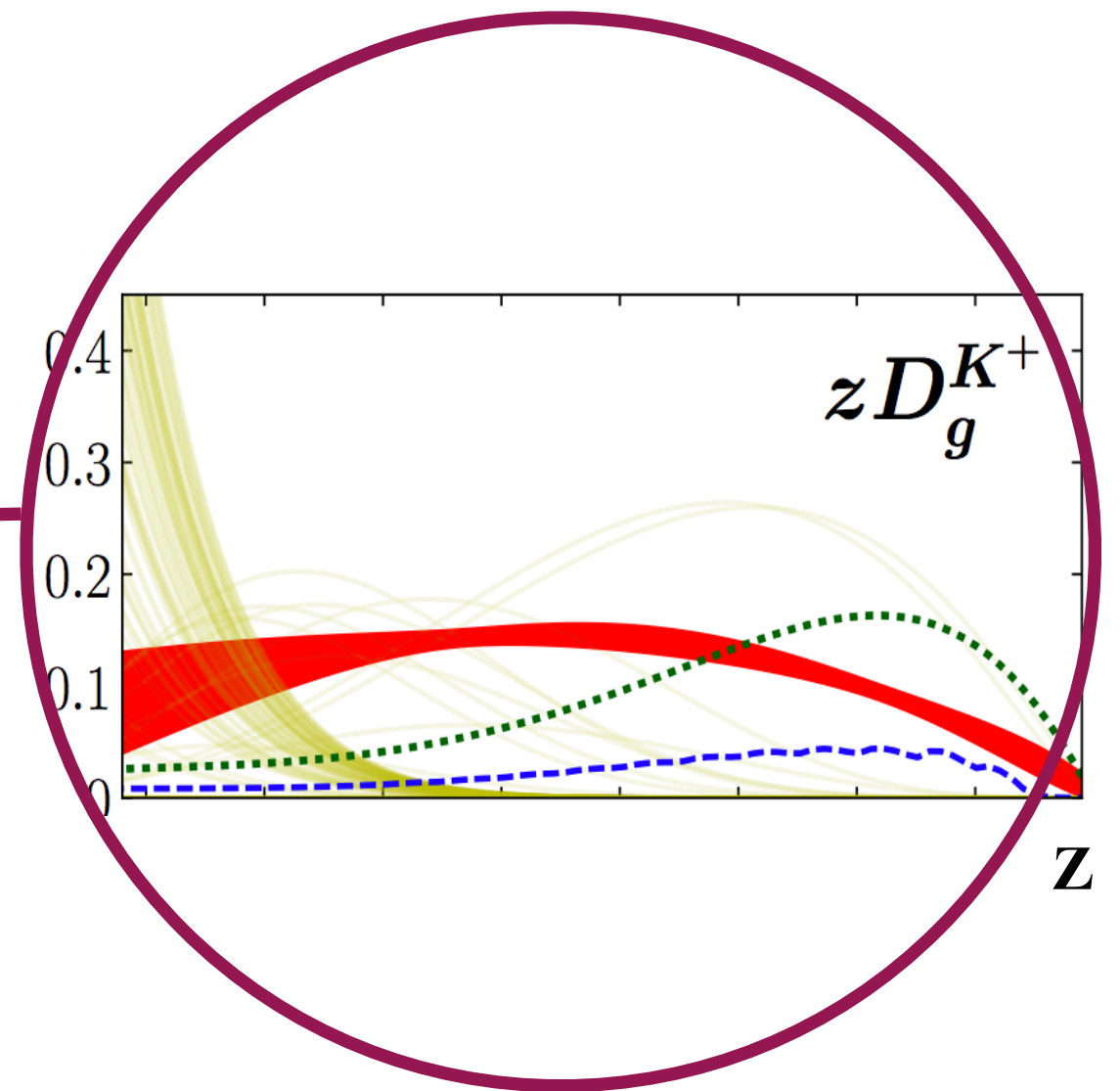
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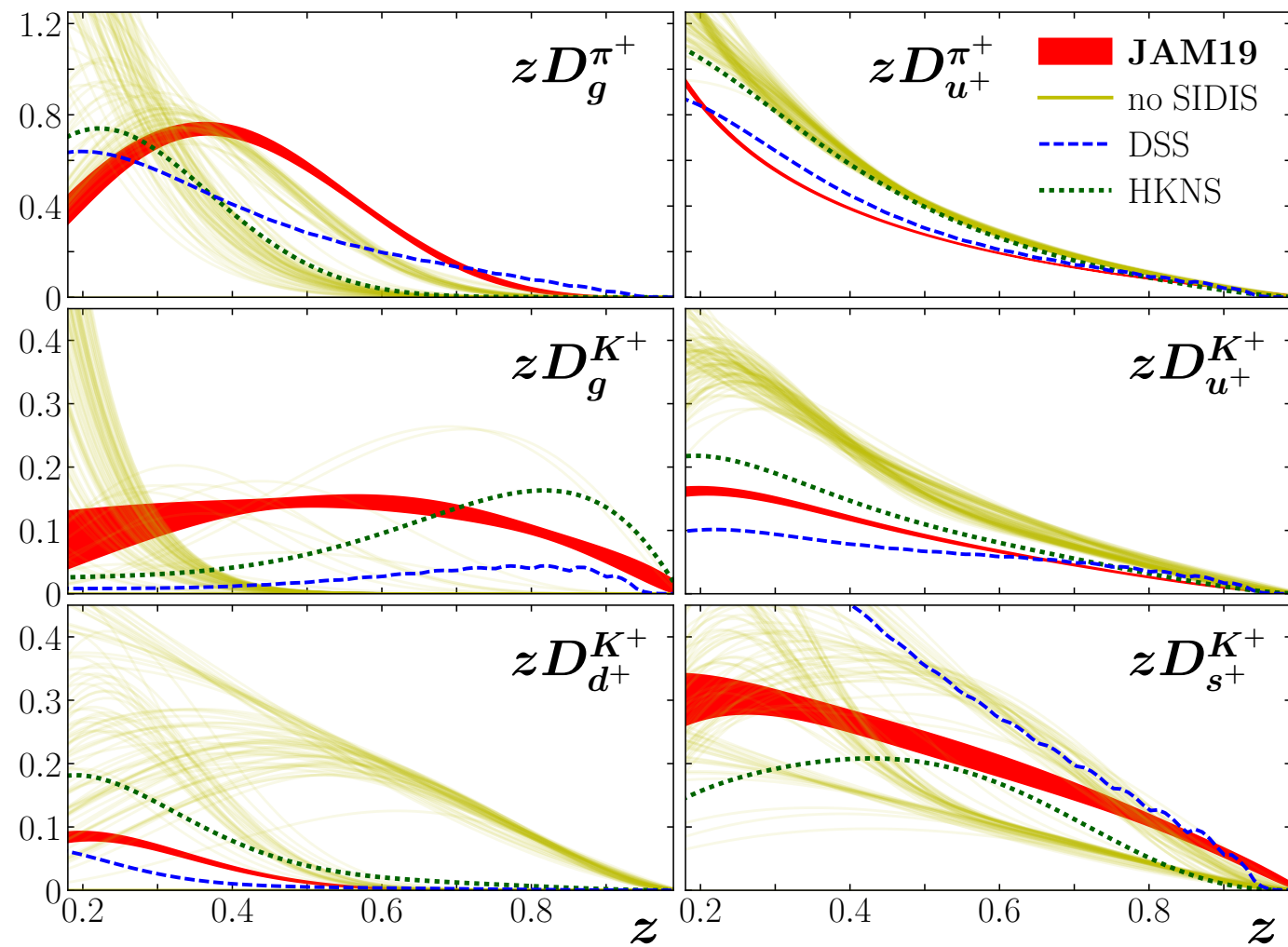
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Constraints on
 $g \rightarrow K^+$

JAM19: FF

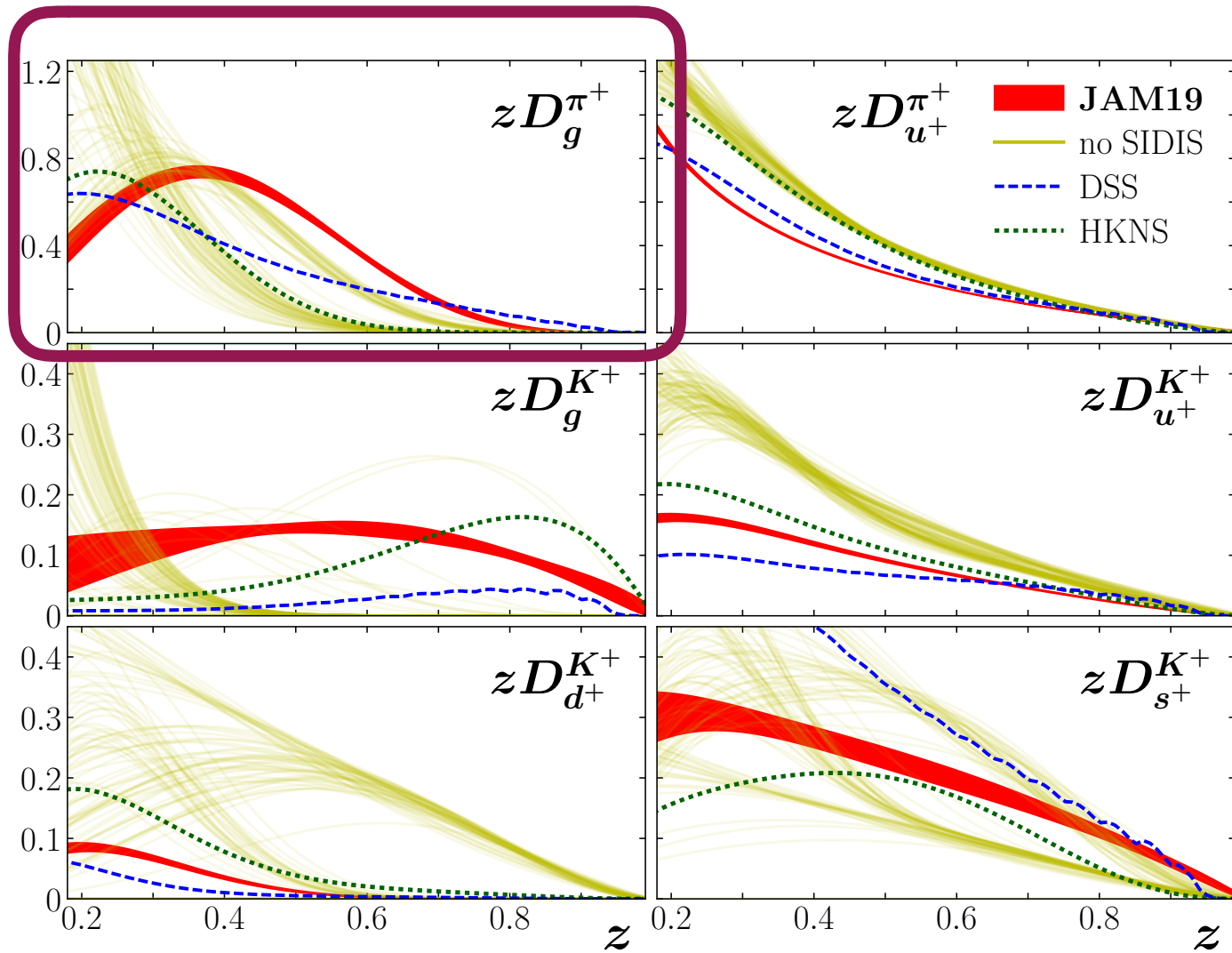
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JAM19: FF

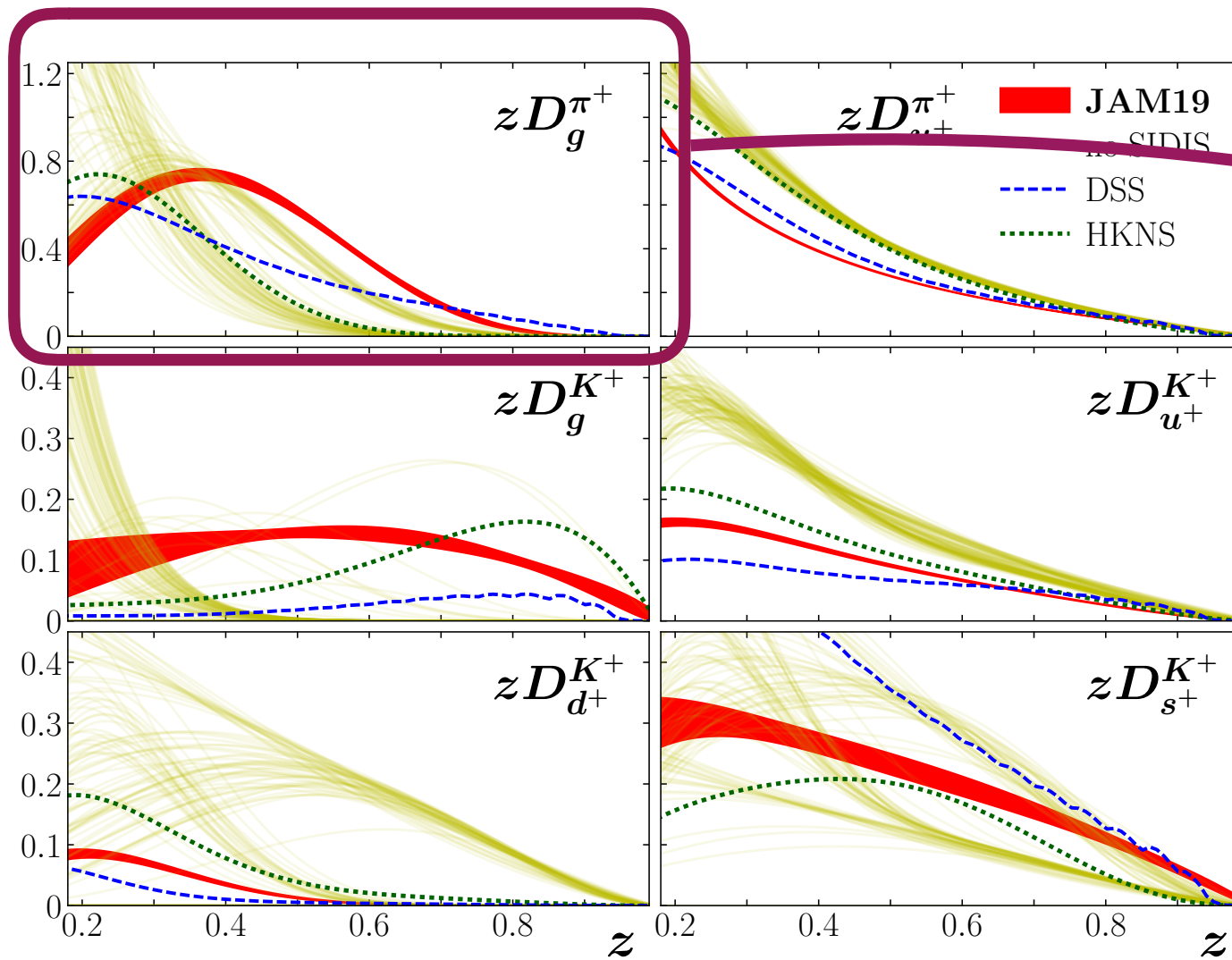
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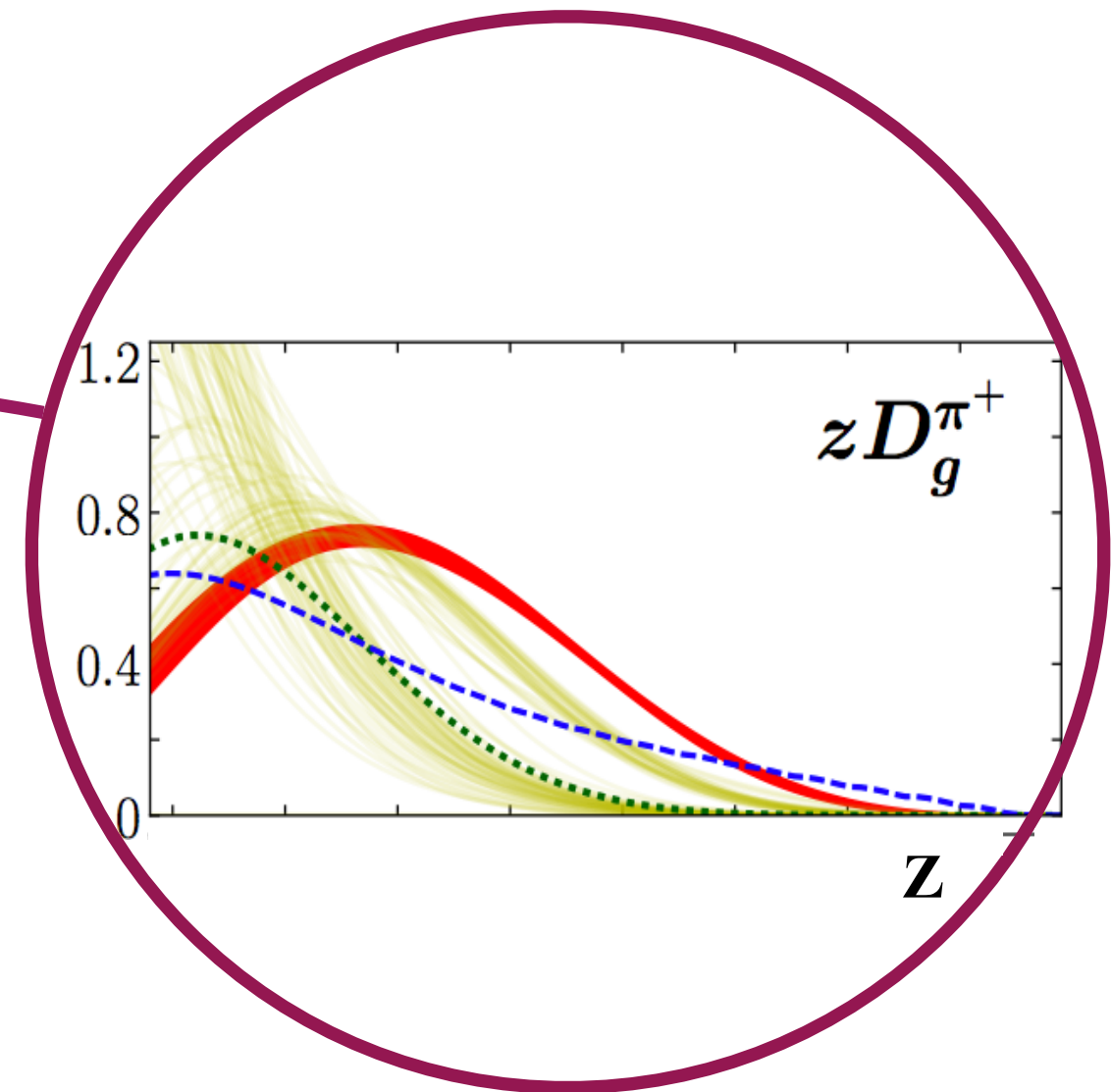
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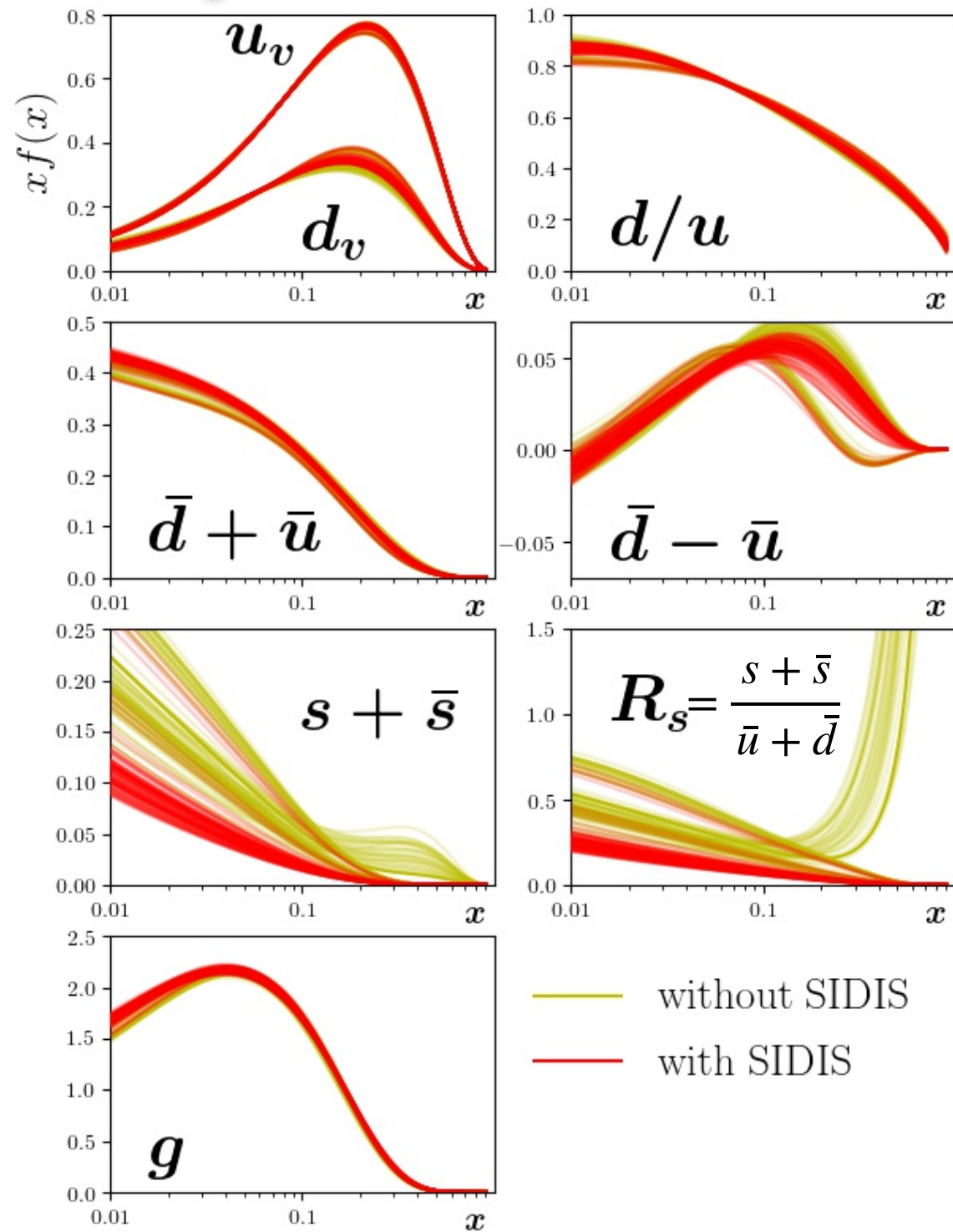


Constraints on

$g \rightarrow \pi^+$

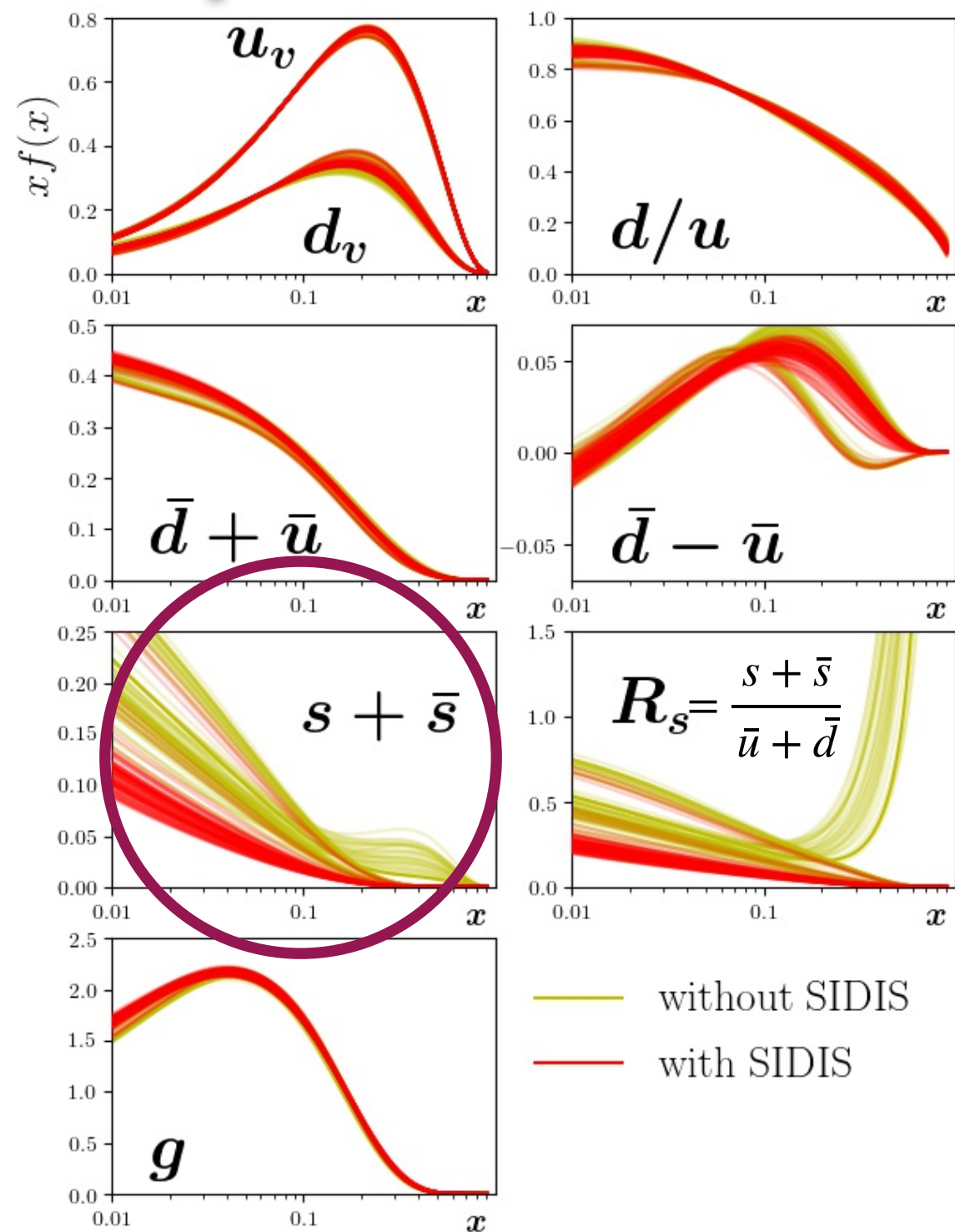
Impact of SIDIS data

Impact of SIDIS data on PDFs



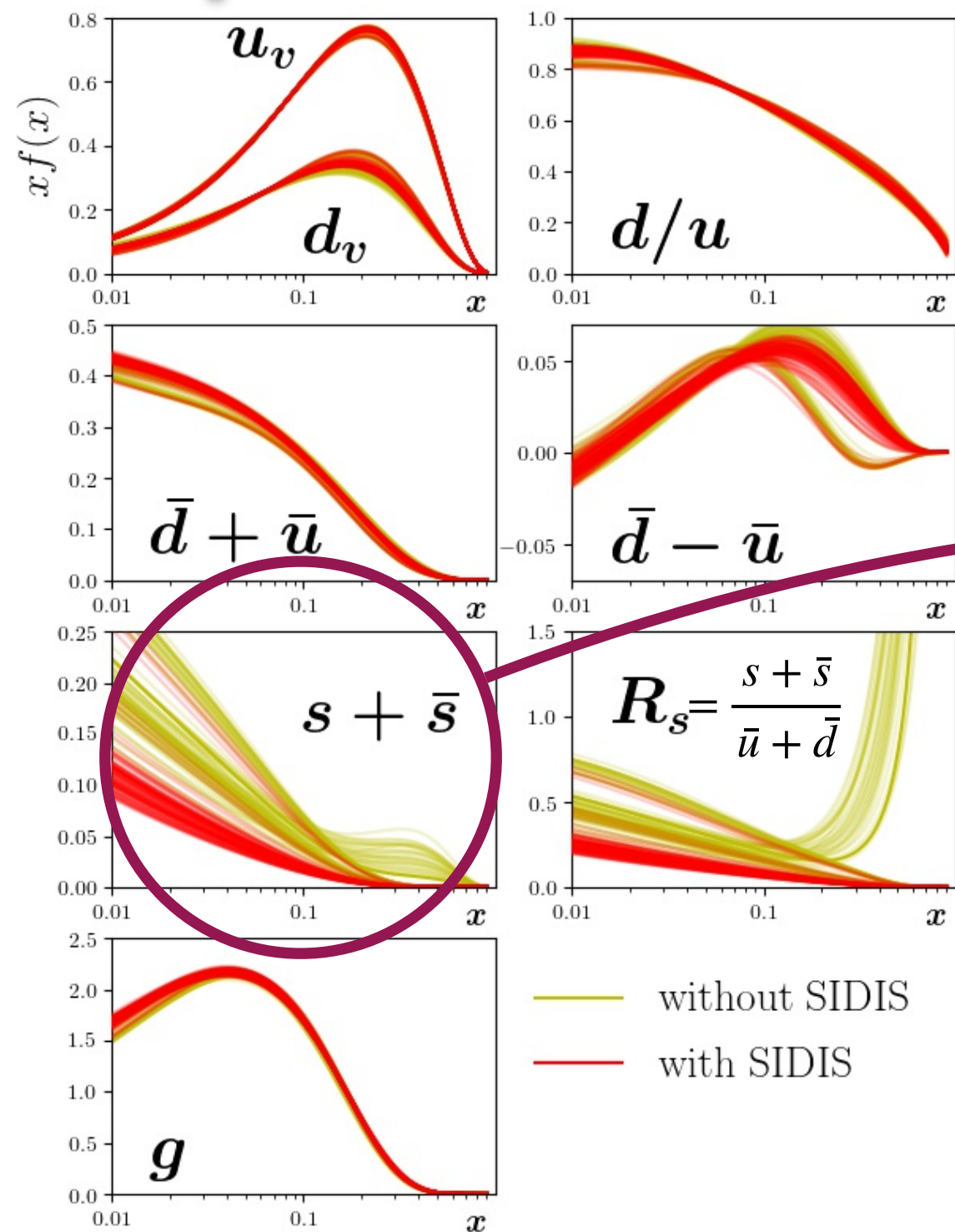
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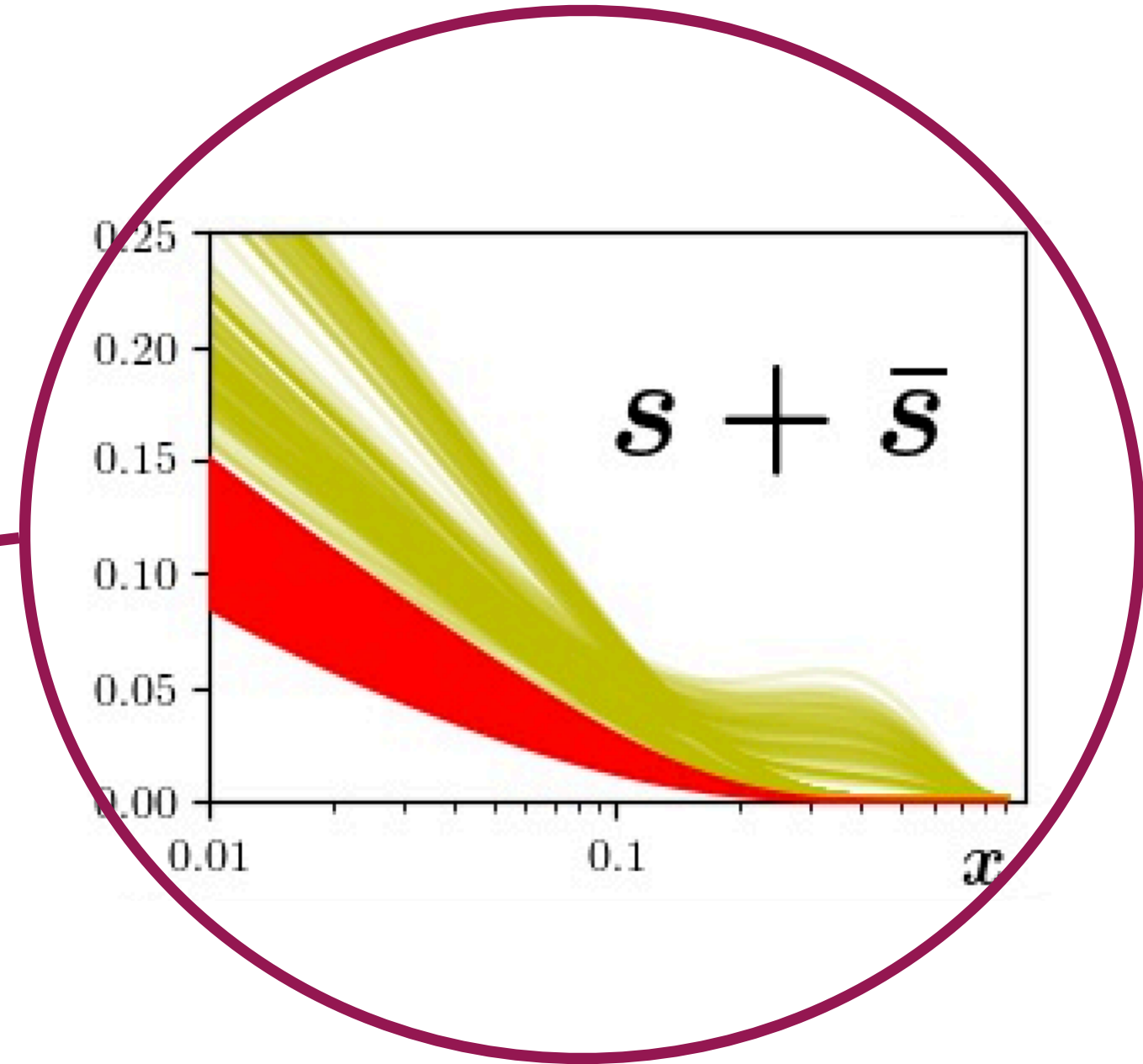


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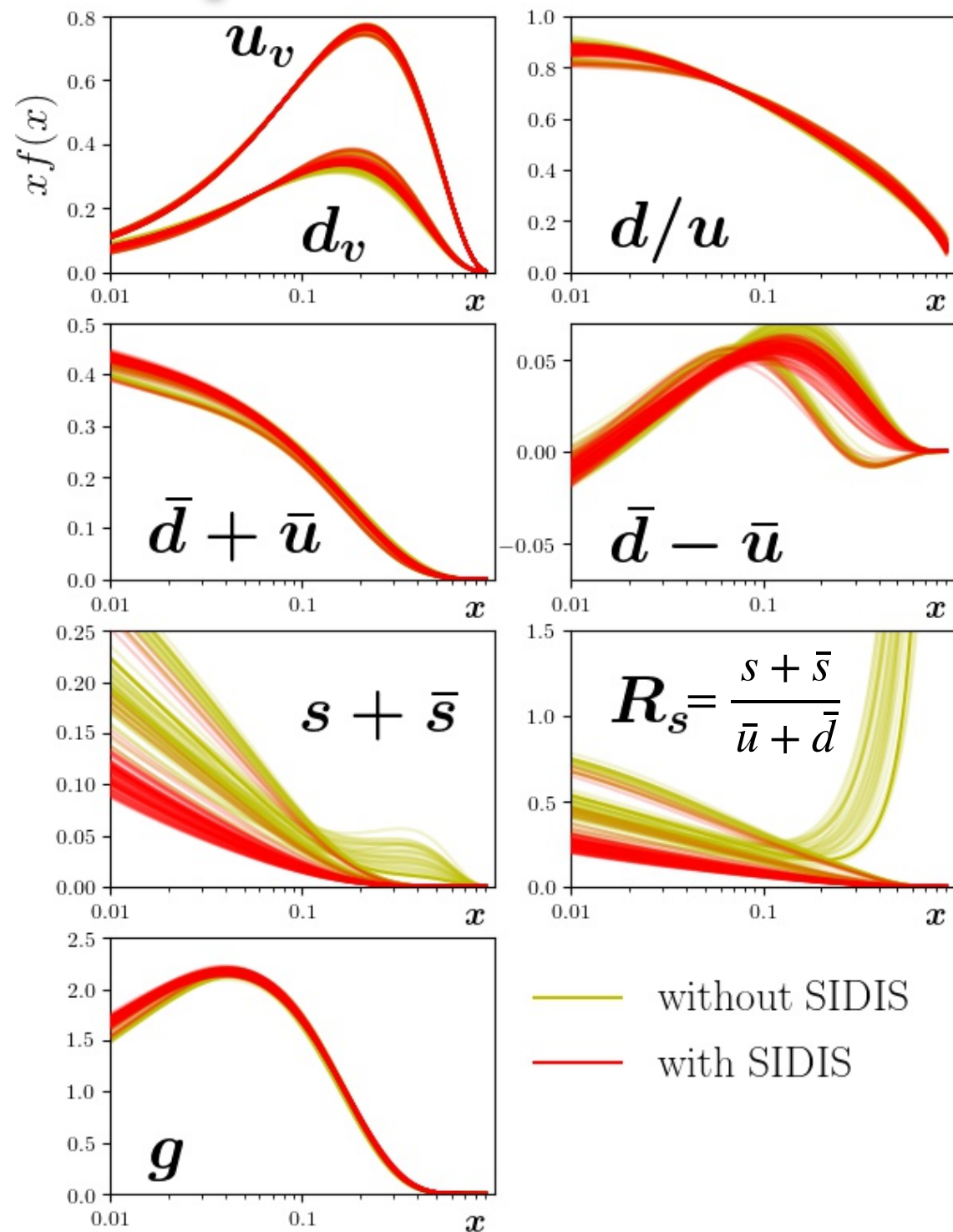


$Q = m_c$



Strong strange
suppression

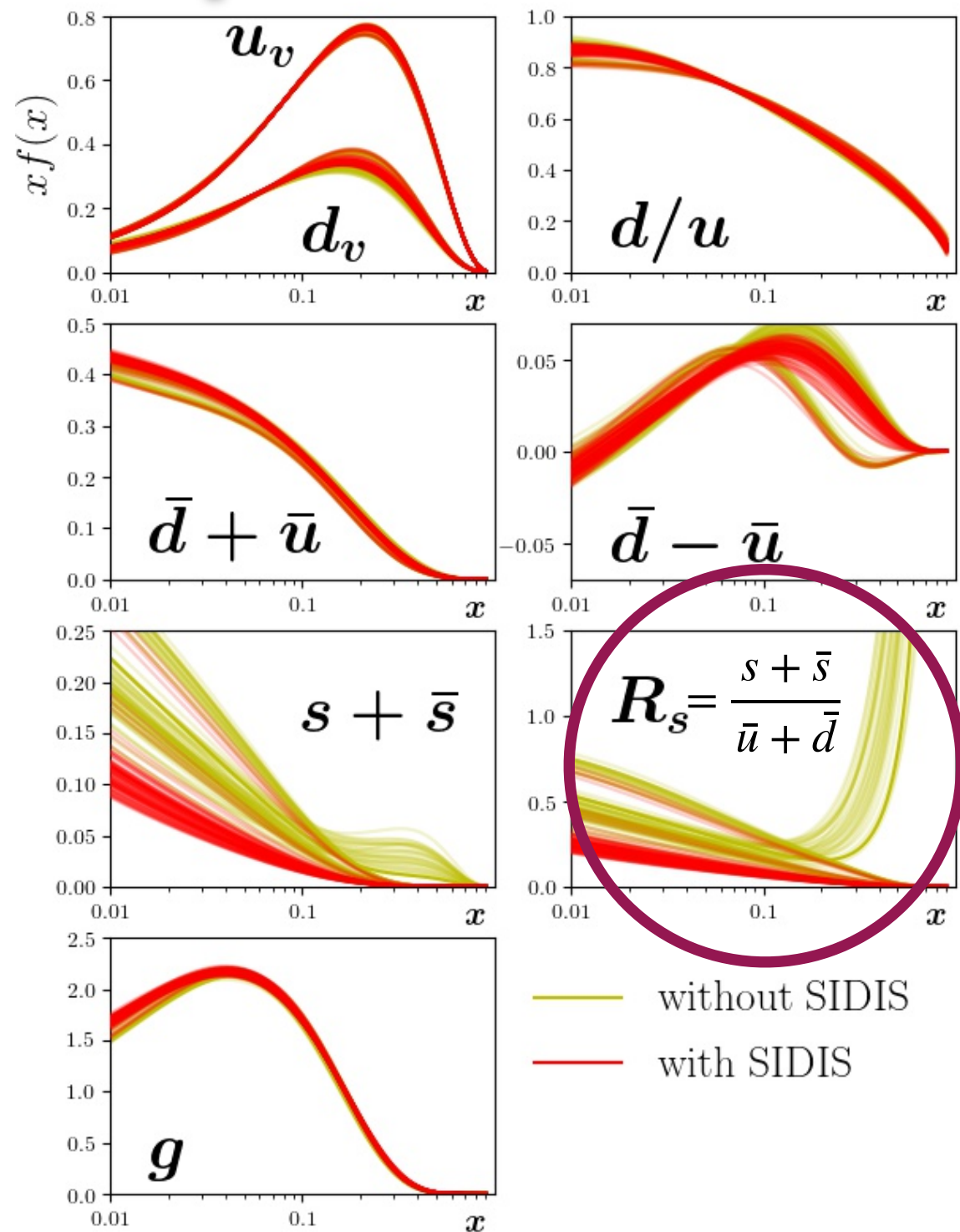
Impact of SIDIS data on PDFs



$$= \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

$Q = m_c$

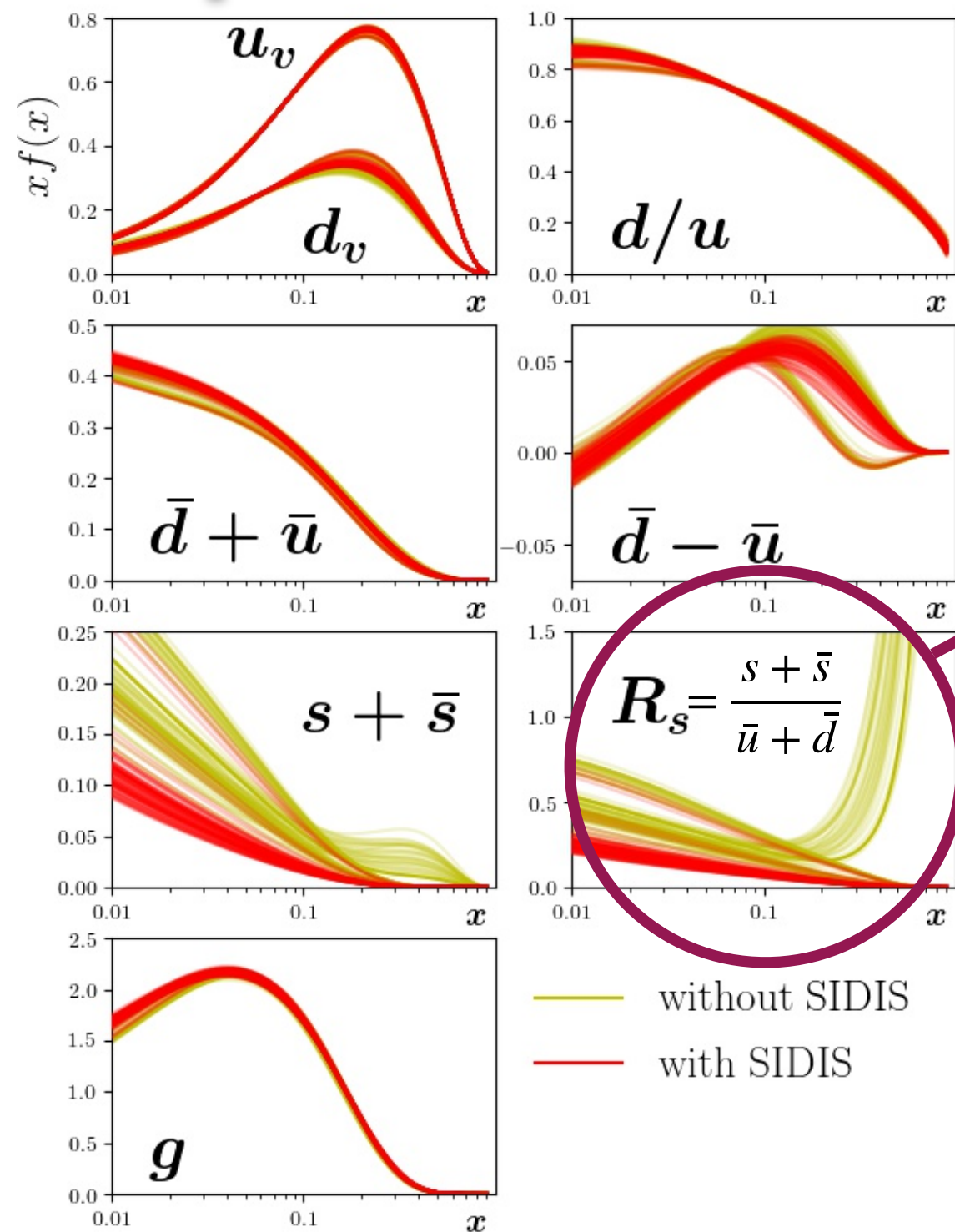
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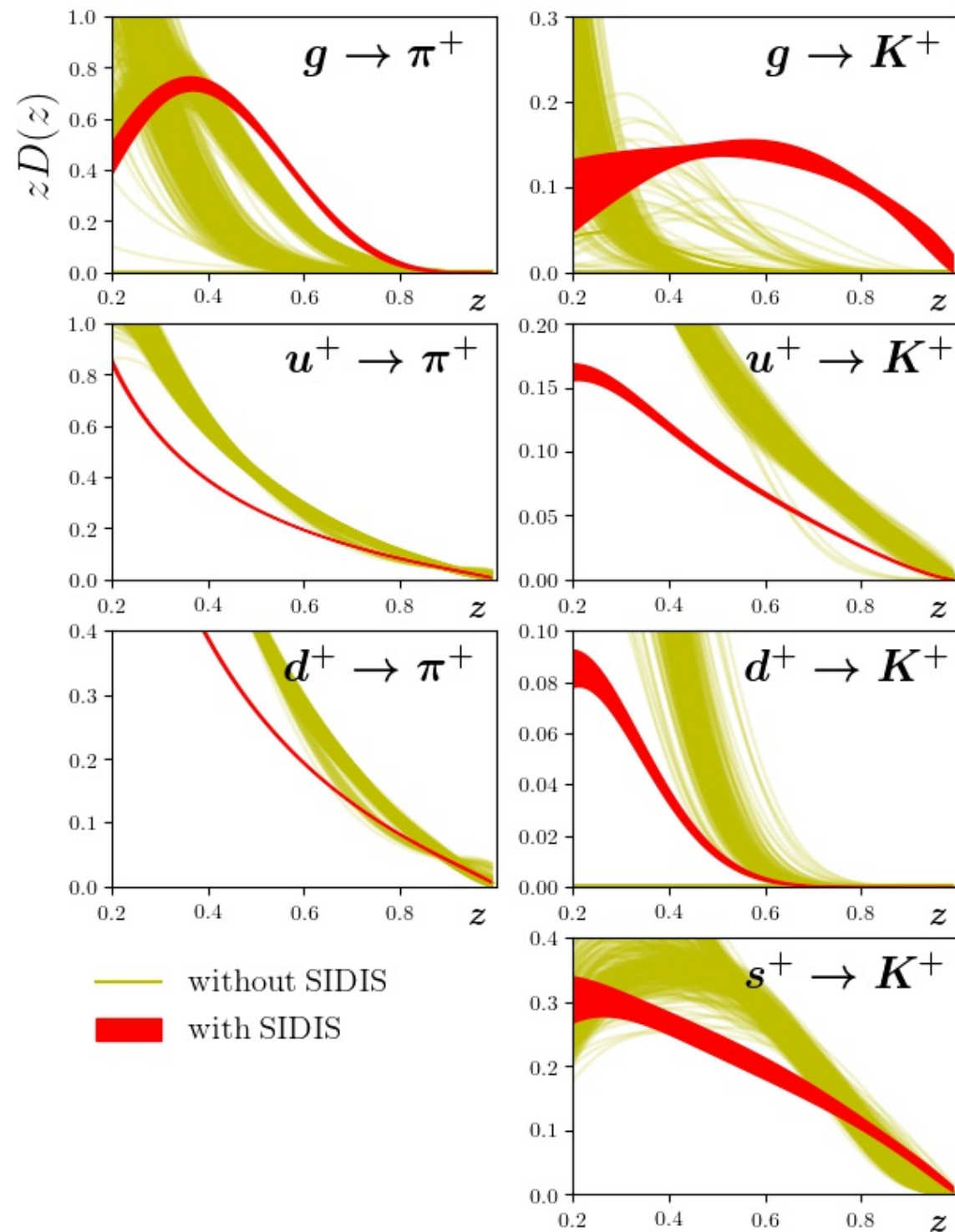
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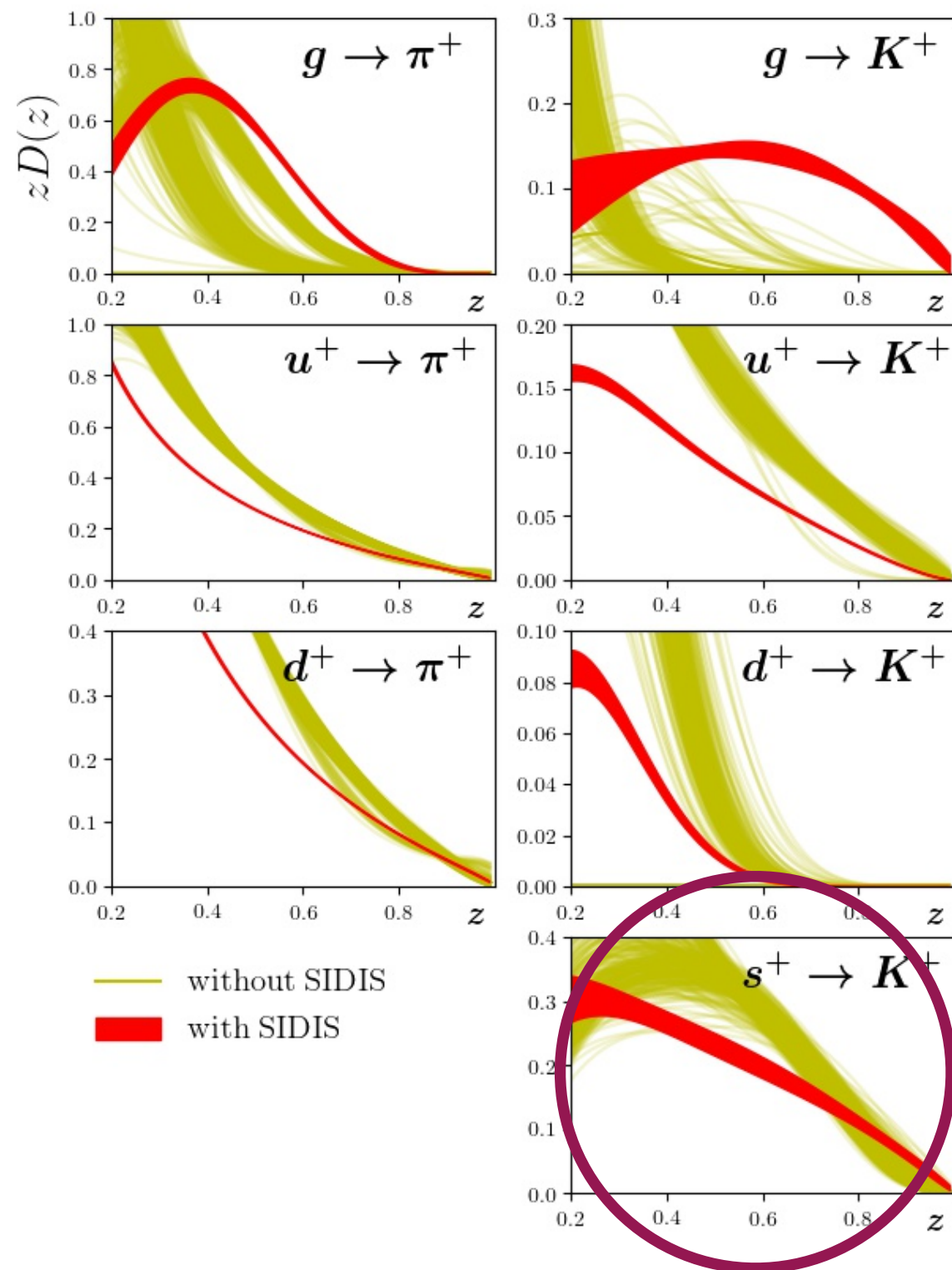
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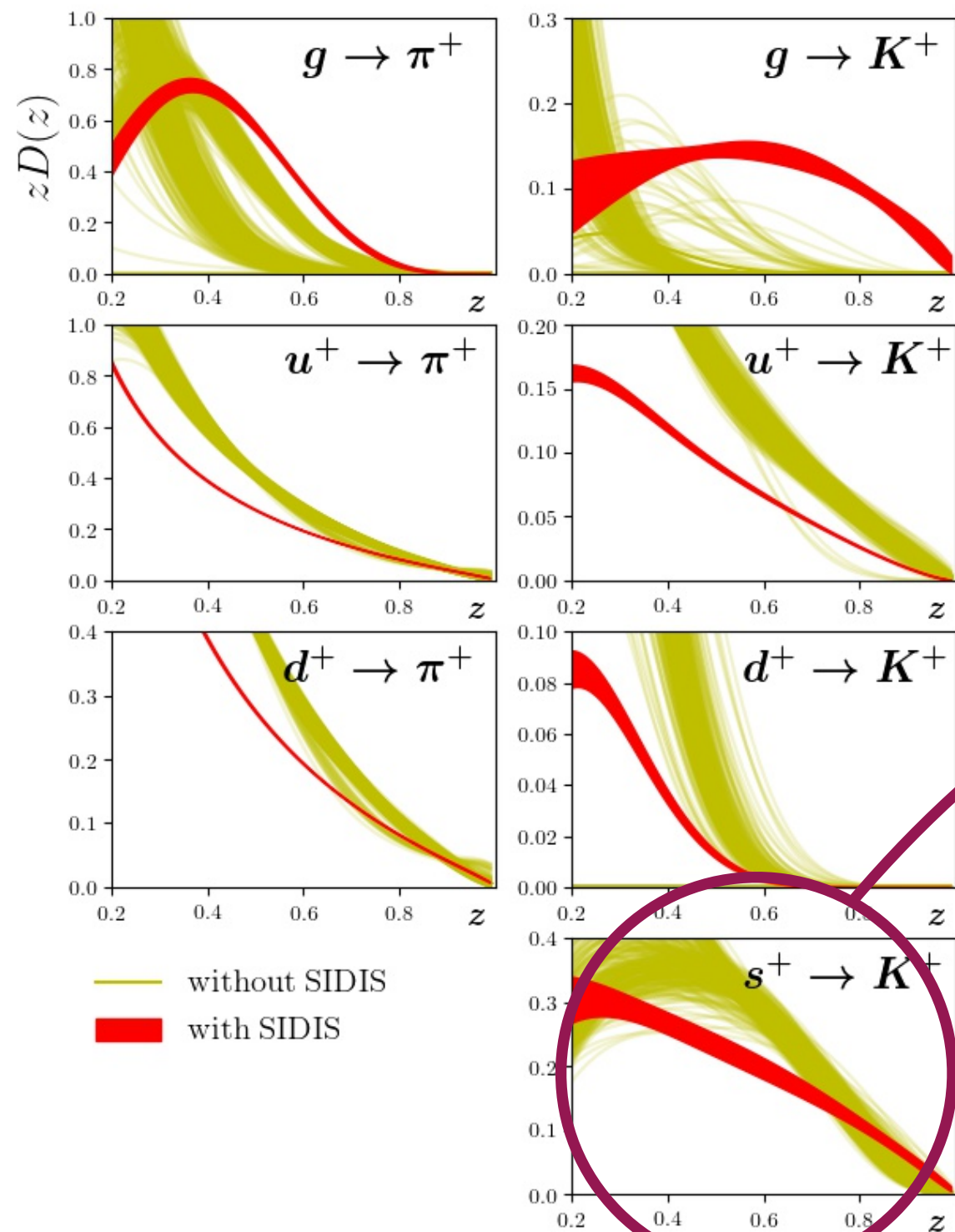
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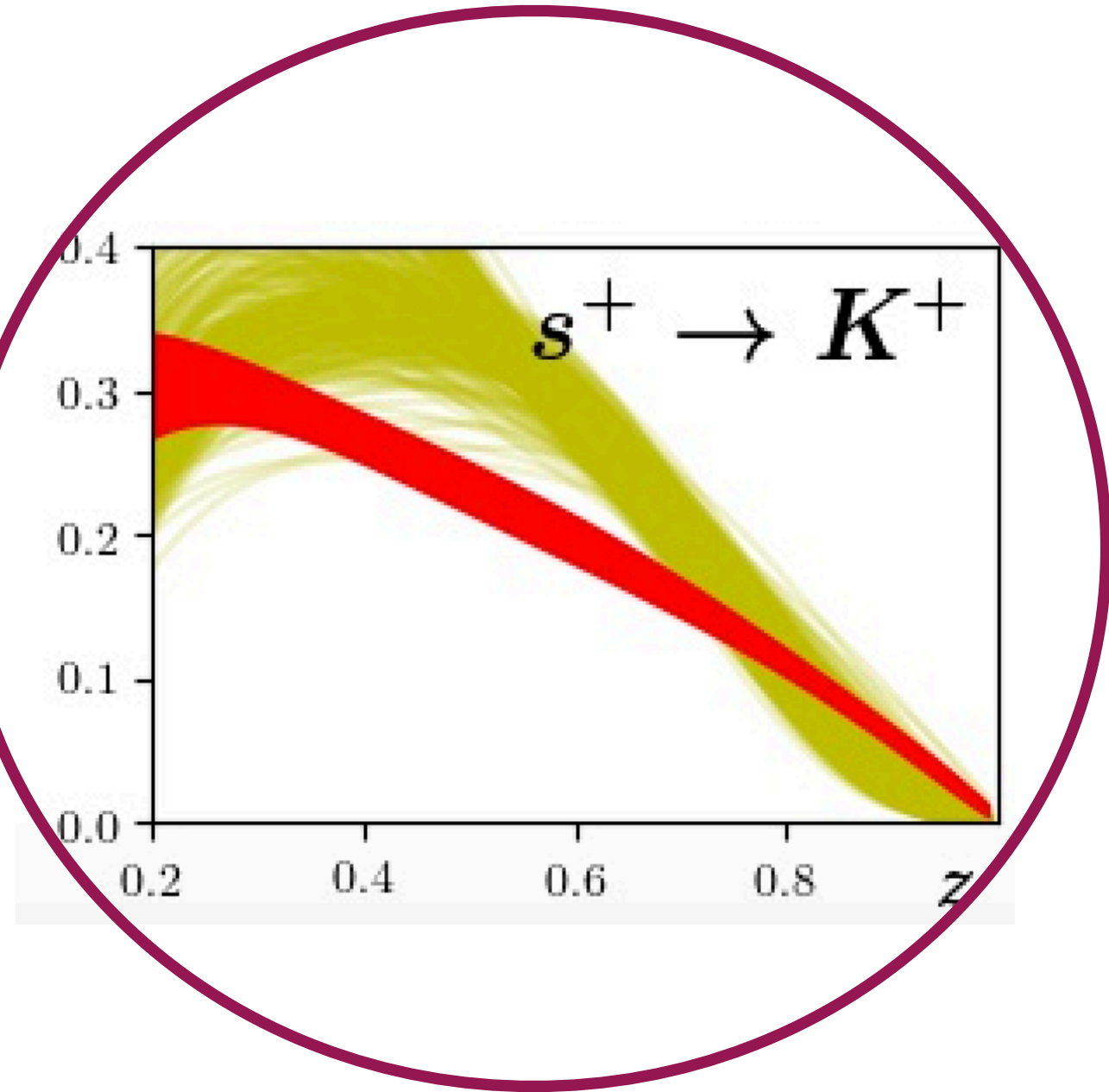


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Impact of SIDIS data on FF

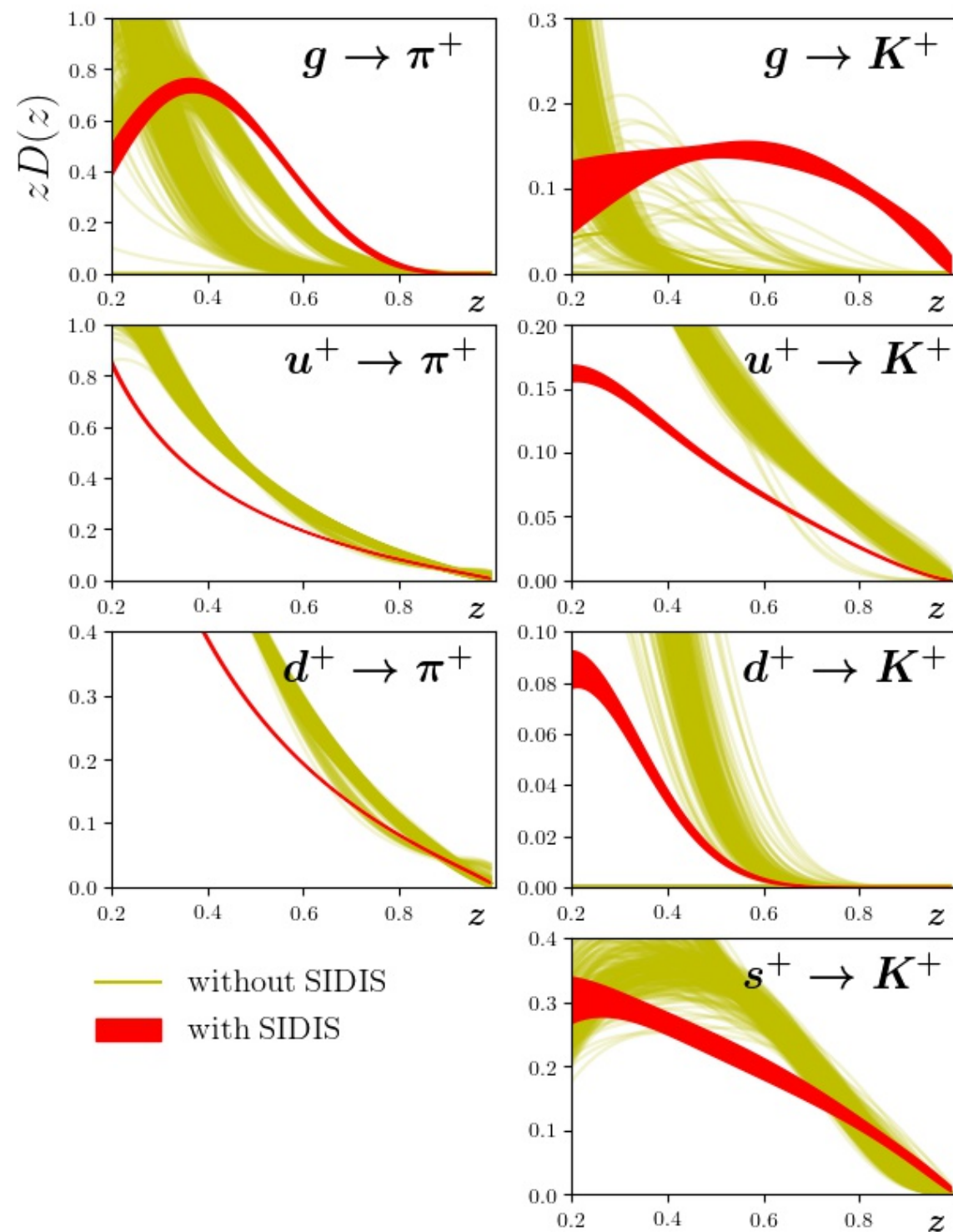


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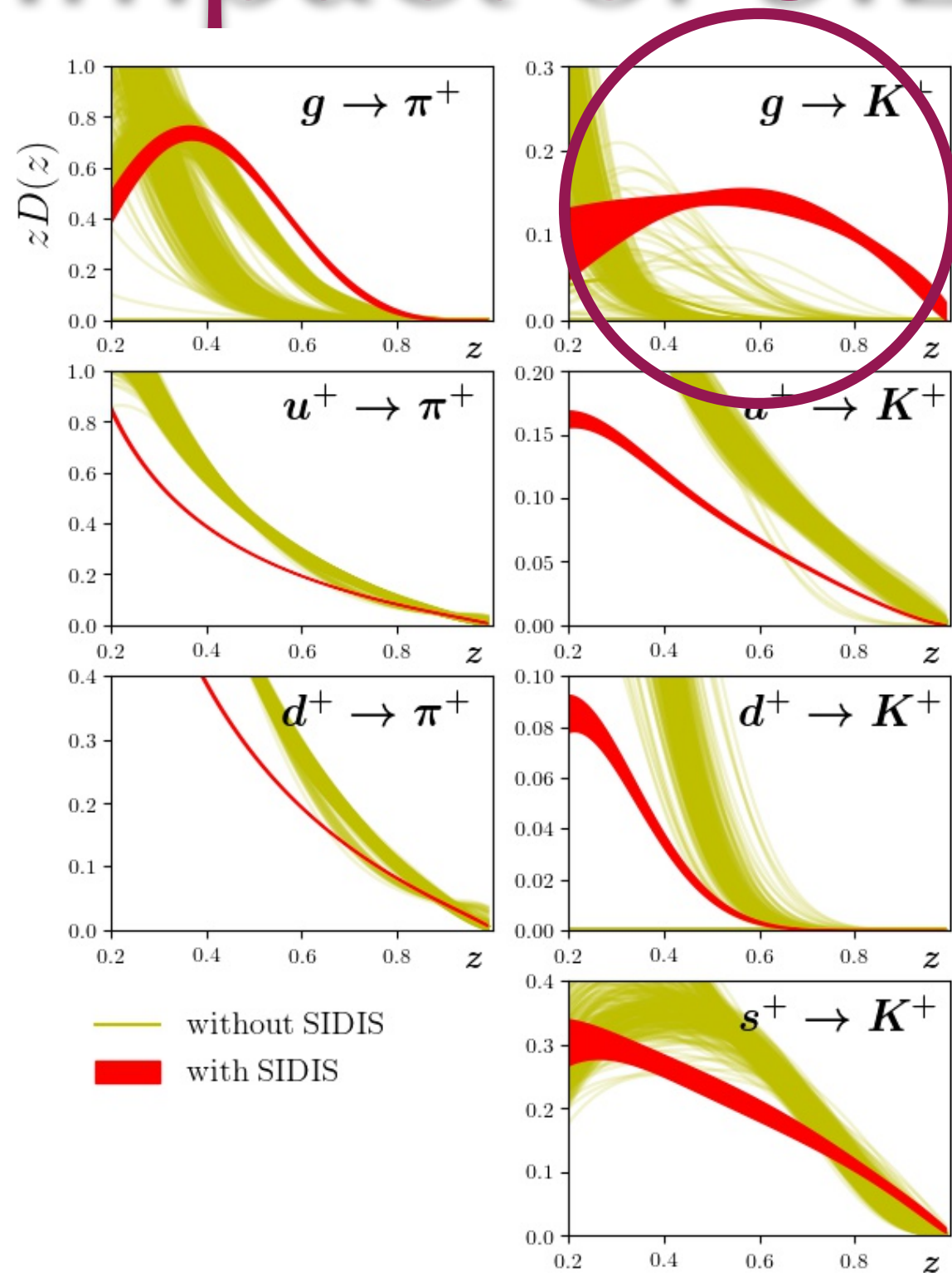
Constraints on
 $s^+ \rightarrow K^+$

Impact of SIDIS data on FF



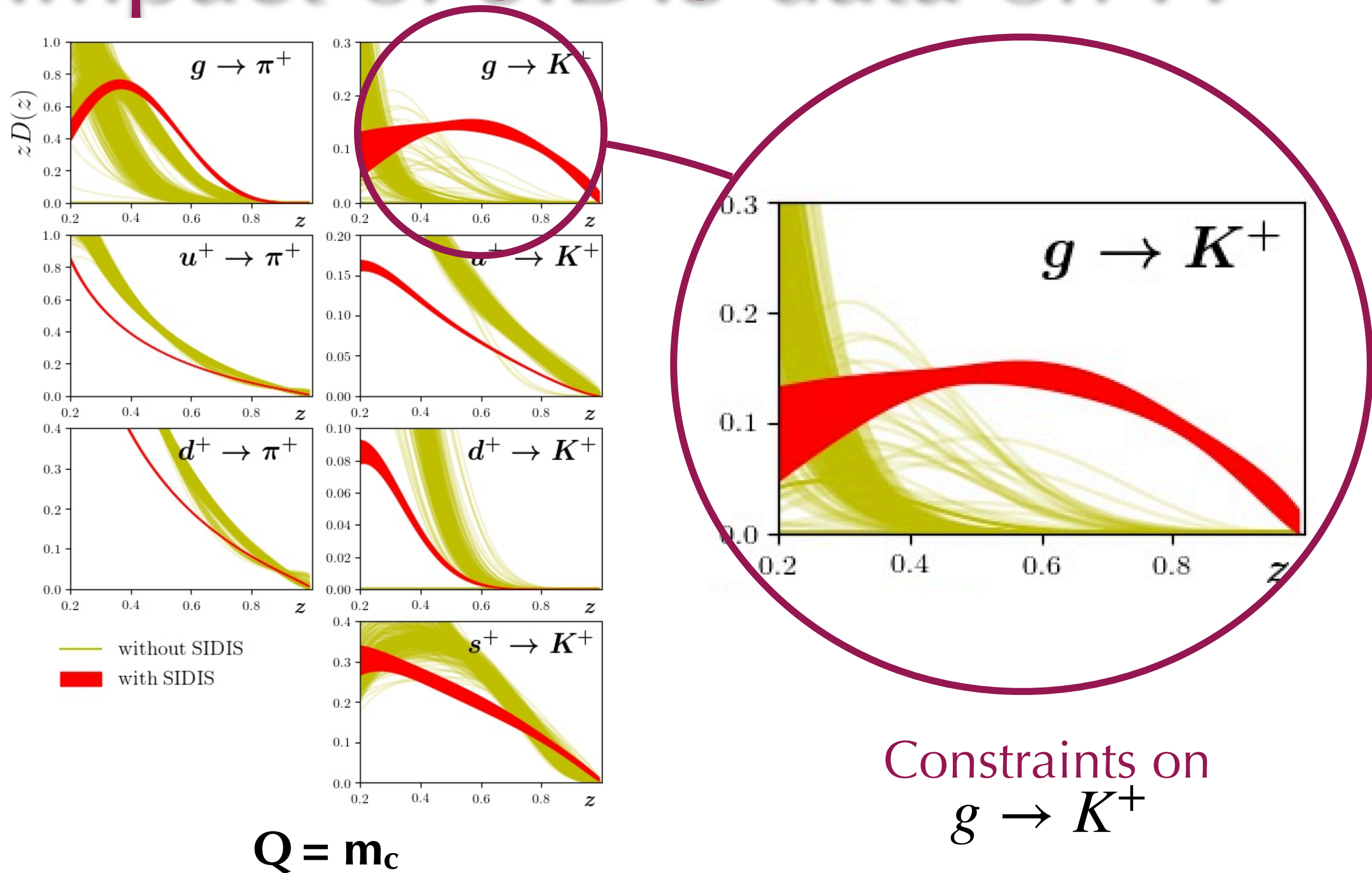
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Impact of SIDIS data on FF

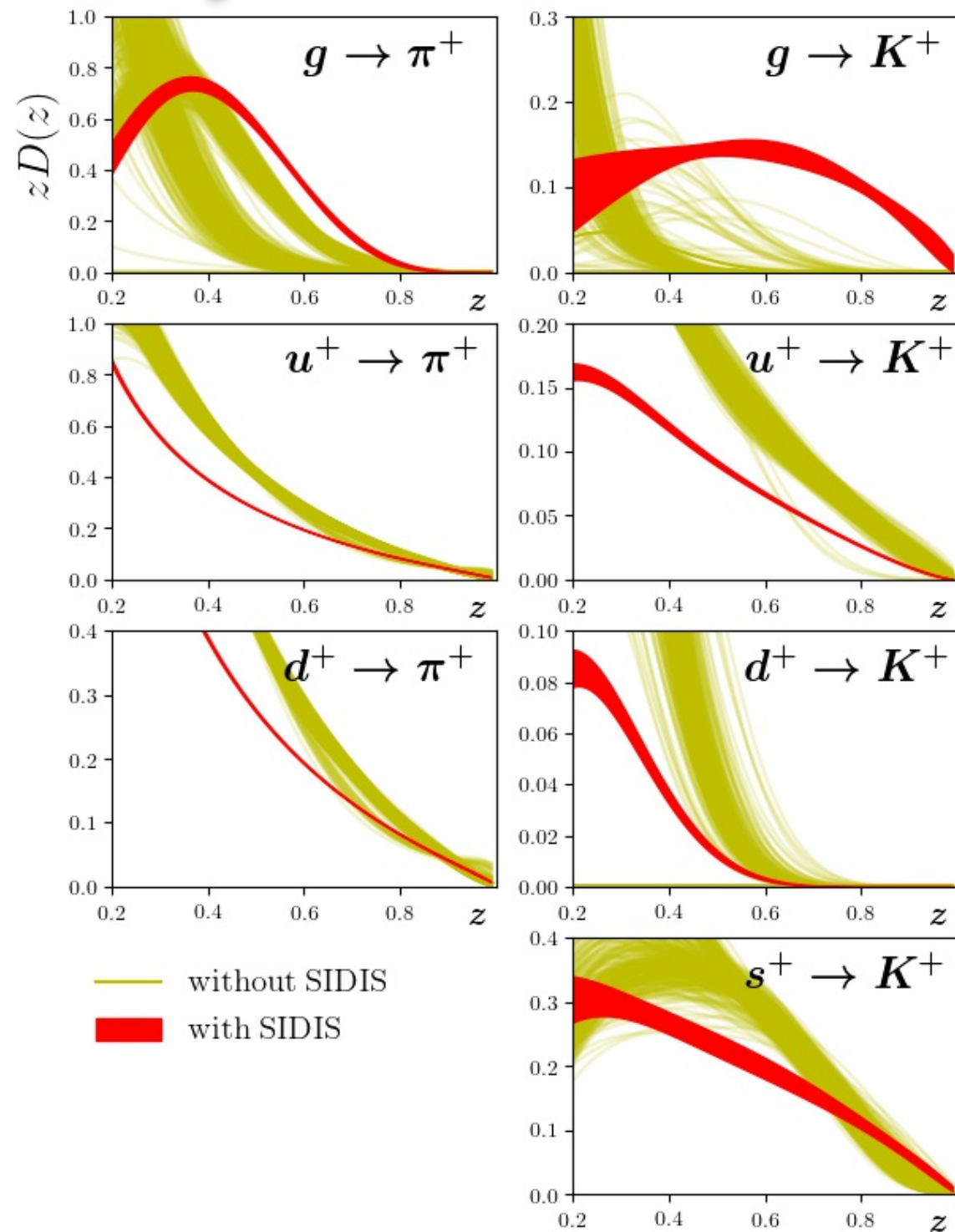


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Impact of SIDIS data on FF

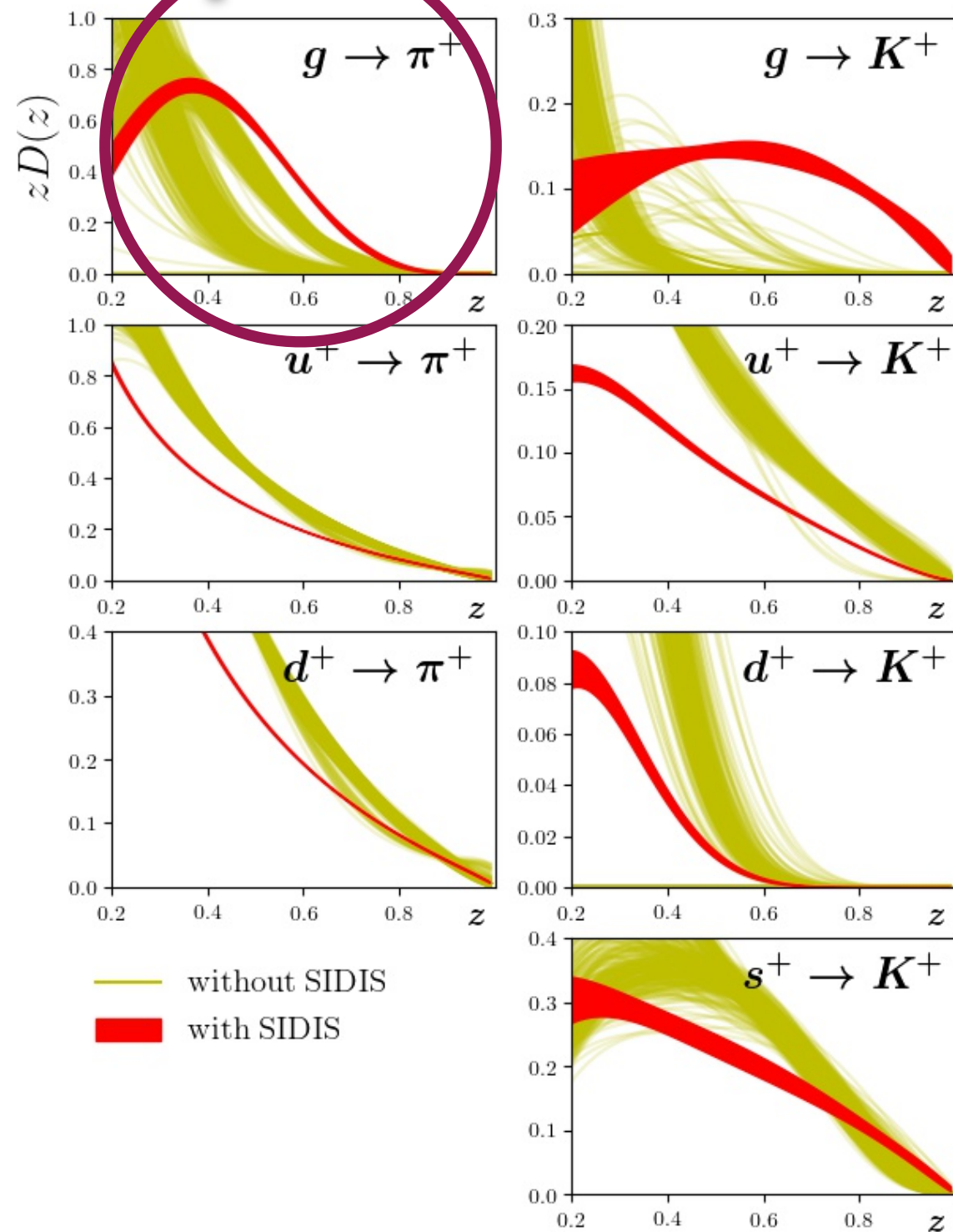


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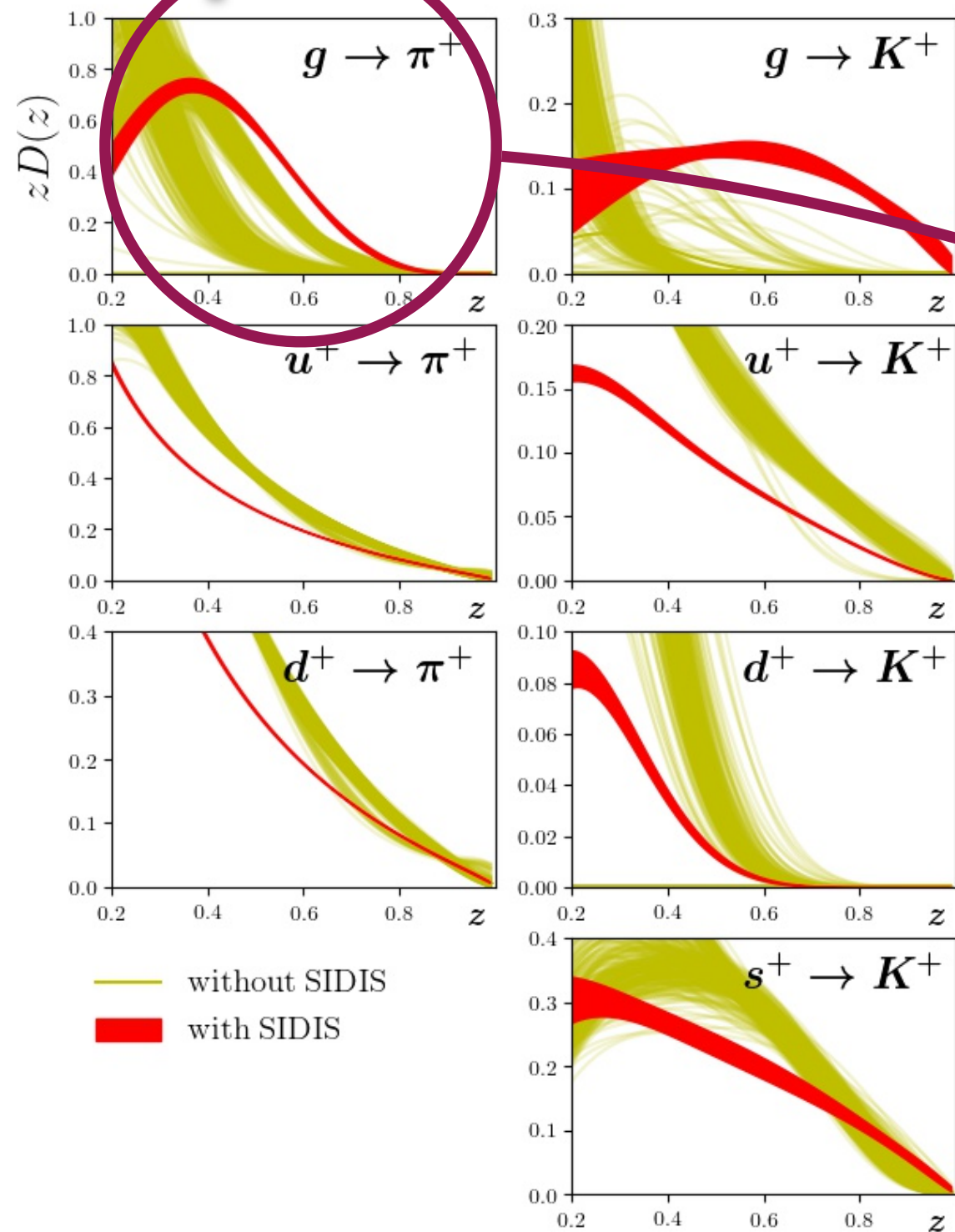
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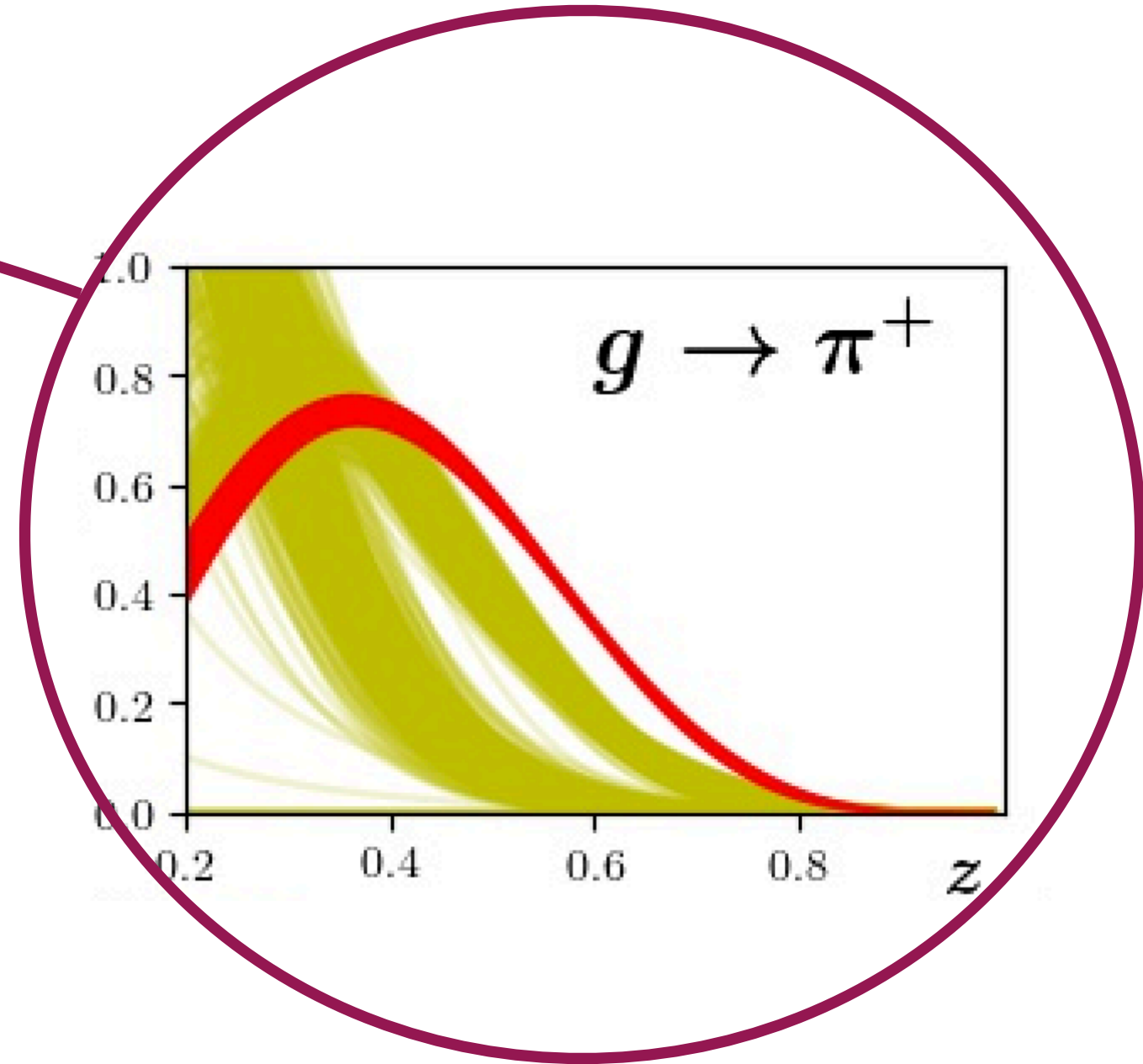


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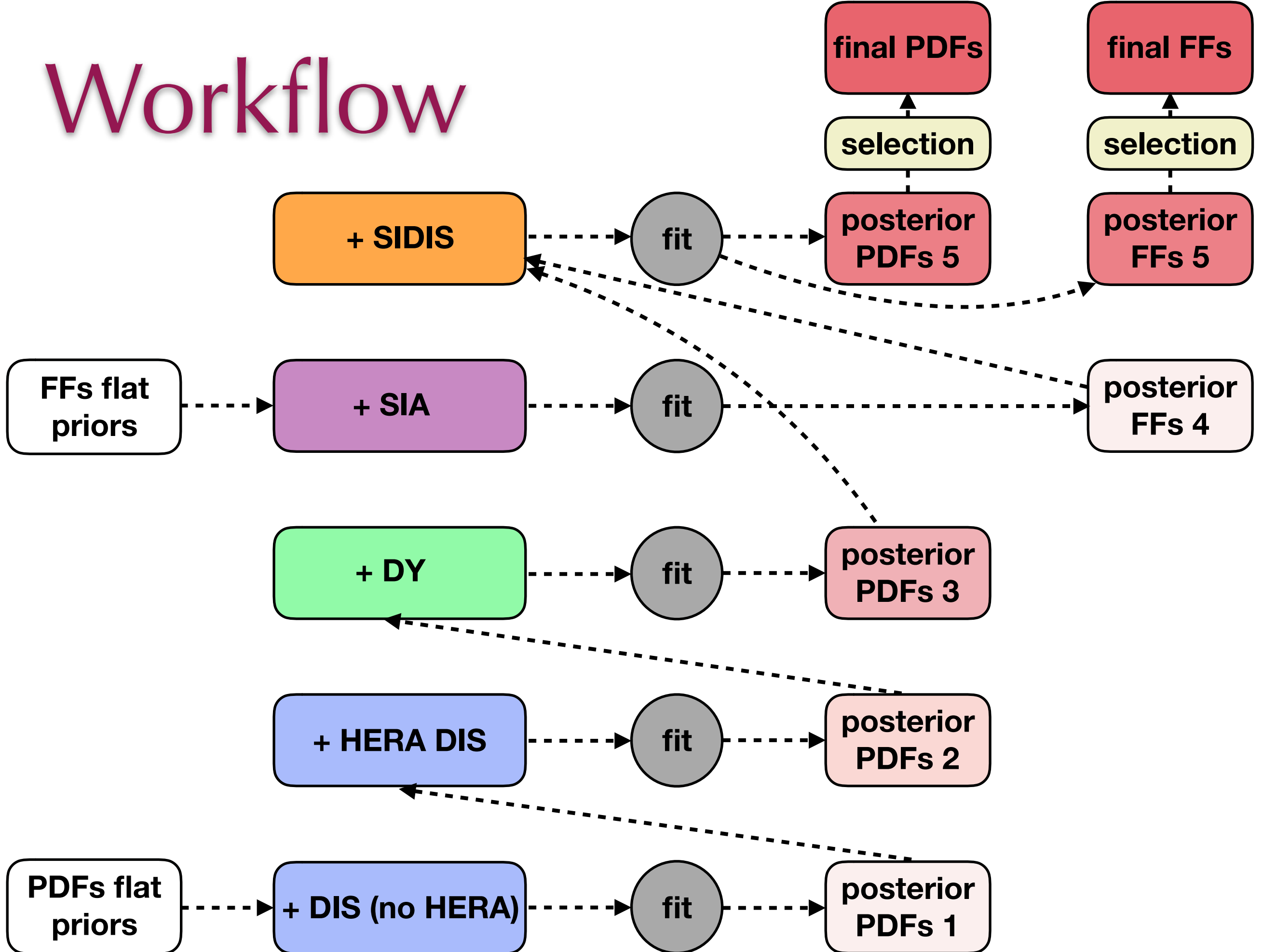


Constraints on
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JAM19

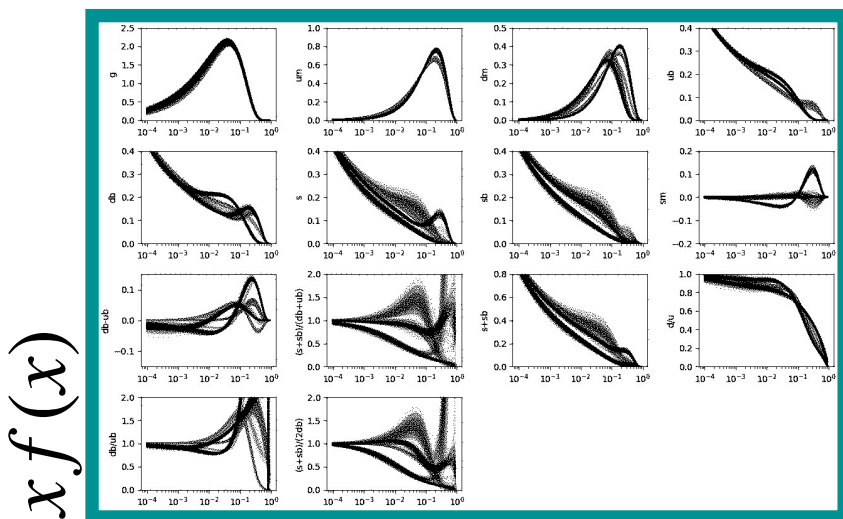
methodology

Workflow



JAM 19: multi-step fitting

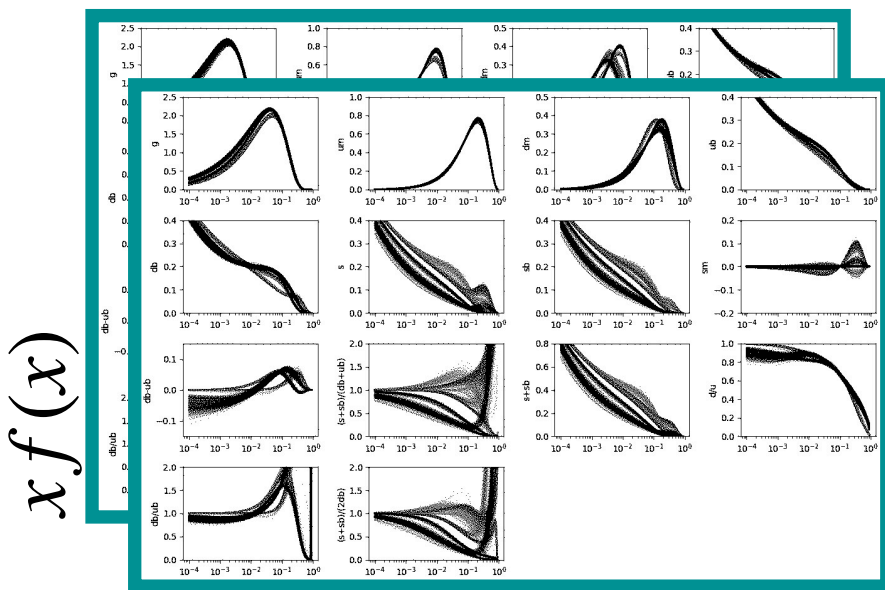
PDFs



+ DIS data

JAM 19: multi-step fitting

PDFs



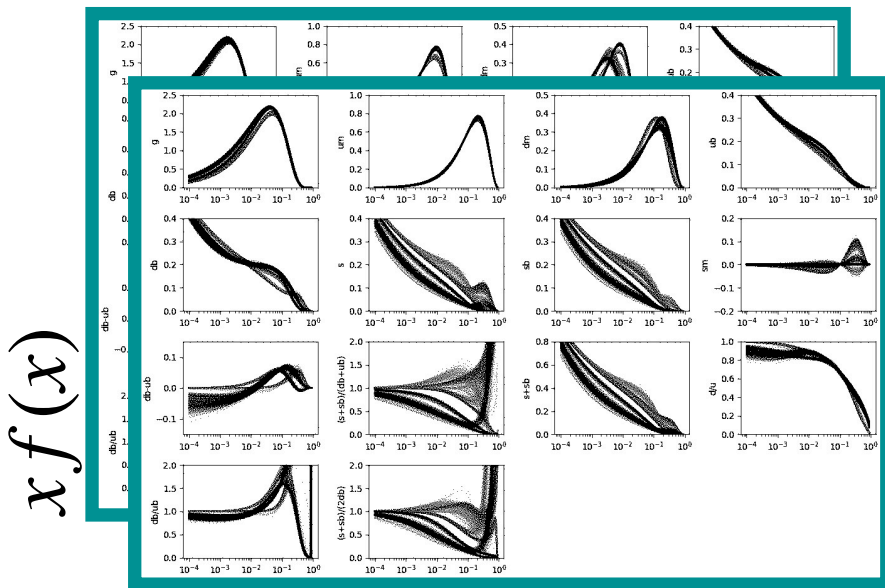
x

+ DIS data

+ DIS + DY data

JAM 19: multi-step fitting

PDFs

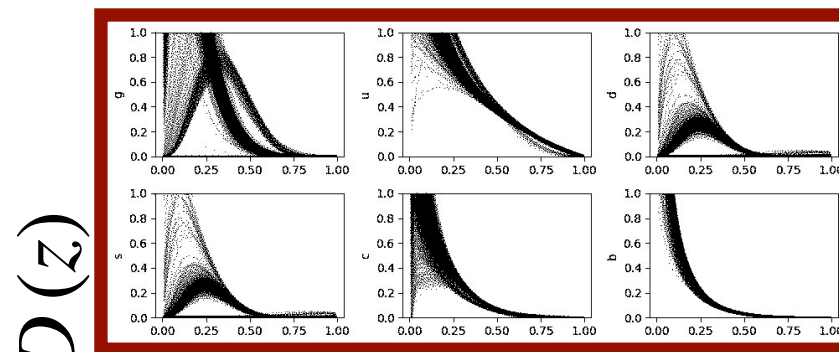


x

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PION FF

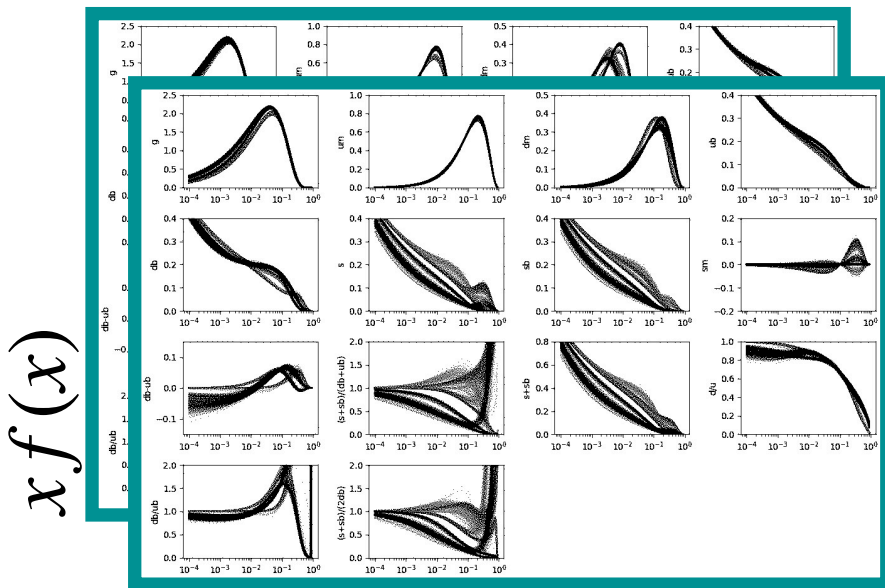


z

+ SLA pion data

JAM 19: multi-step fitting

PDFs

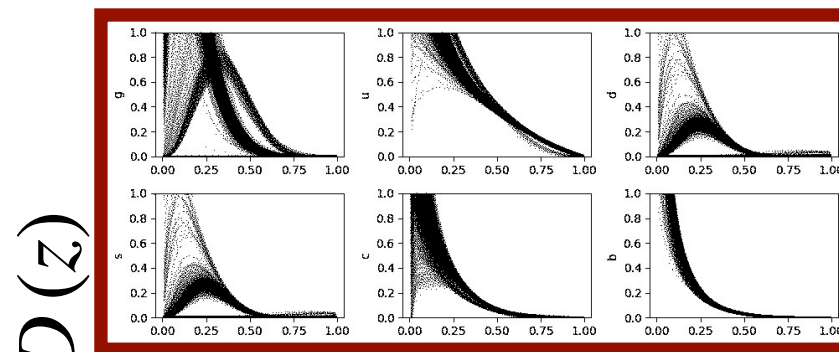


x

+ DIS data

+ DIS + DY data

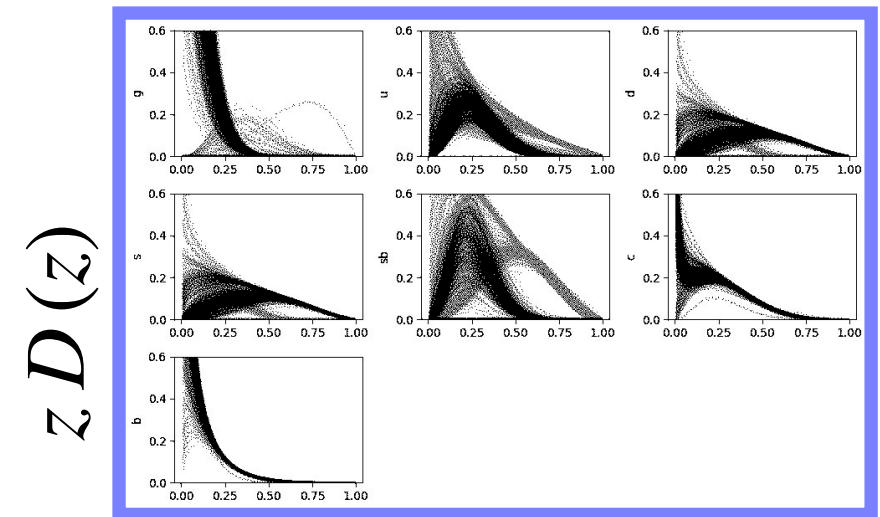
PION FF



z

+ SIA pion data

KAON FF

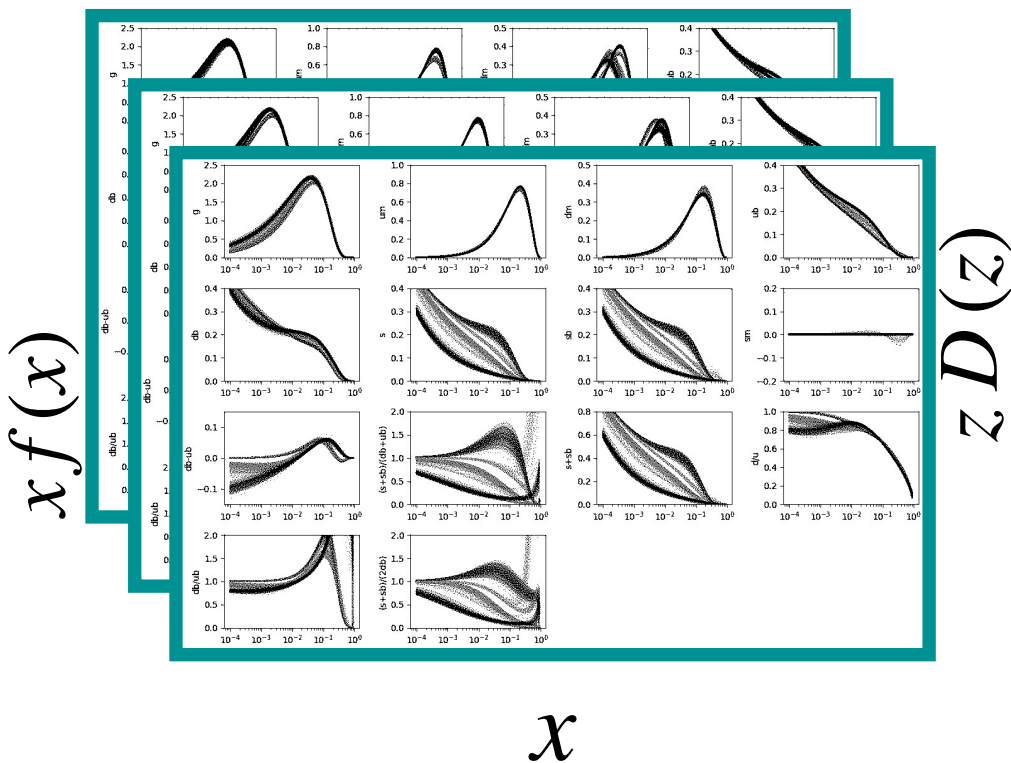


z

+ SIA kaon data

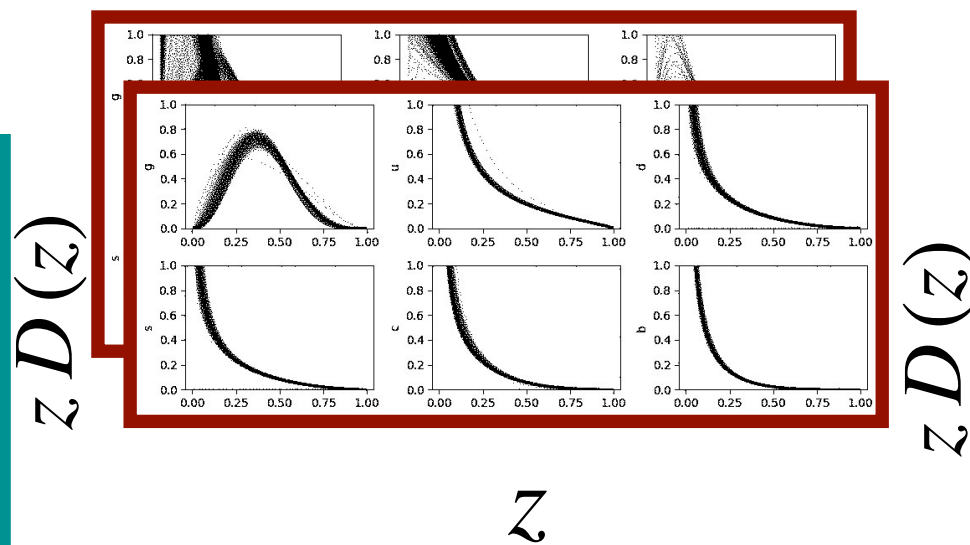
JAM 19: multi-step fitting

PDFs



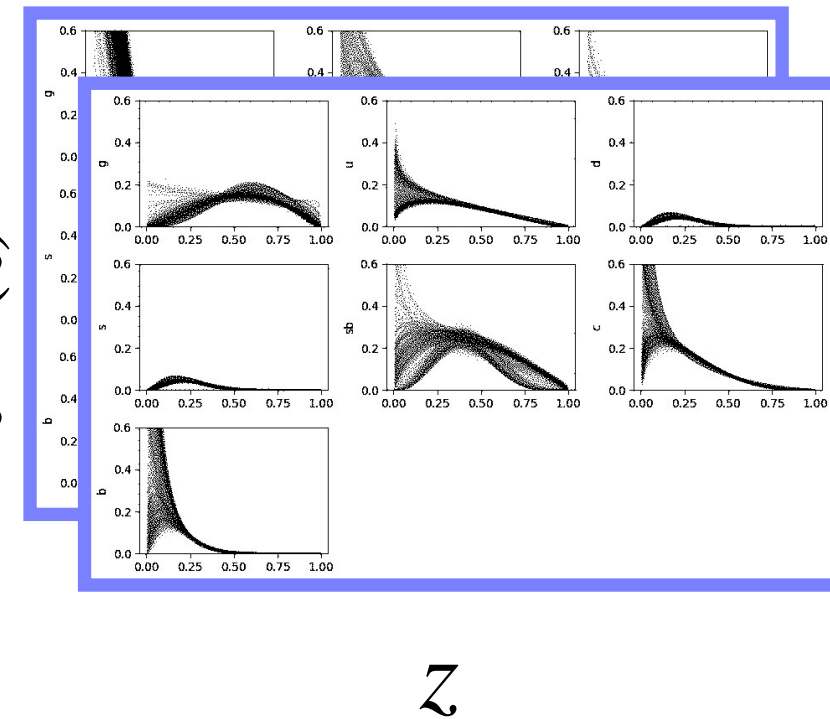
+ DIS data
+ DIS + DY data
+ SIDIS data

PION FF



+ SIA pion data
+ SIDIS pion data

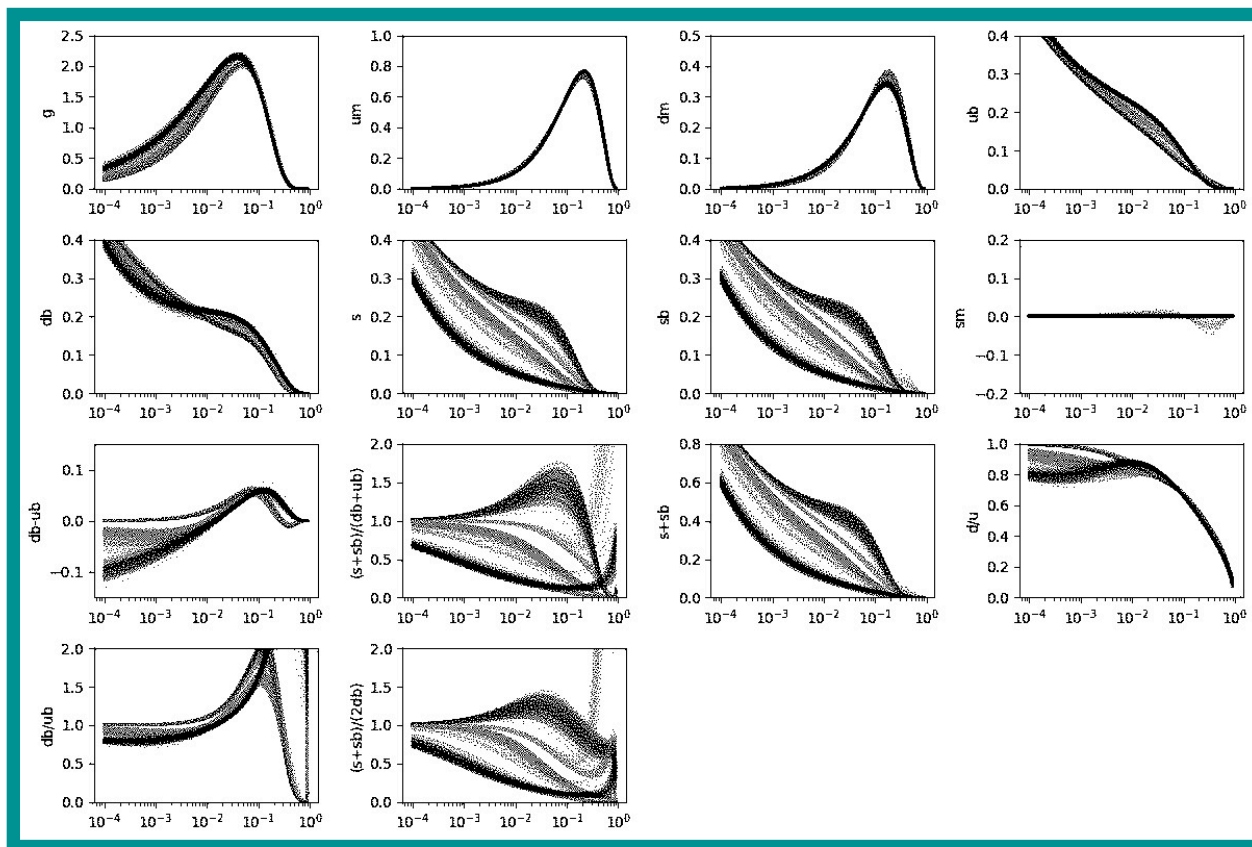
KAON FF



+ SIA kaon data
+ SIDIS kaon data

Discriminating multiple solutions

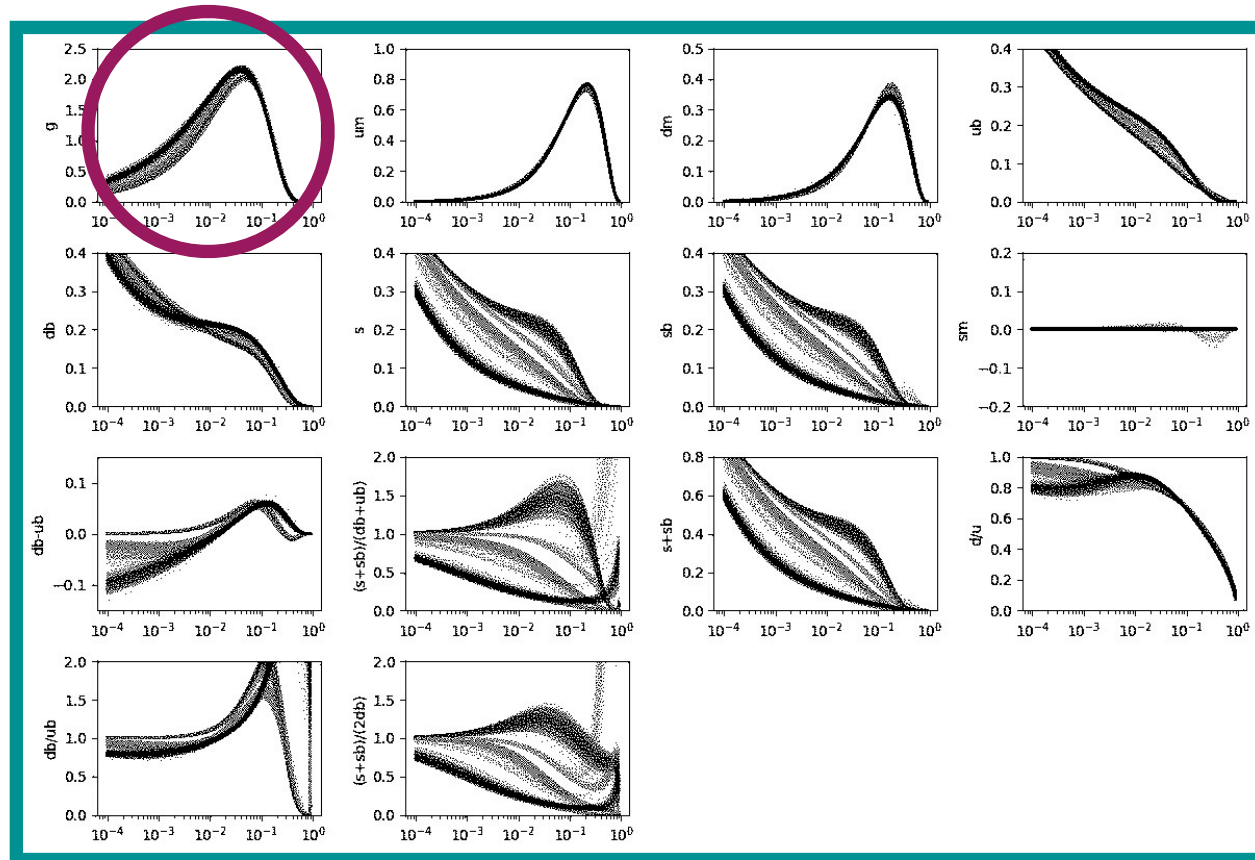
$xf(x)$



x

Discriminating multiple solutions

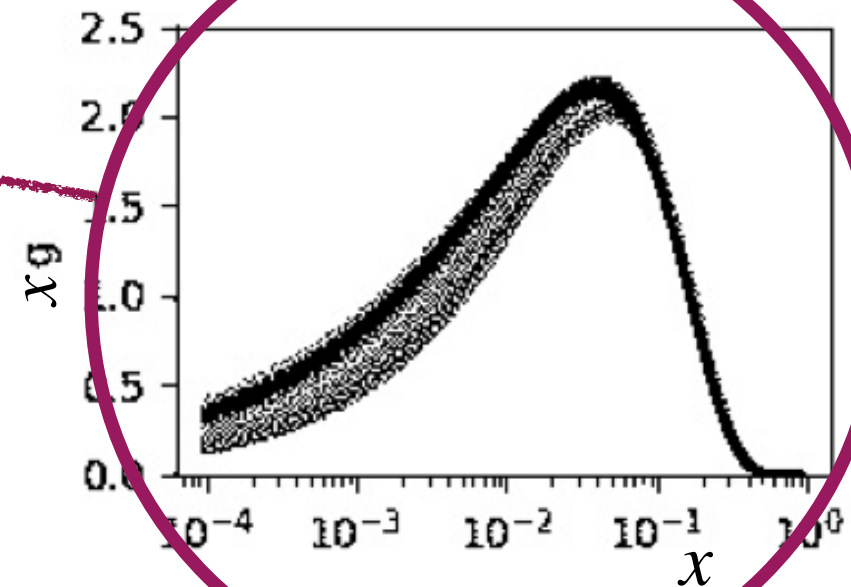
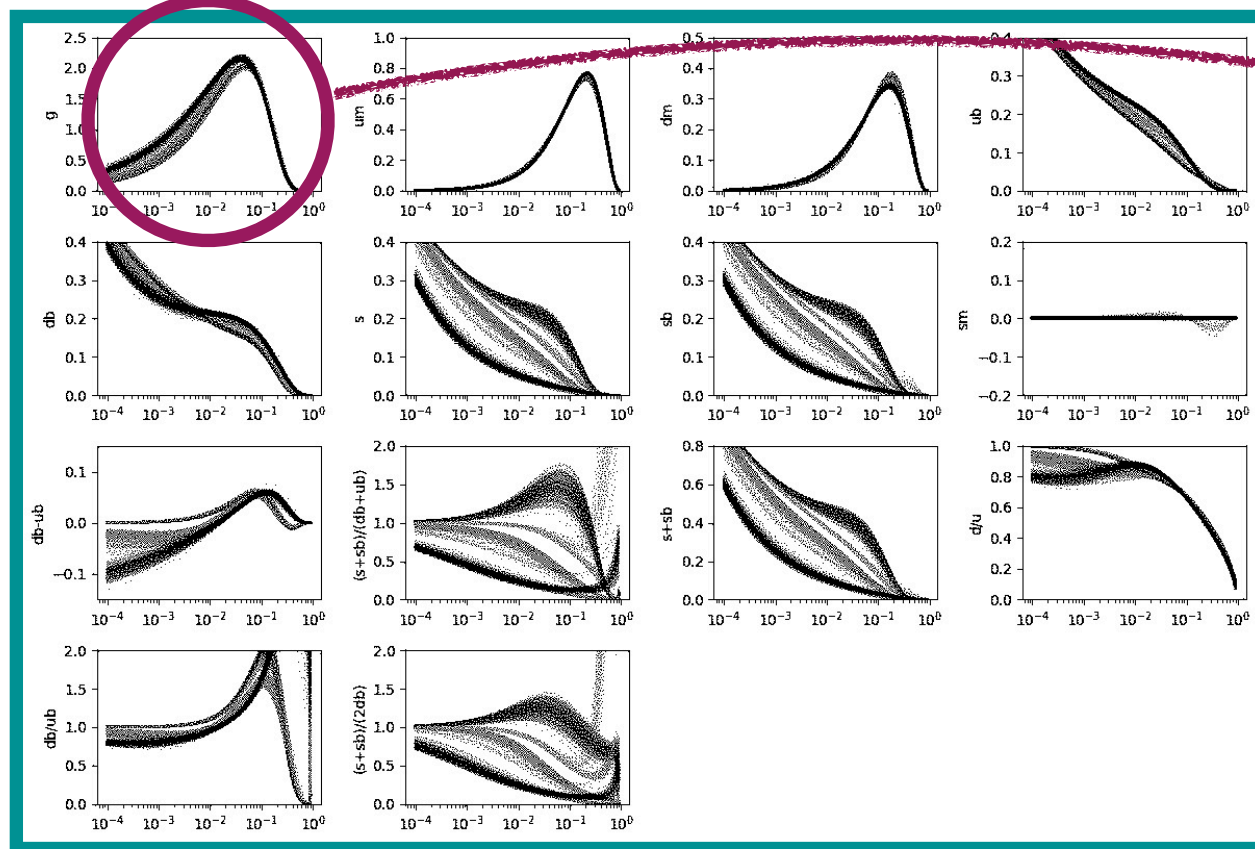
$xf(x)$



x

Discriminating multiple solutions

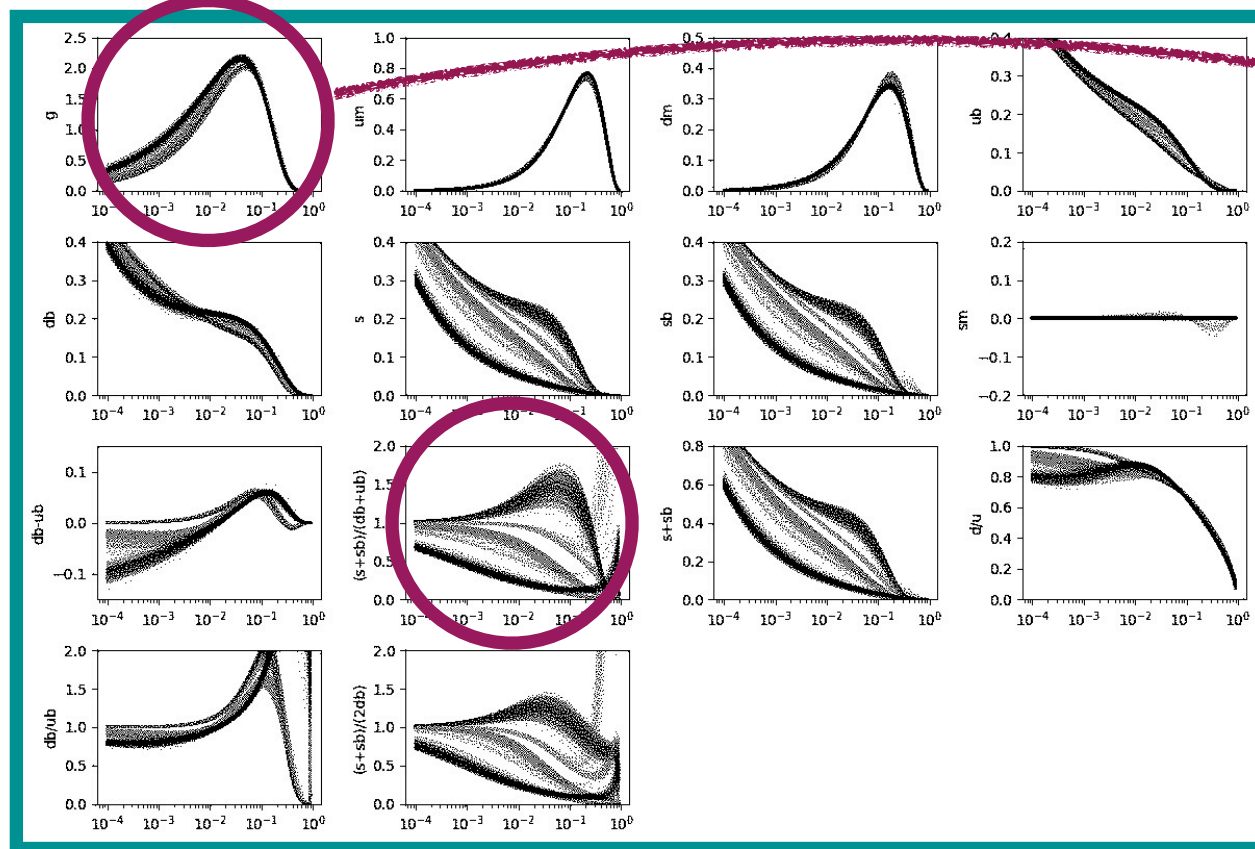
$xf(x)$



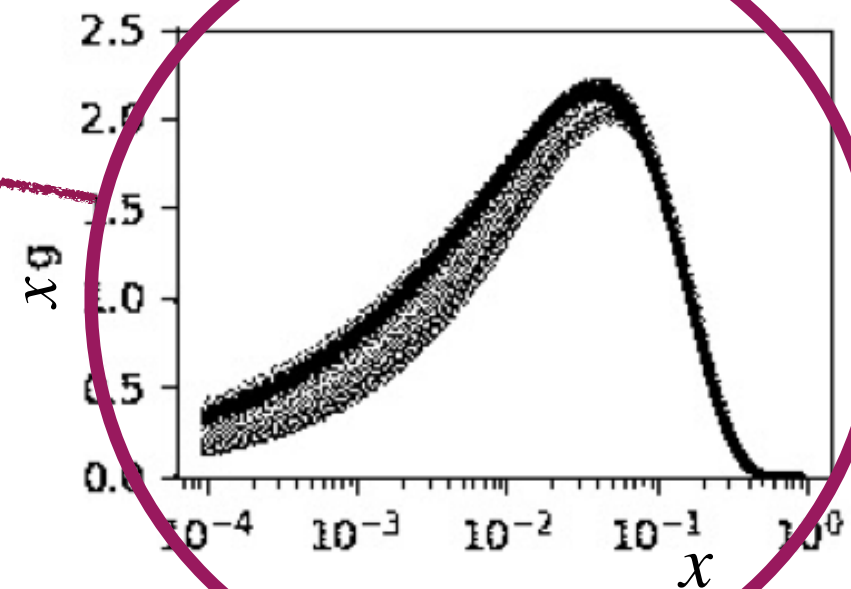
x

Discriminating multiple solutions

$xf(x)$

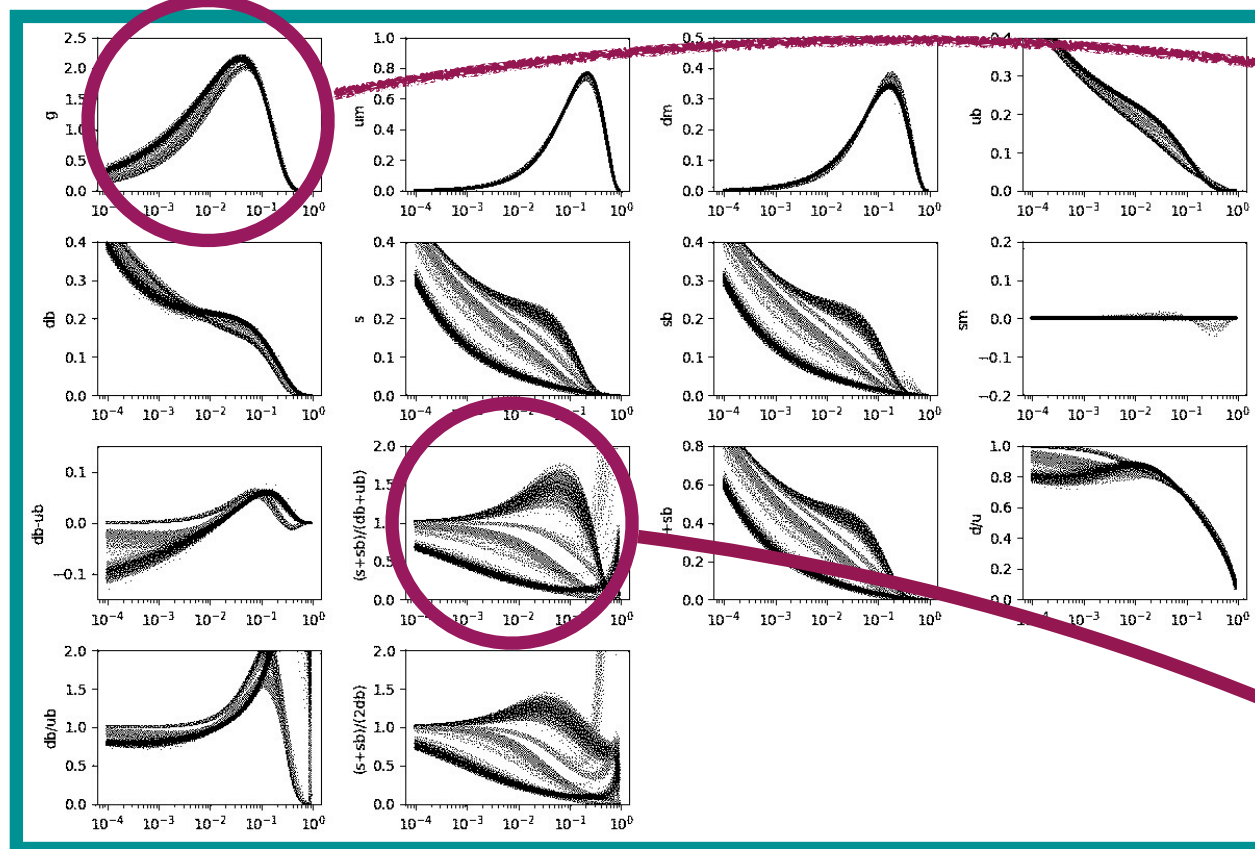


x



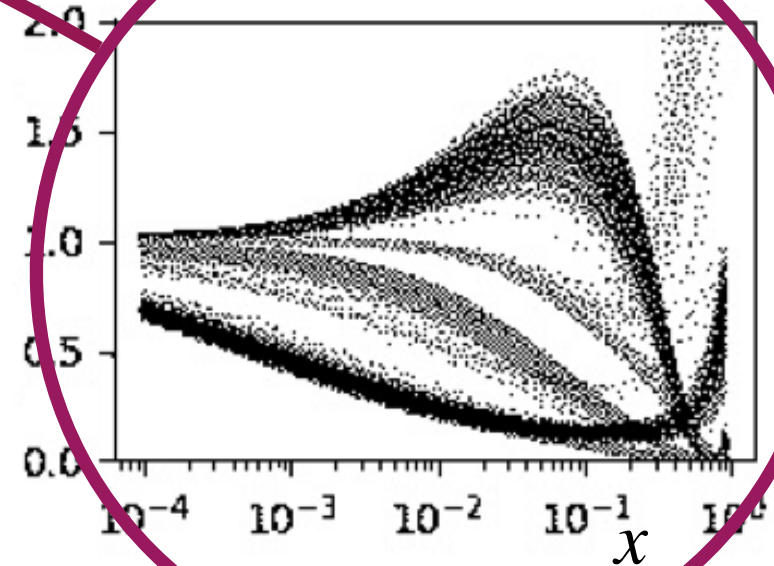
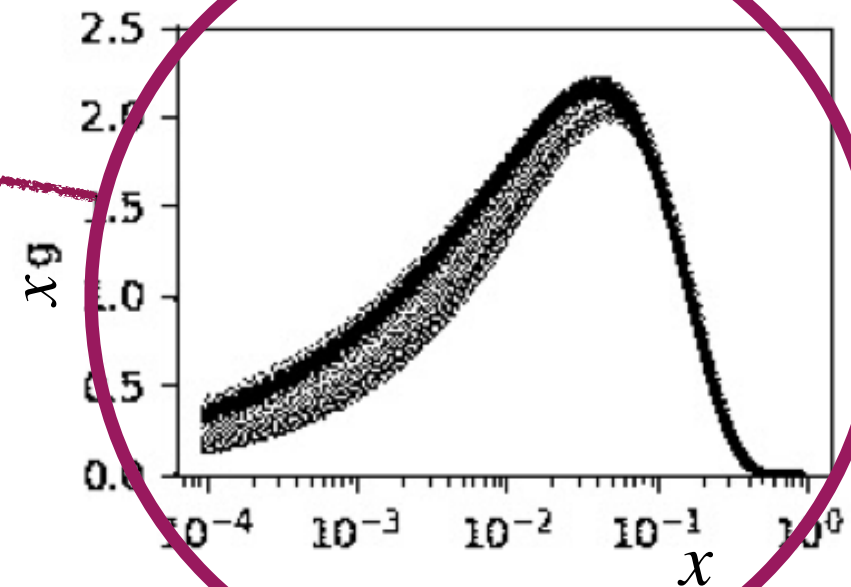
Discriminating multiple solutions

$xf(x)$



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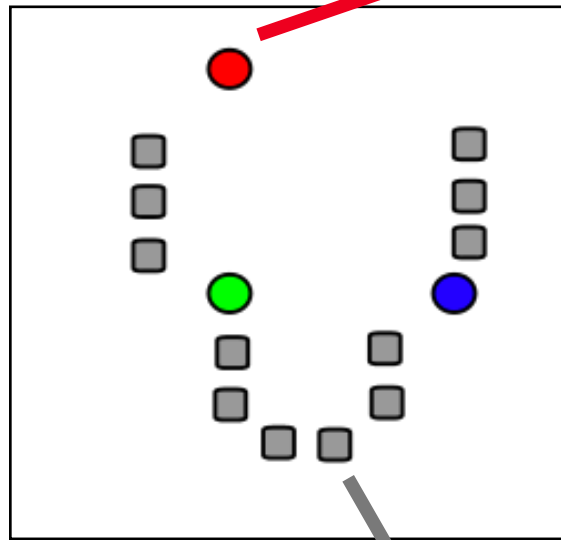
$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$



k-means clustering

E . g . $f(x) = x^\alpha (1 - x)^\beta$

(α^*, β^*) : centroid

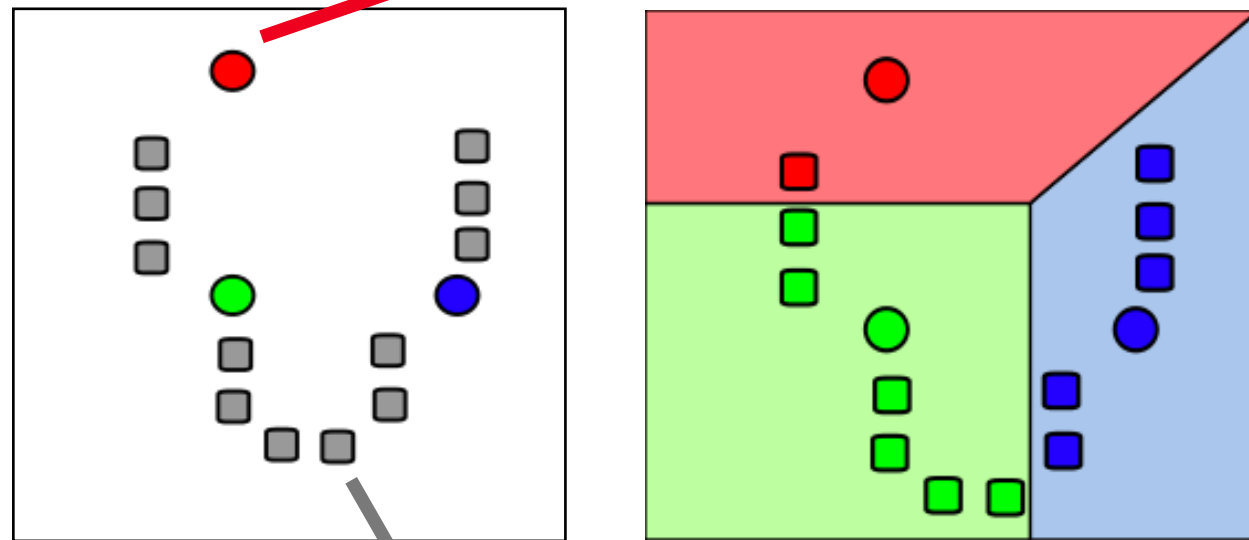


(α_i, β_i) : replica

k-means clustering

E . g . $f(x) = x^\alpha (1 - x)^\beta$

(α^*, β^*) : centroid



Initialization

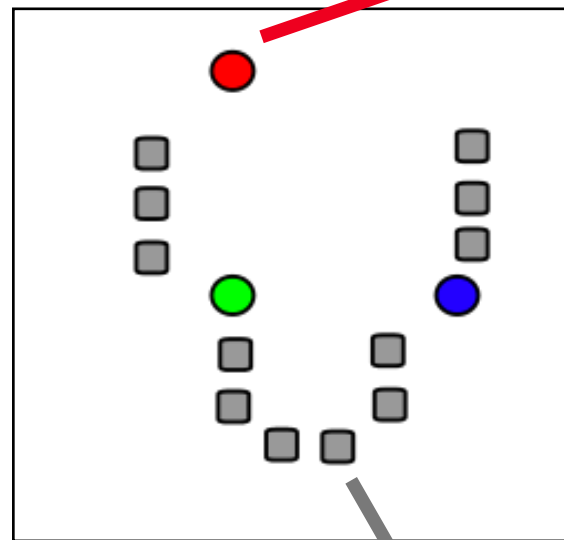
Assignment

(α_i, β_i) : replica

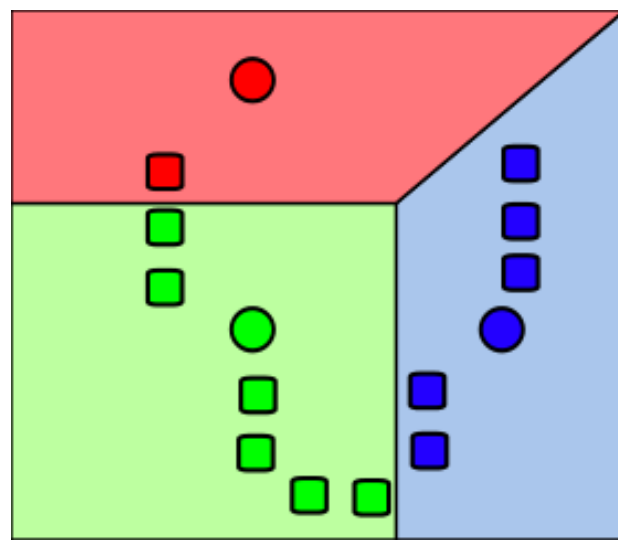
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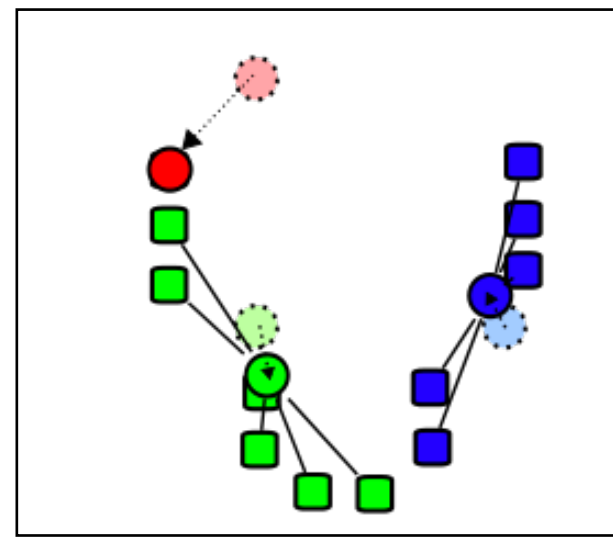
(α^*, β^*) : centroid



Initialization



Assignment



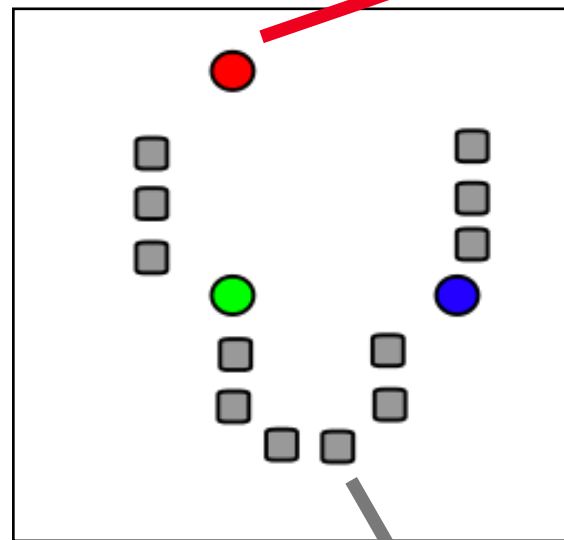
Update

(α_i, β_i) : replica

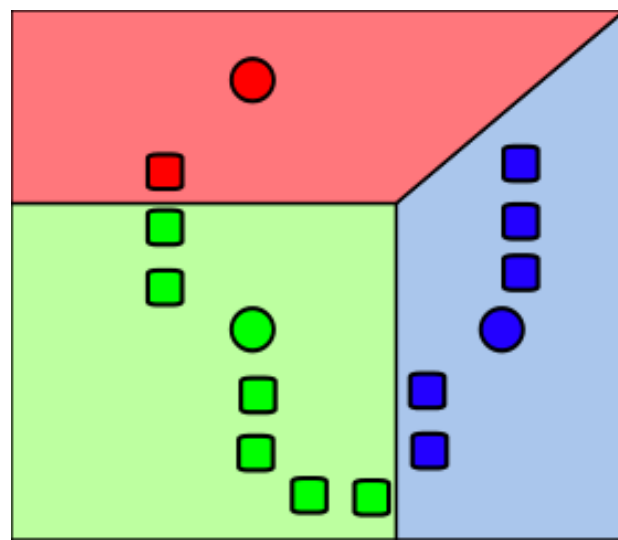
k-means clustering

E . g . $f(x) = x^\alpha (1 - x)^\beta$

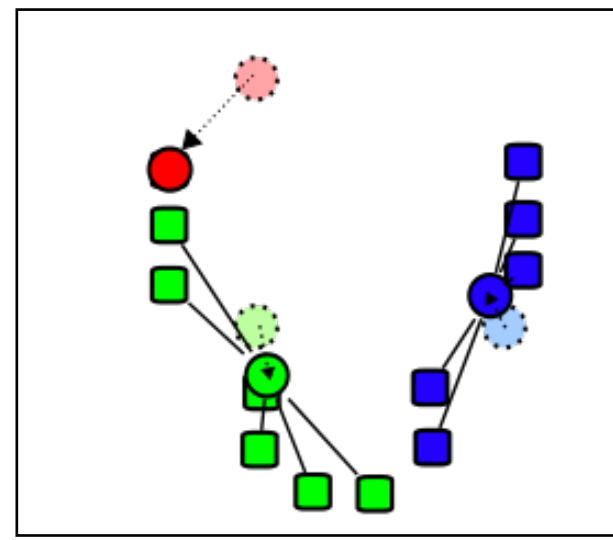
(α^*, β^*) : centroid



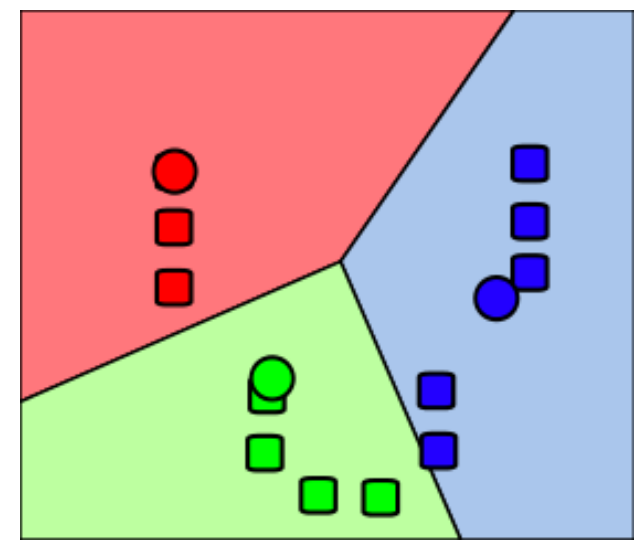
Initialization



Assignment



Update



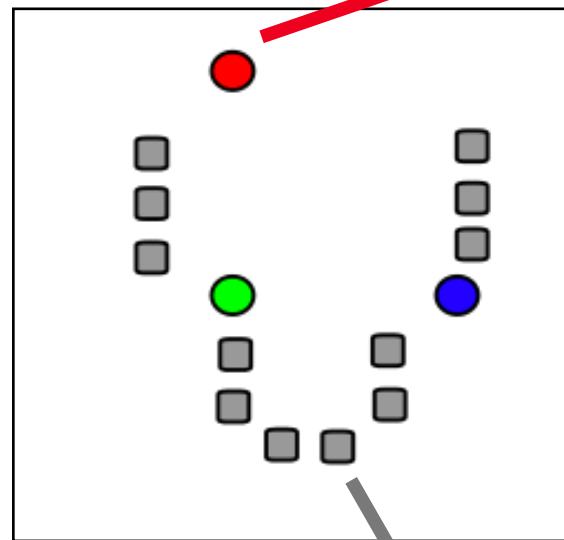
Assignment

(α_i, β_i) : replica

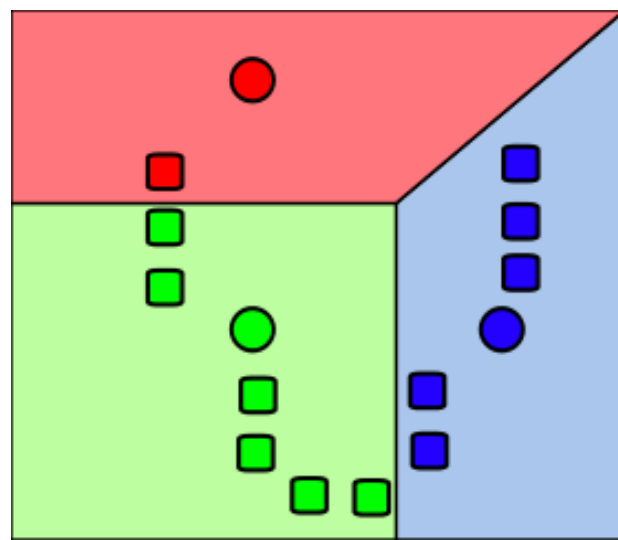
k-means clustering

E . g . $f(x) = x^\alpha (1 - x)^\beta$

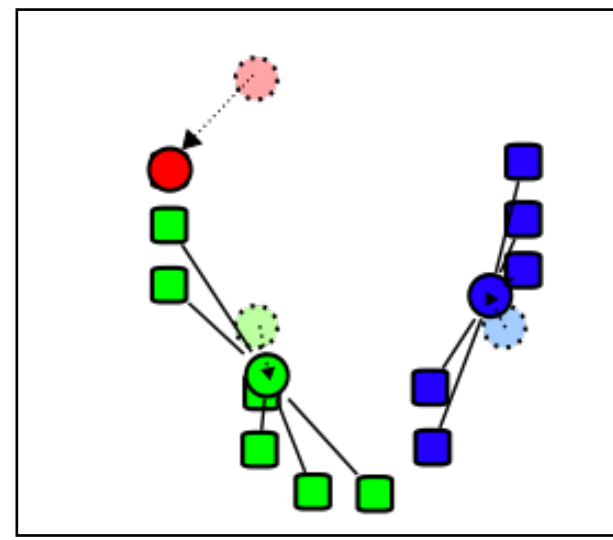
(α^*, β^*) : centroid



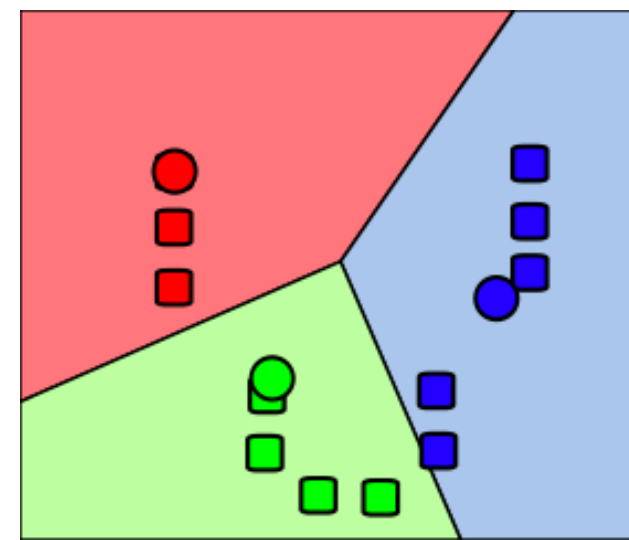
Initialization



Assignment



Update

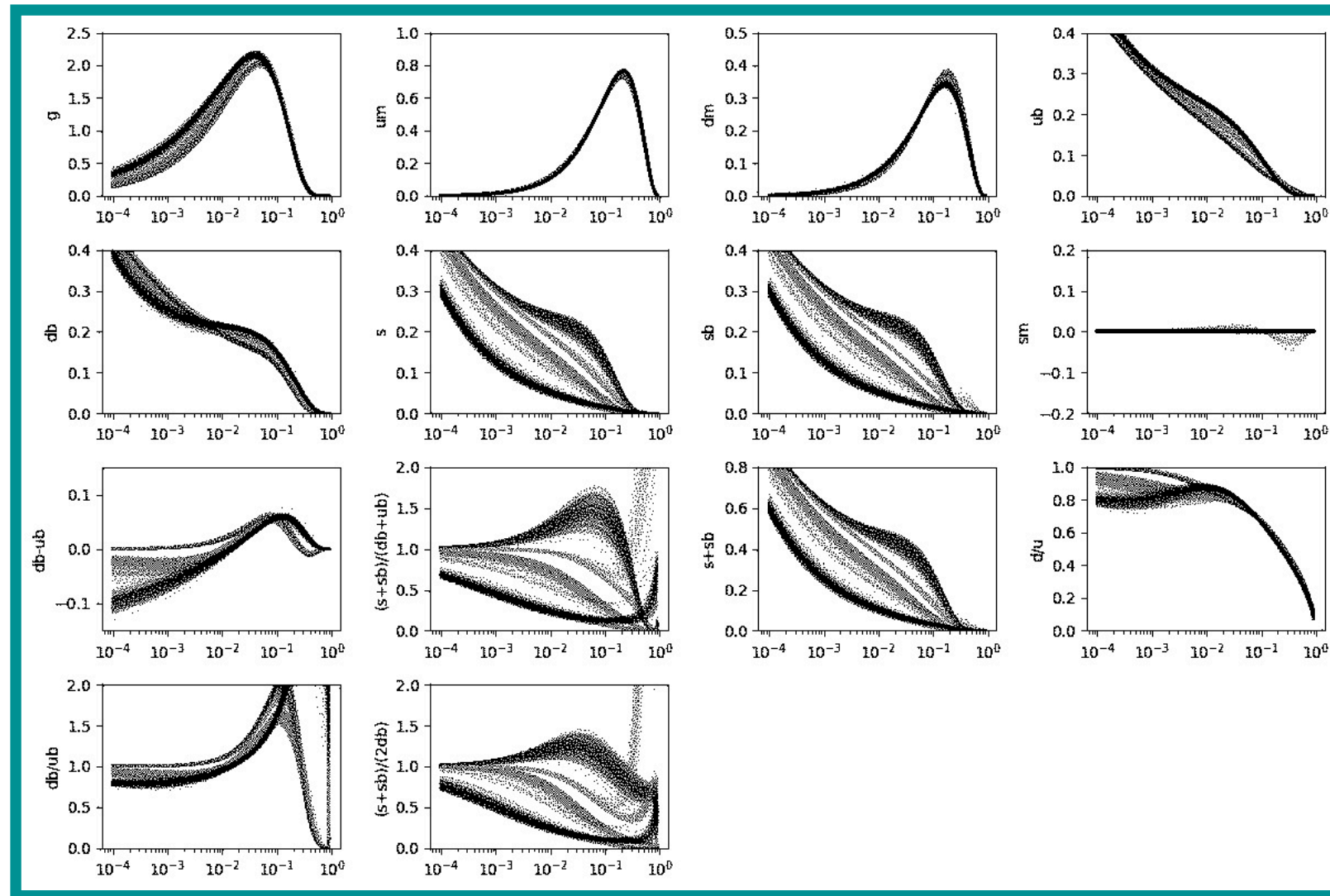


Assignment

Repeat until convergence

(α_i, β_i) : replica

Discriminating multiple solutions

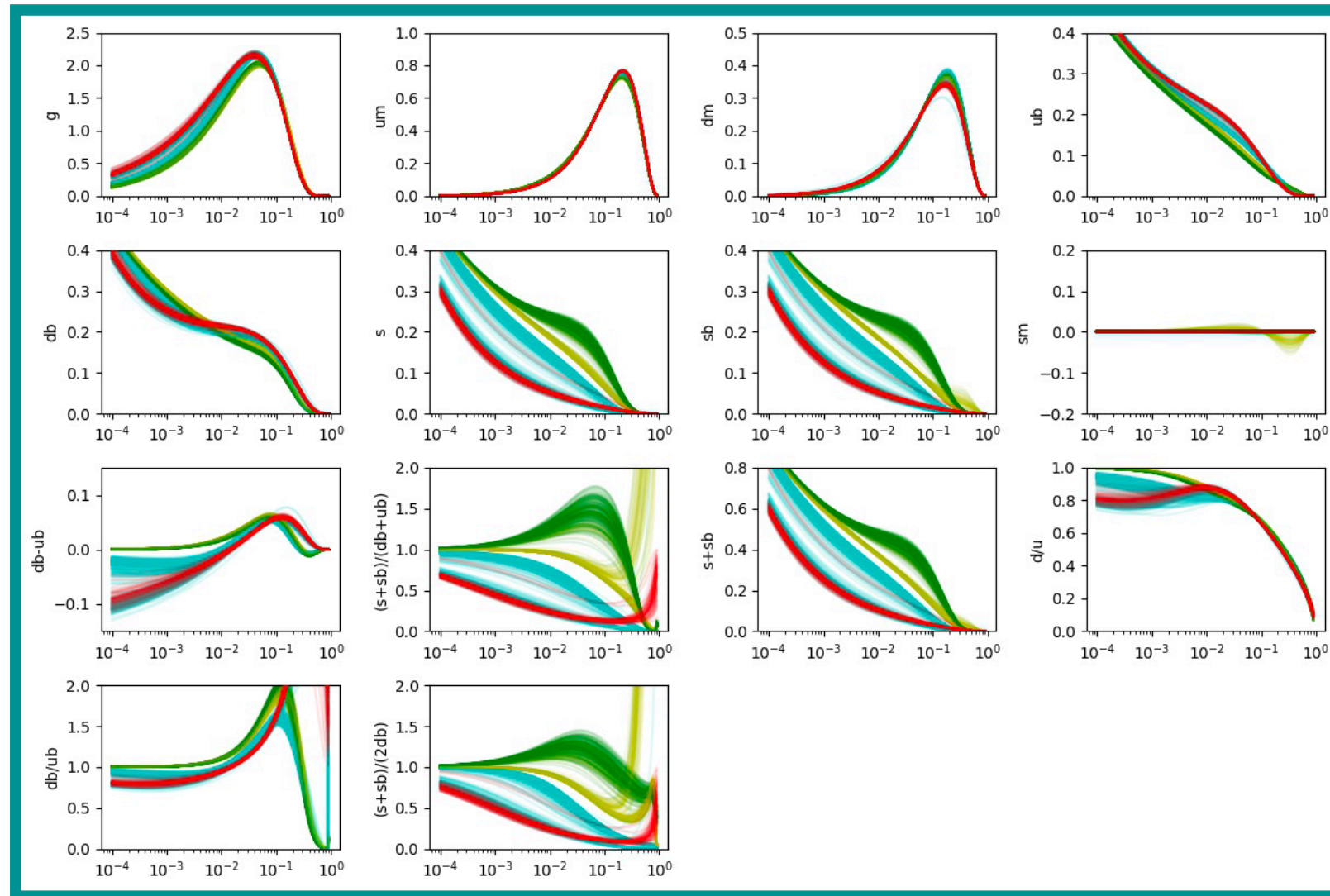


+ DIS data

+ DIS + DY data

+ SIDIS data

Discriminating multiple solutions



+ DIS data

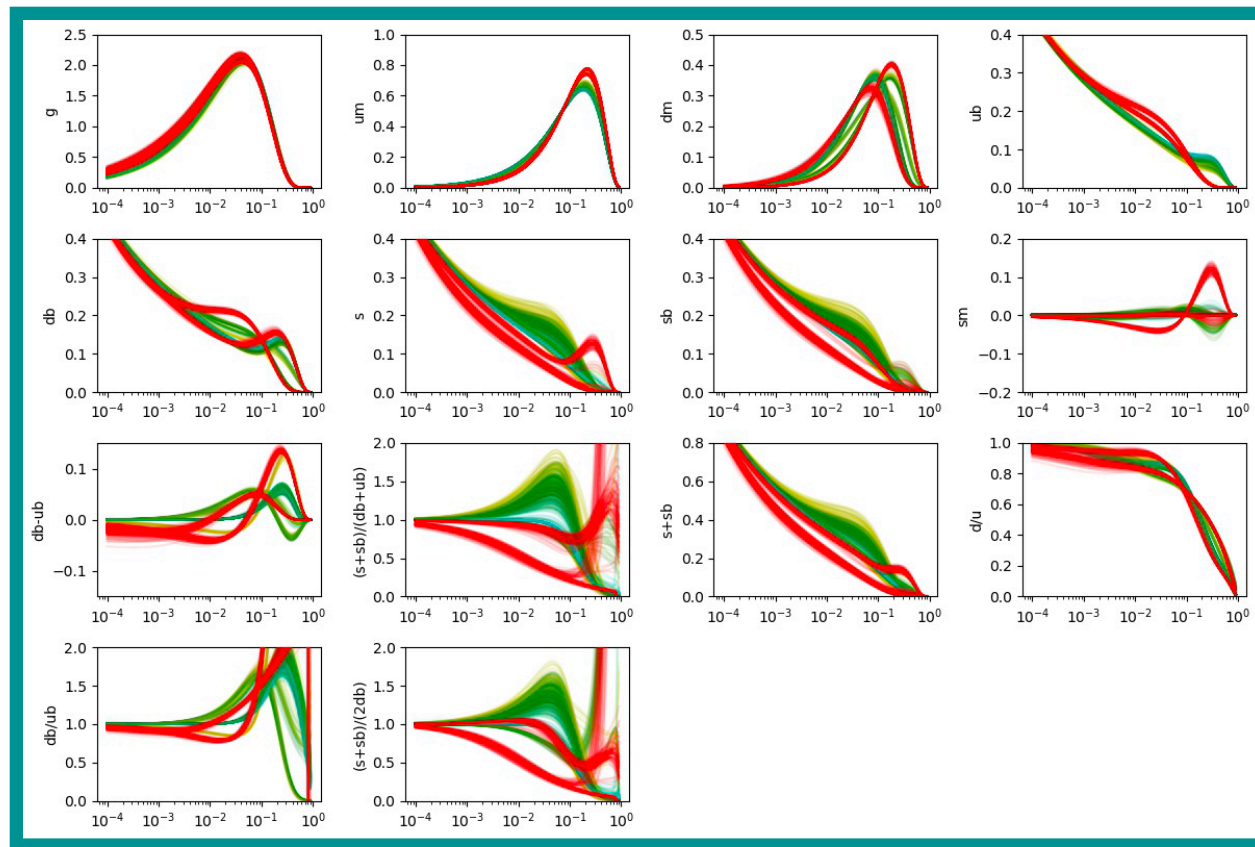
+ DIS + DY data

+ SIDIS data

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

PDFs



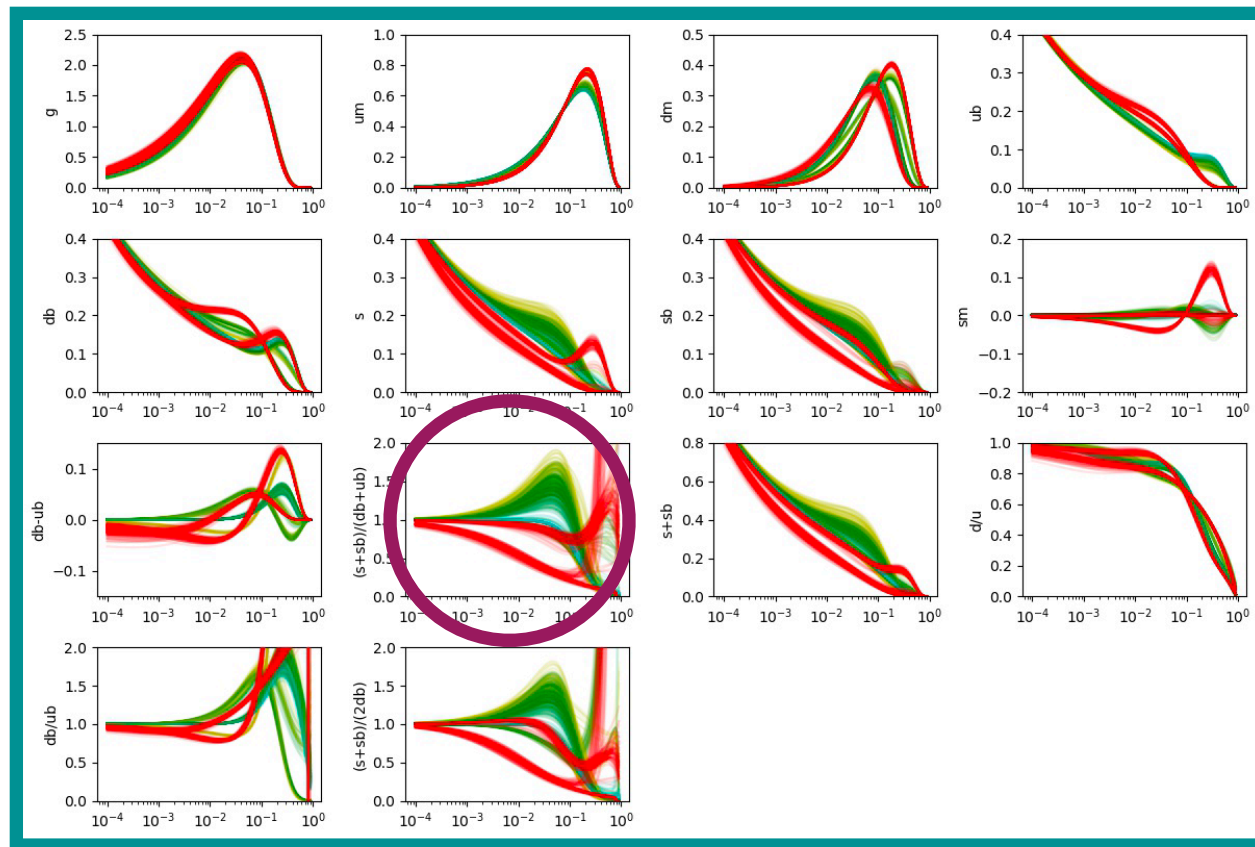
x

+ DIS data

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

PDFs



x

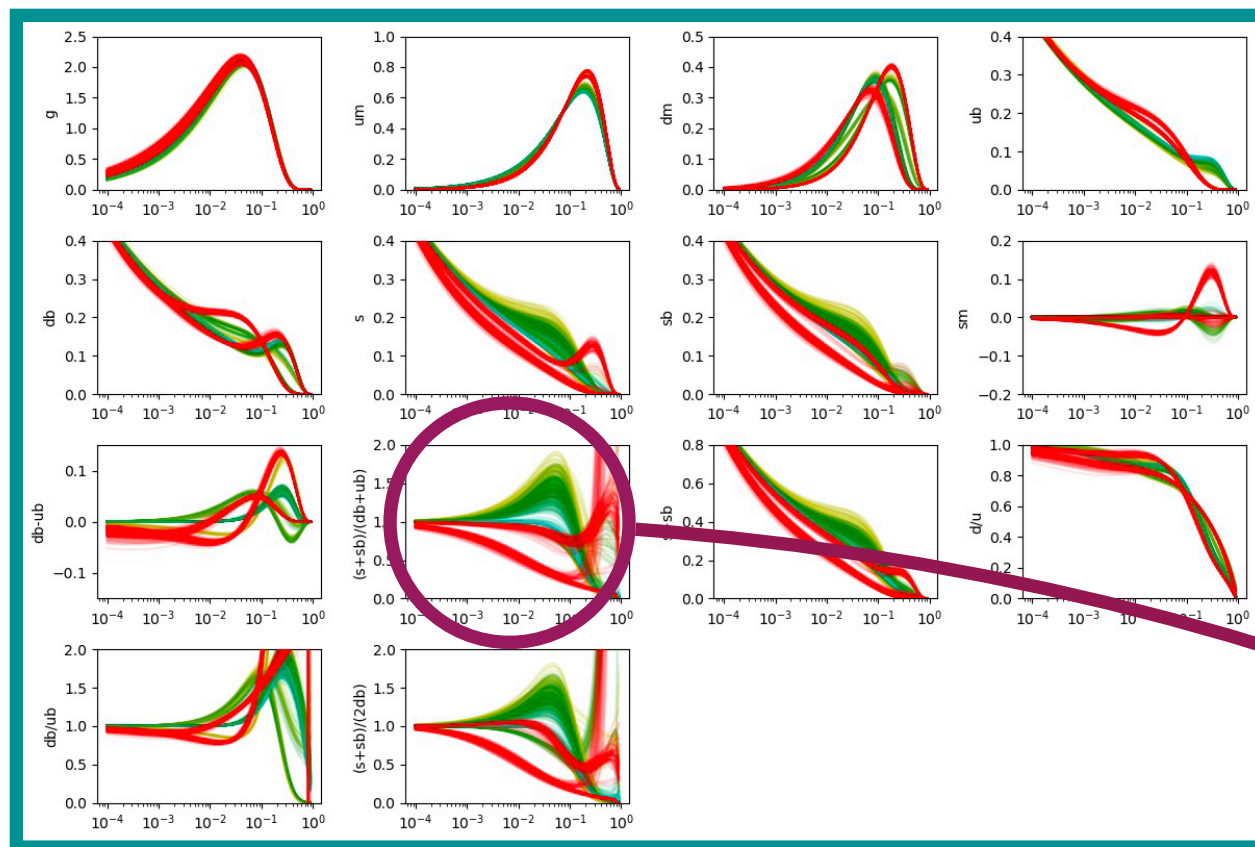
+ DIS data

$xf(x)$

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

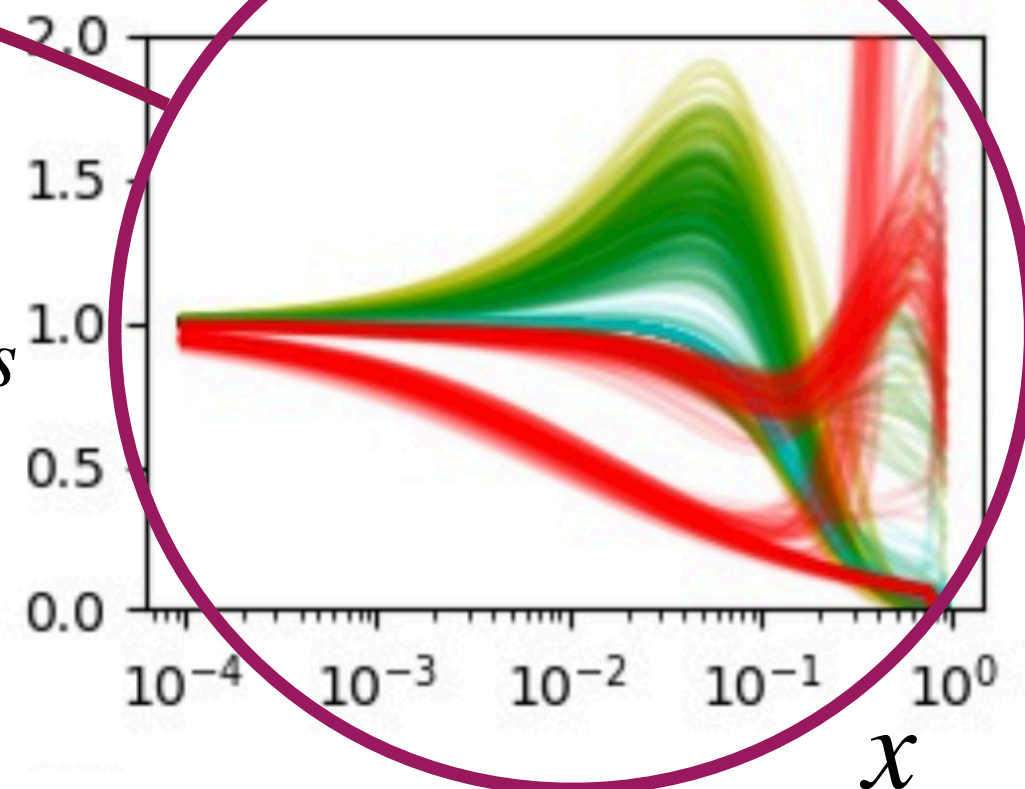
PDFs



x

+ DIS data

R_s

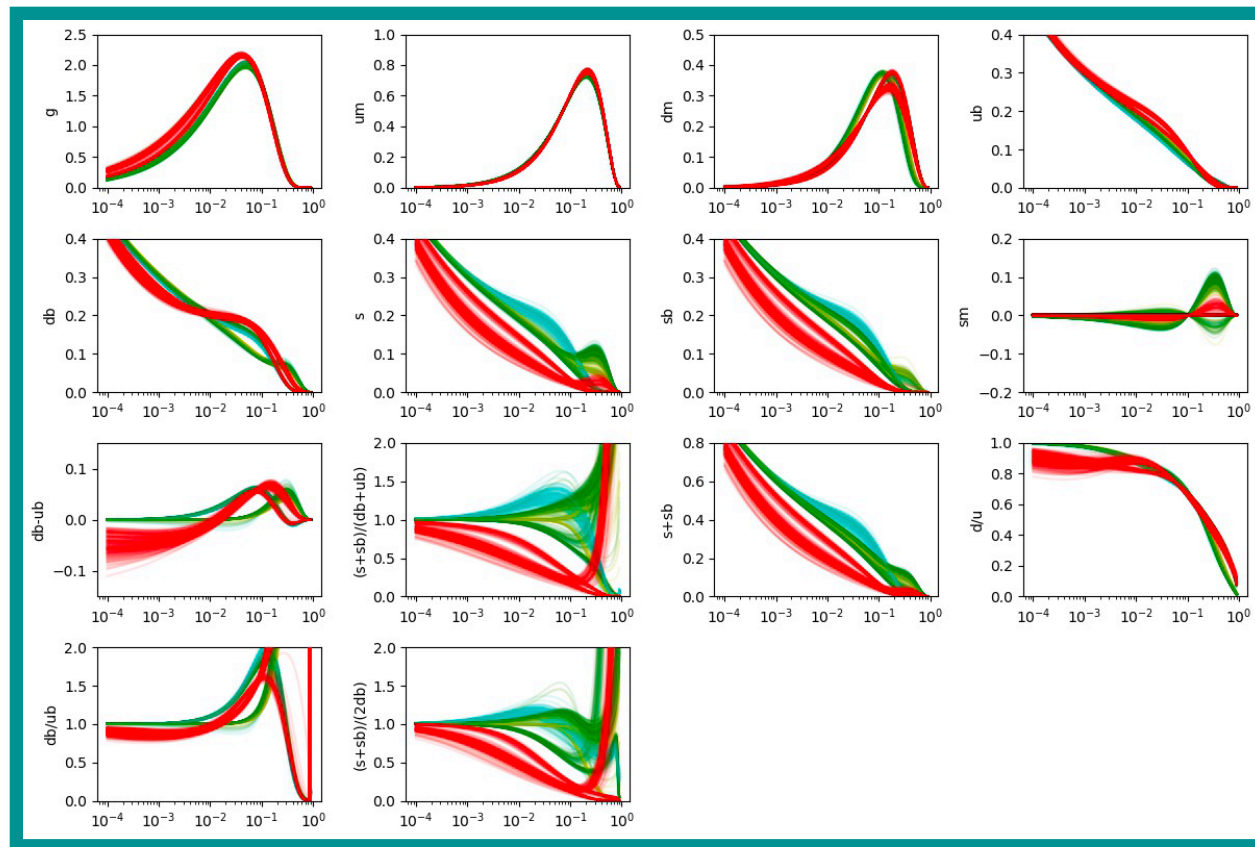


x

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

PDFs



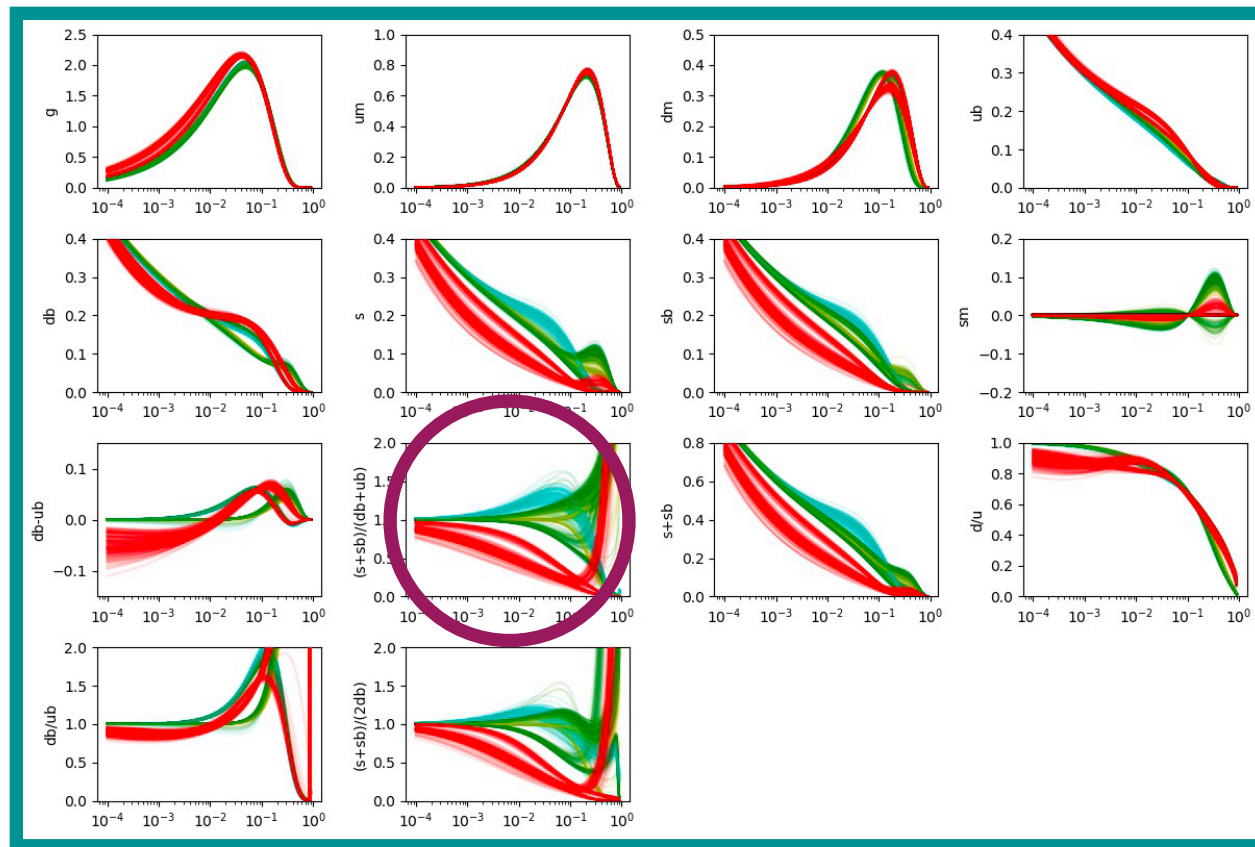
x

+ DIS data
+ DY data

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

PDFs



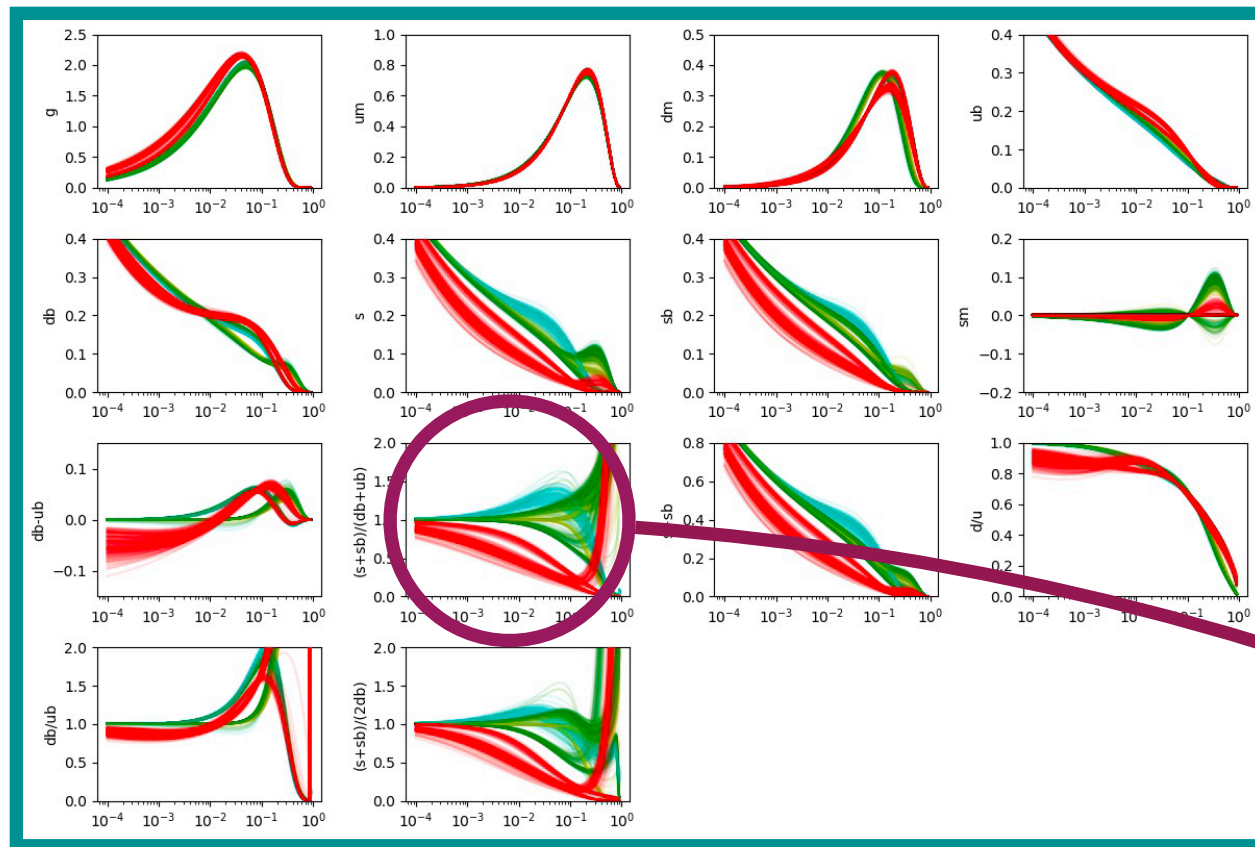
x

+ DIS data
+ DY data

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

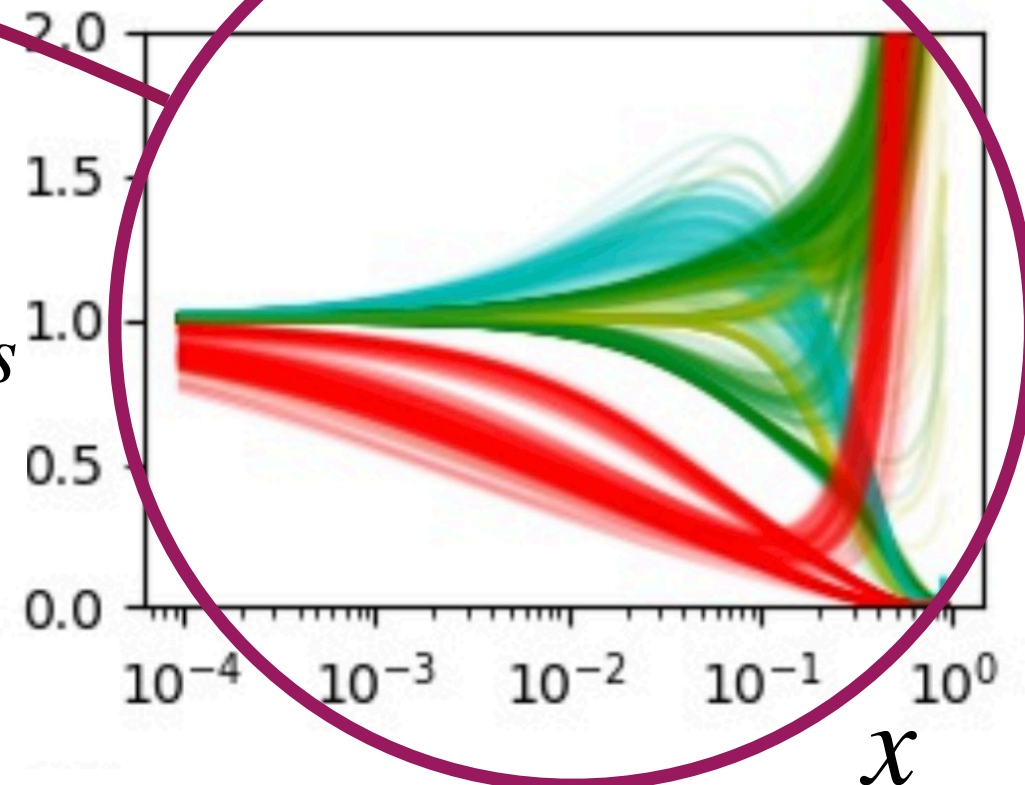
PDFs



x

+ DIS data
+ DY data

R_s

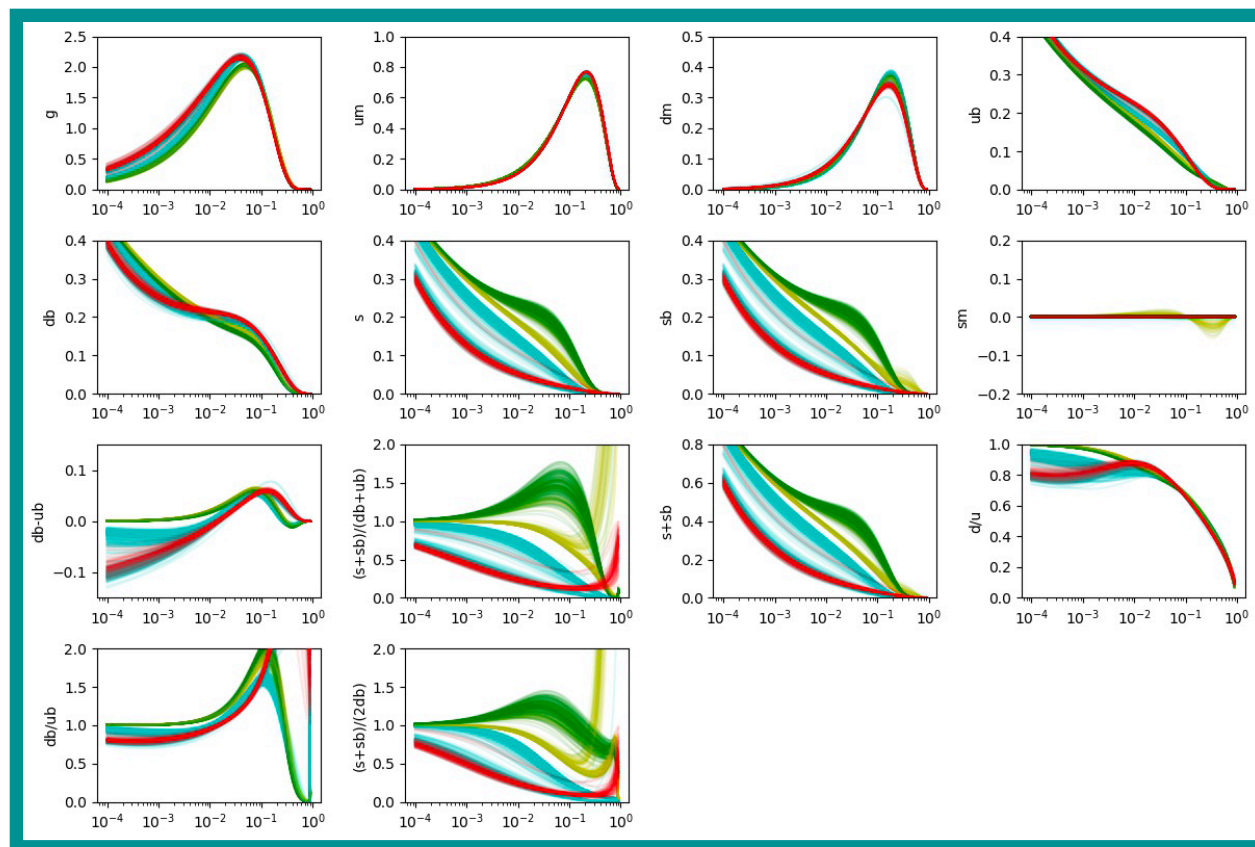


x

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

PDFs



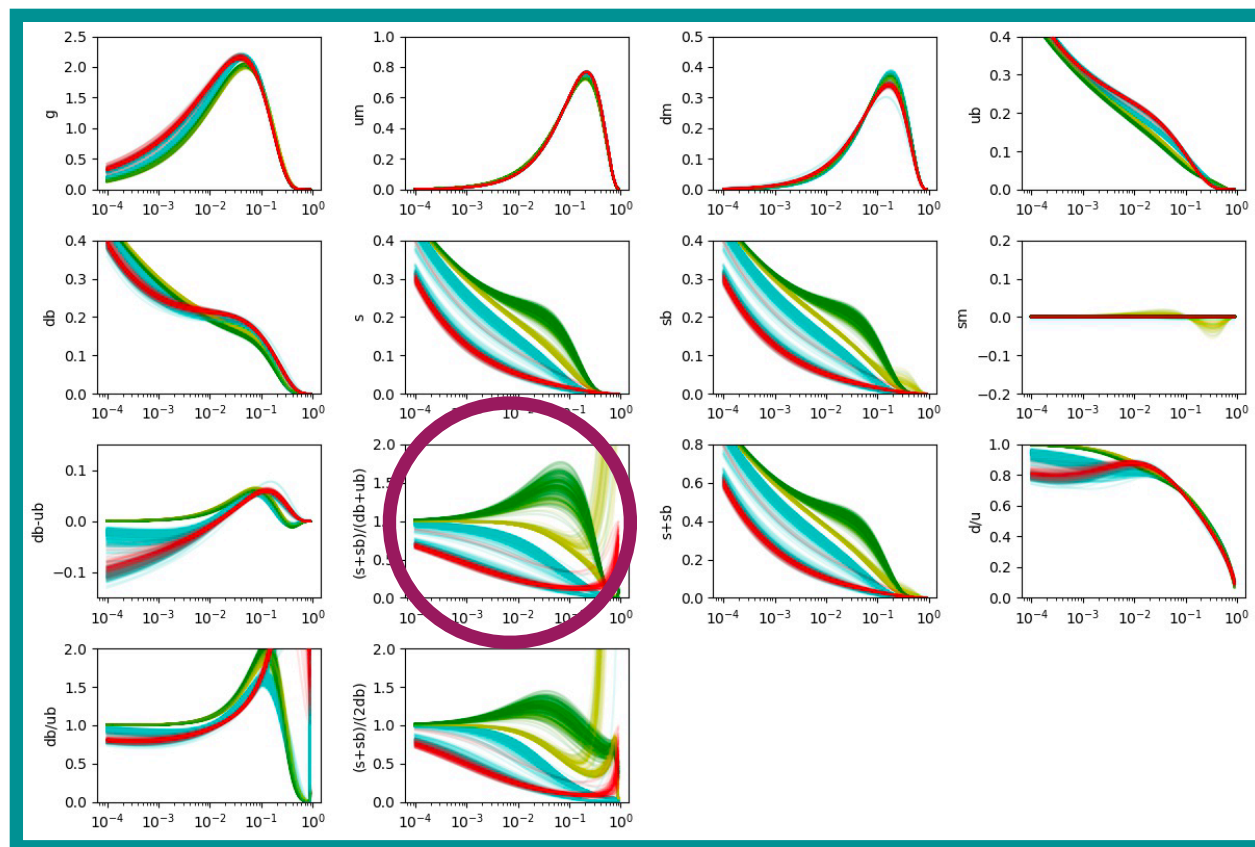
x

- + DIS data
- + DY data
- + SIA + SIDIS data

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

PDFs



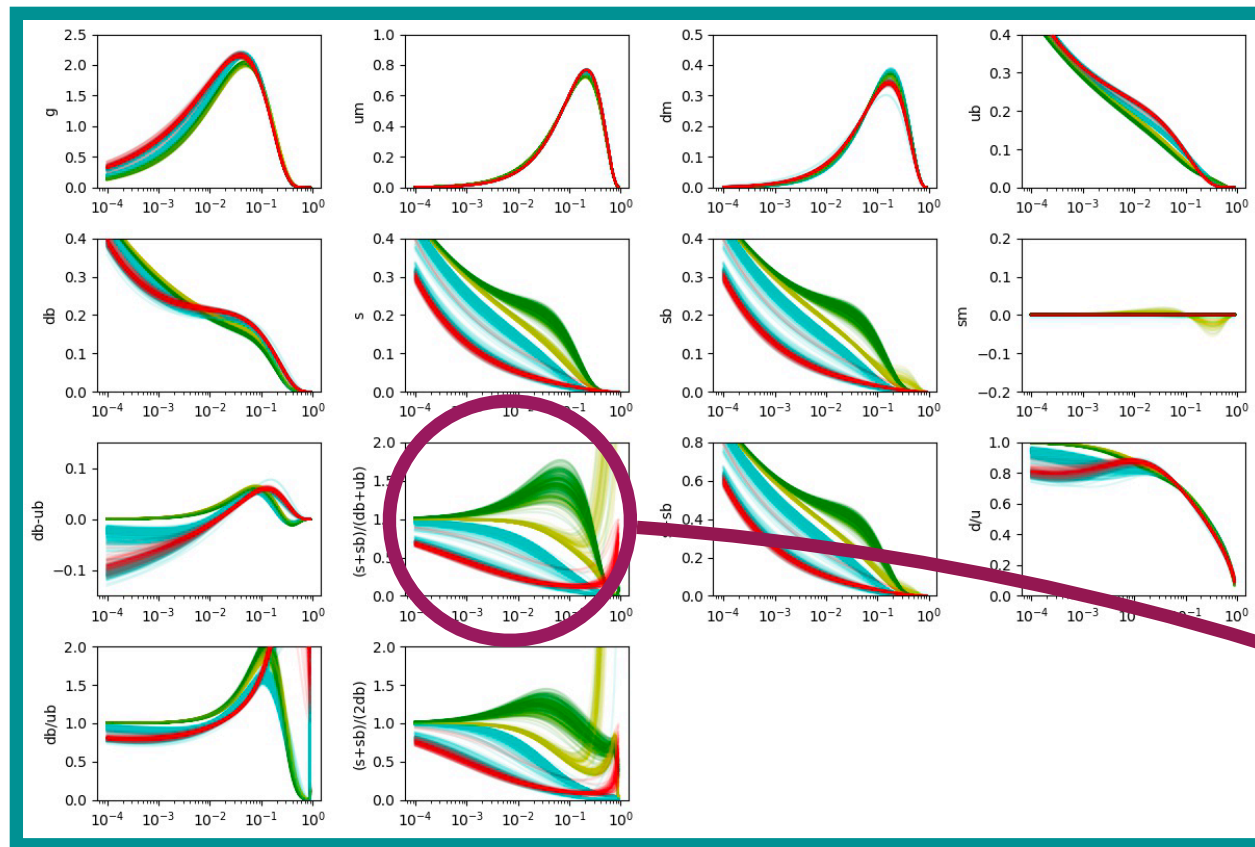
x

- + DIS data
- + DY data
- + SIA + SIDIS data

Constraints on R_s

$$R_s = \frac{s + \bar{s}}{\bar{u} + \bar{d}}$$

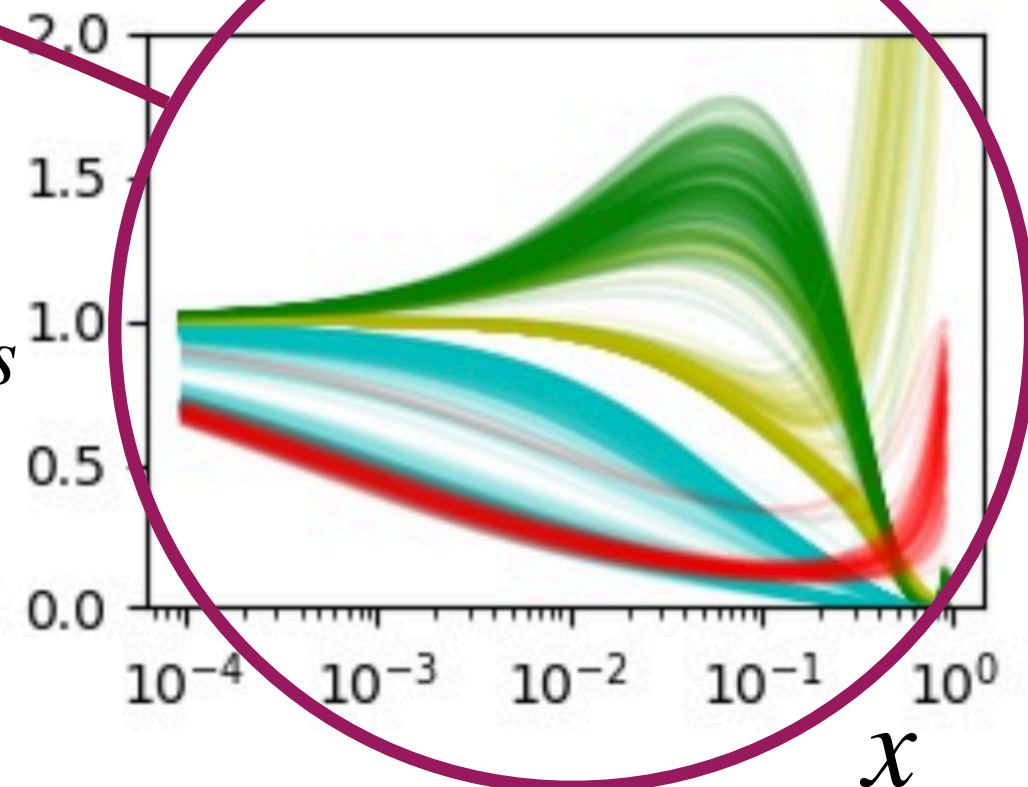
PDFs



x

- + DIS data
- + DY data
- + SIA + SIDIS data

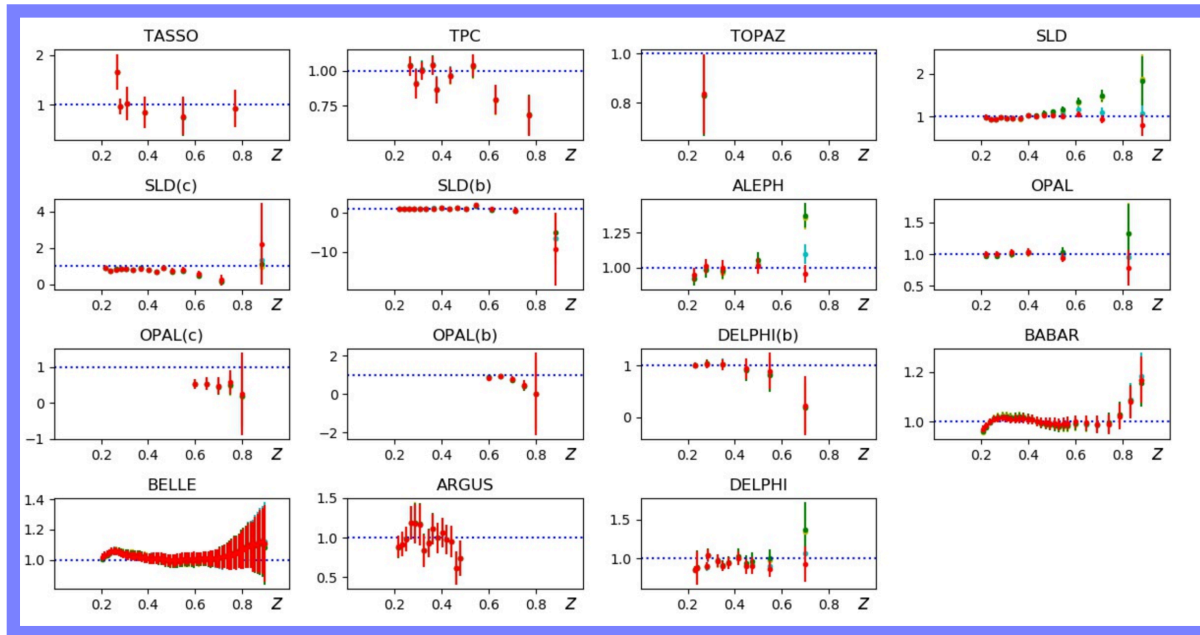
R_s



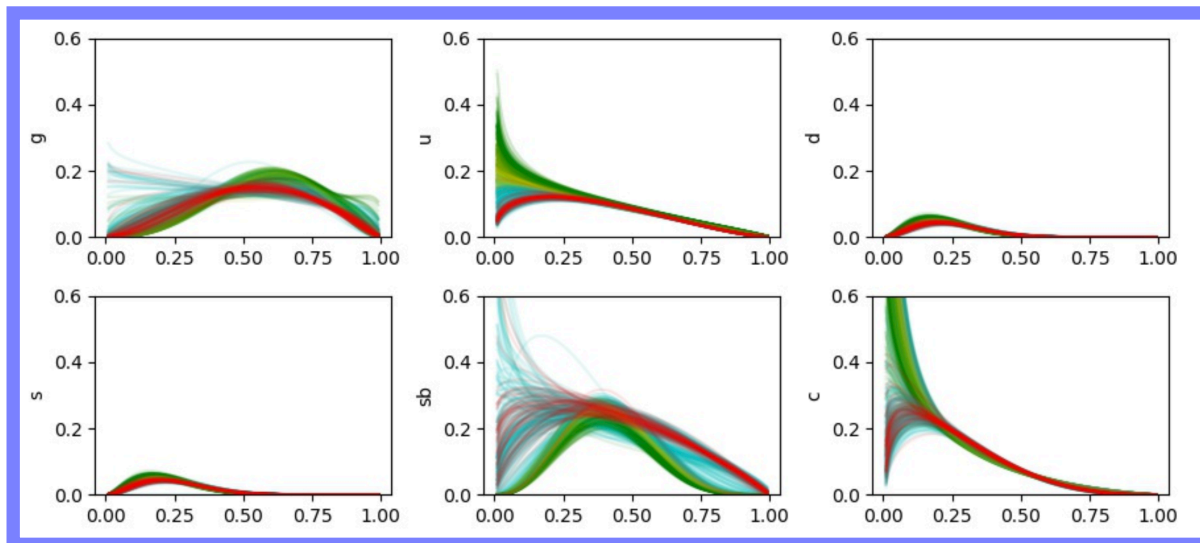
x

SIA K^+/K^- data

Data/Theory



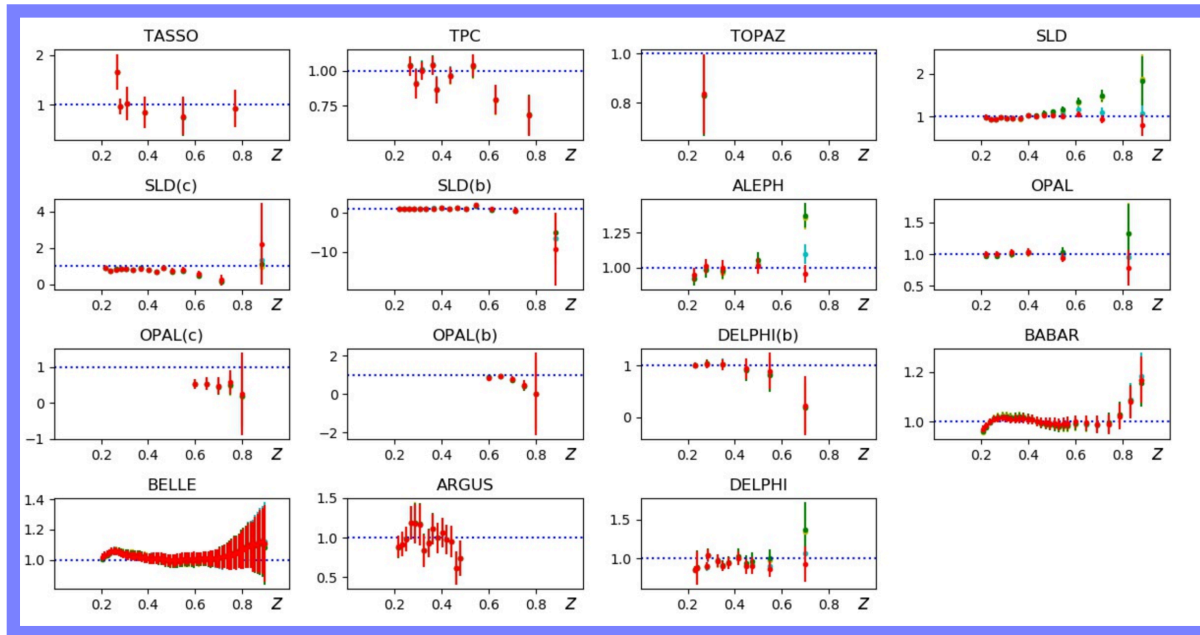
Z



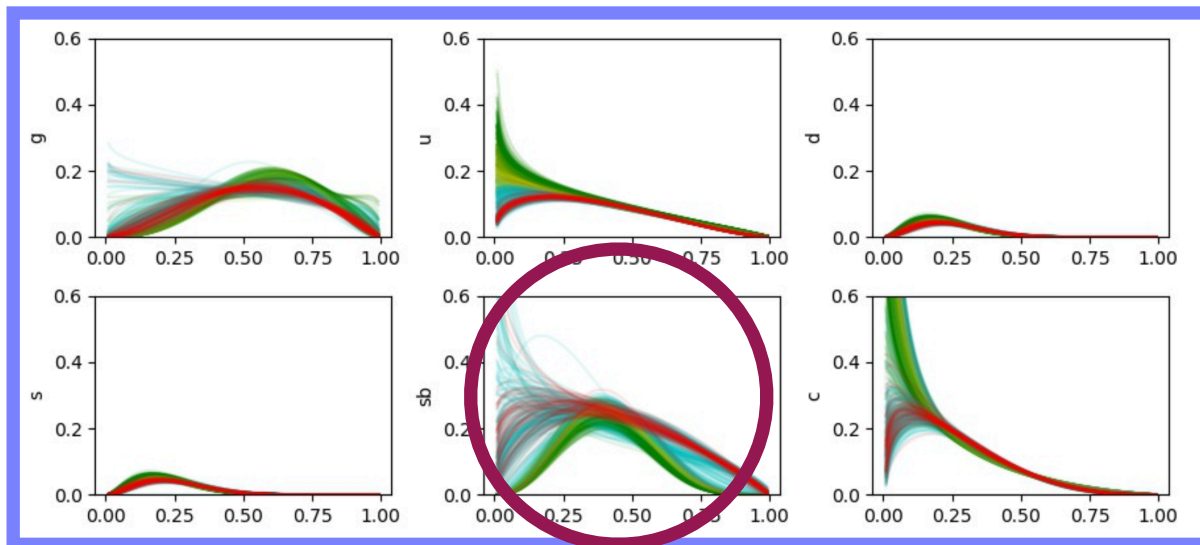
Z

SIA K^+/K^- data

Data/Theory



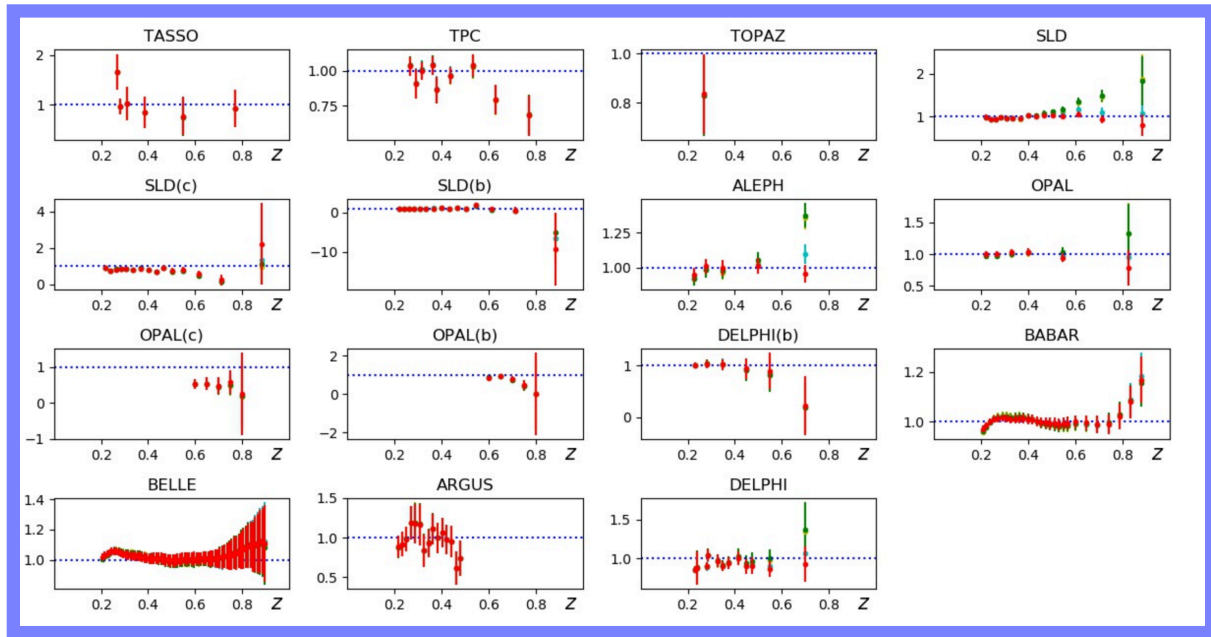
Z



Z

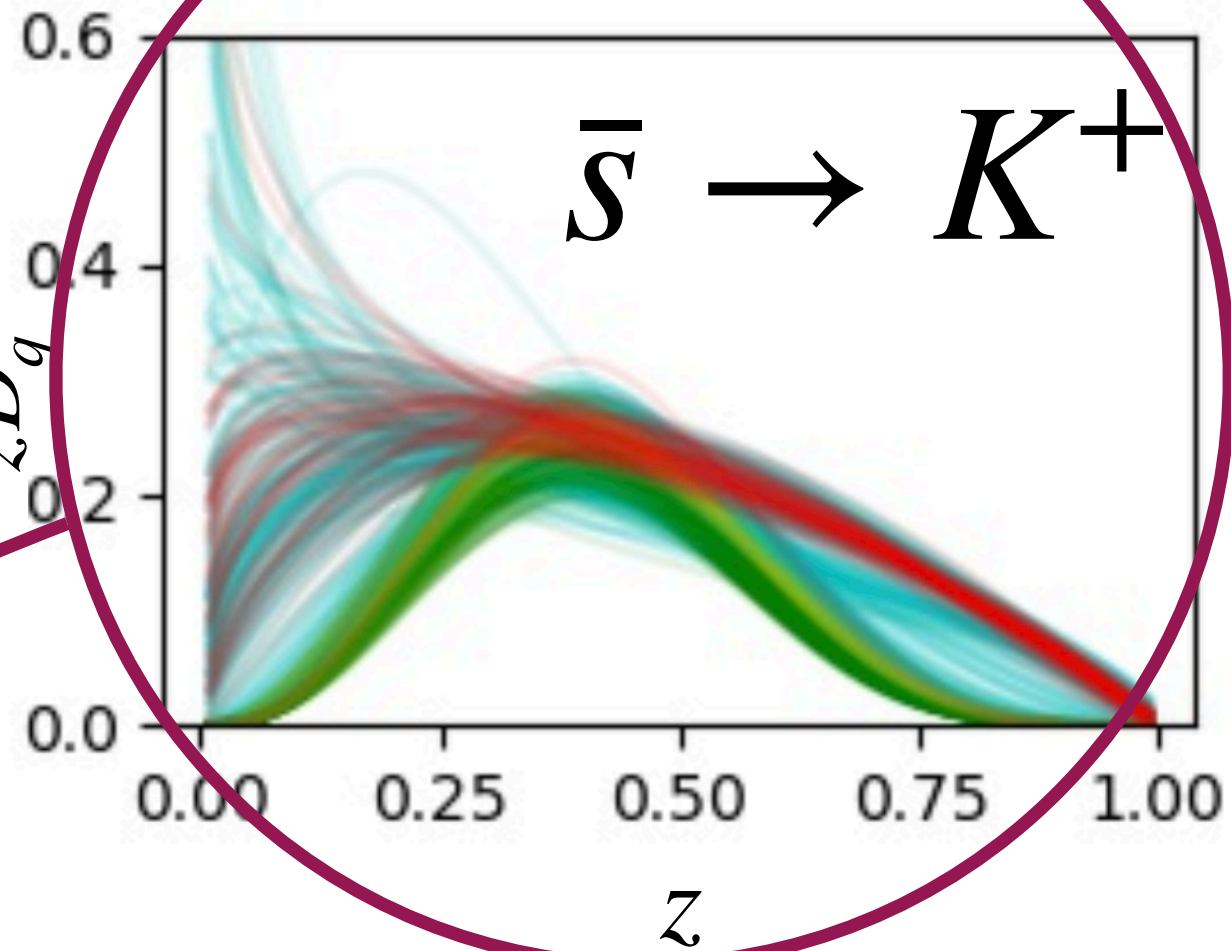
SIA K^+/K^- data

Data/Theory

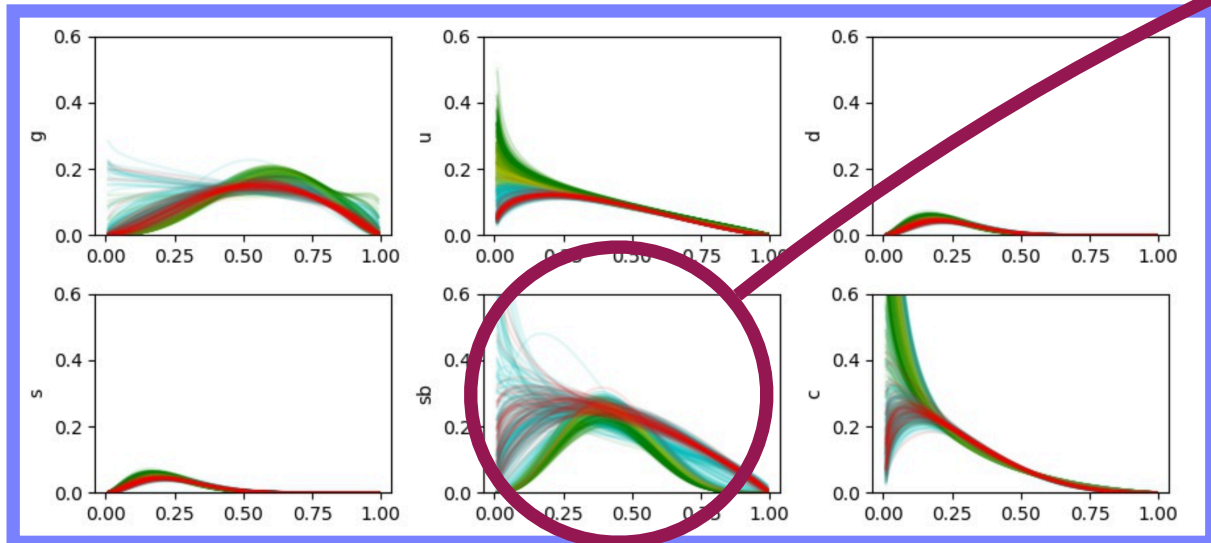


z

zD_q^{K+}



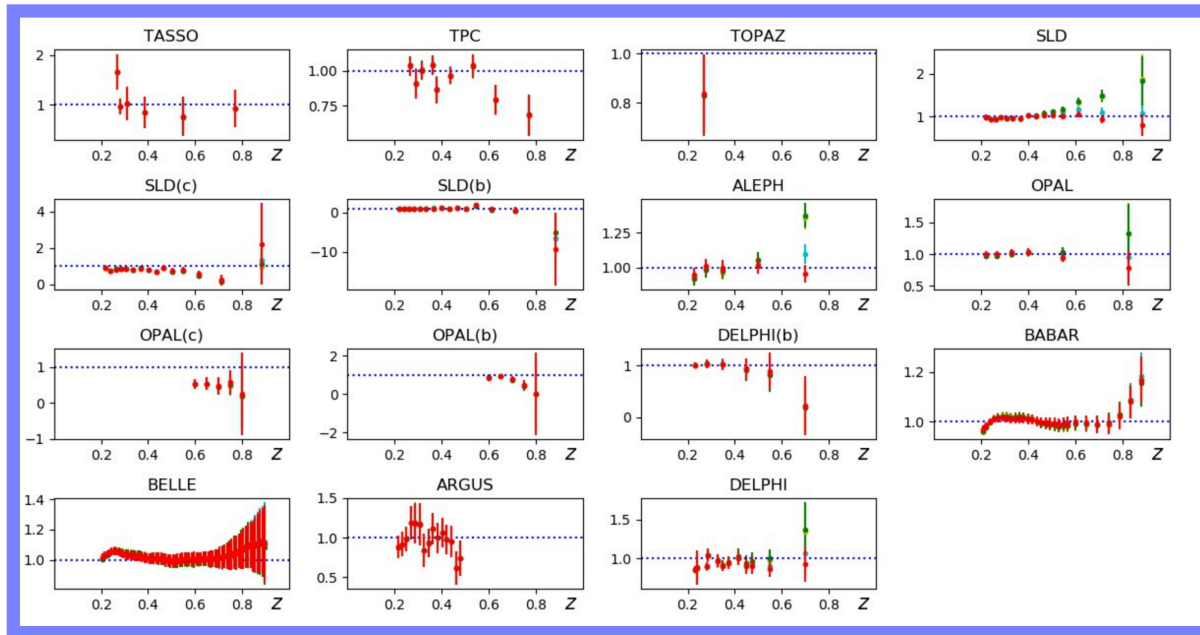
z



z

SIA K^+/K^- data

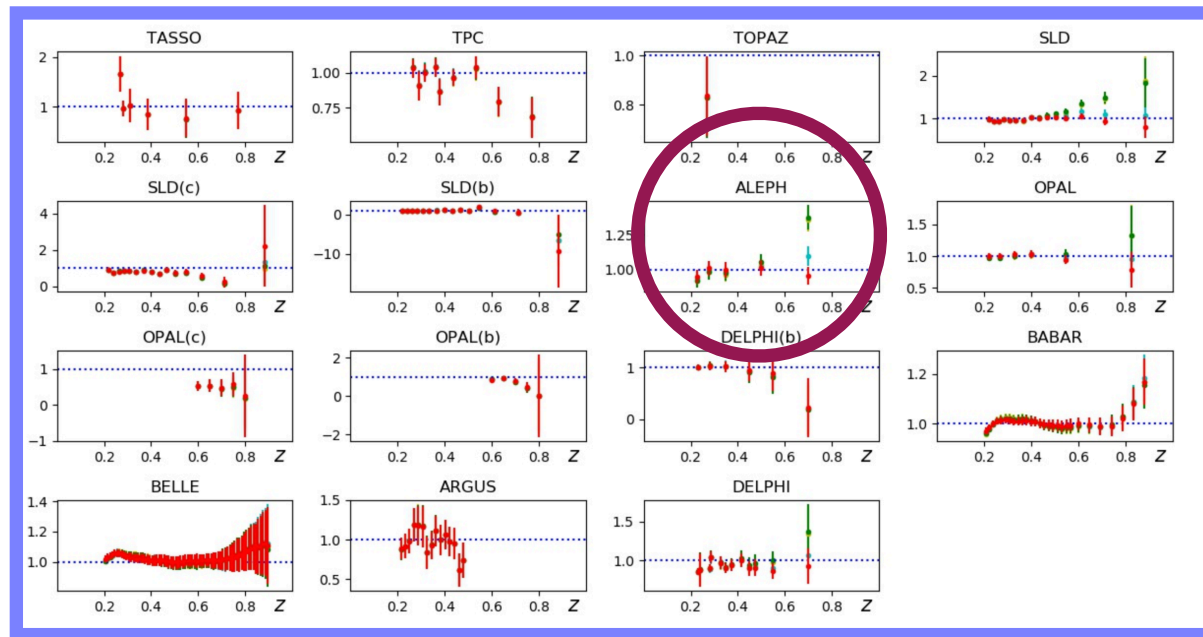
Data/Theory



Z

SIA K^+/K^- data

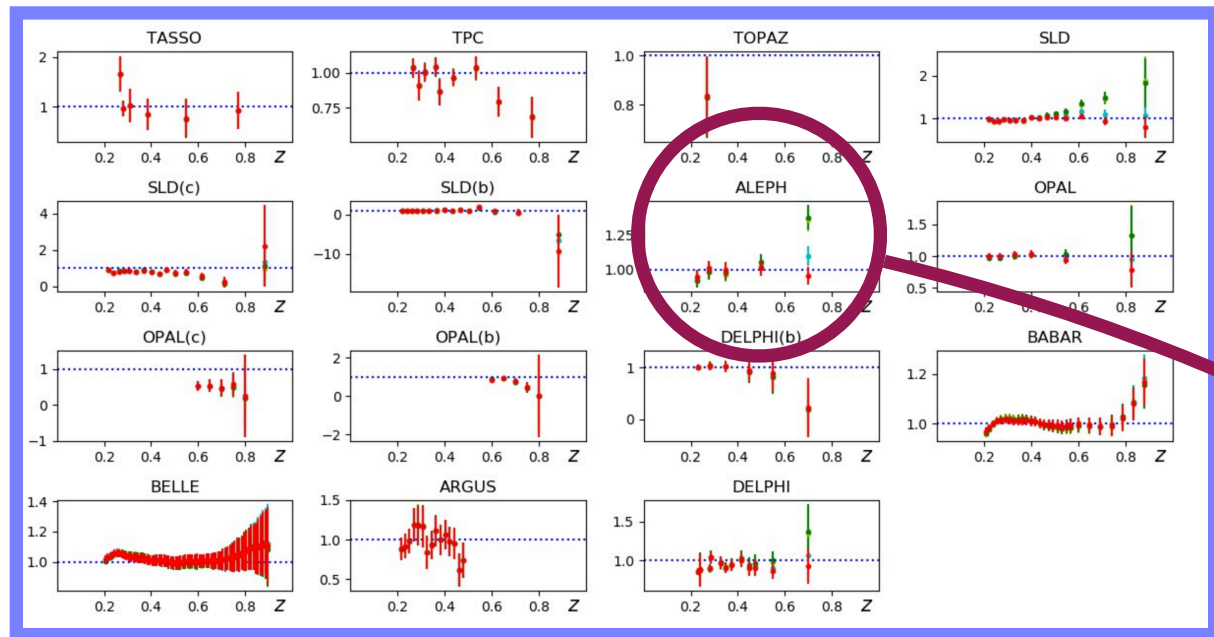
Data/Theory



$\sqrt{s}$

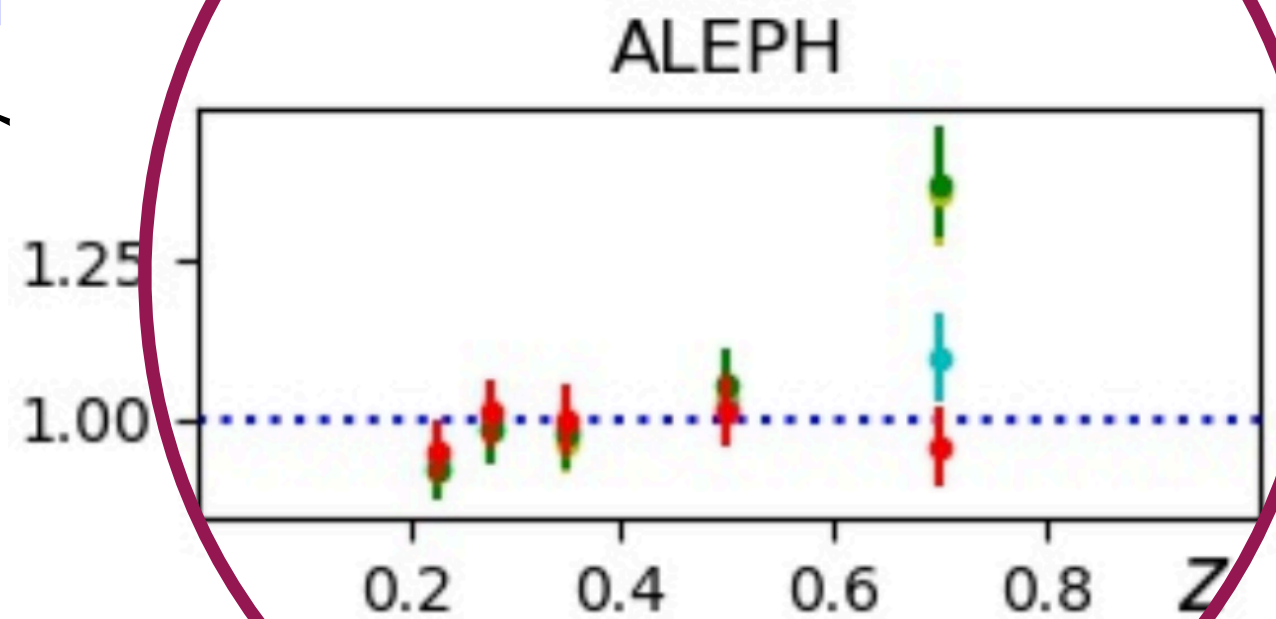
SIA K^+/K^- data

Data/Theory



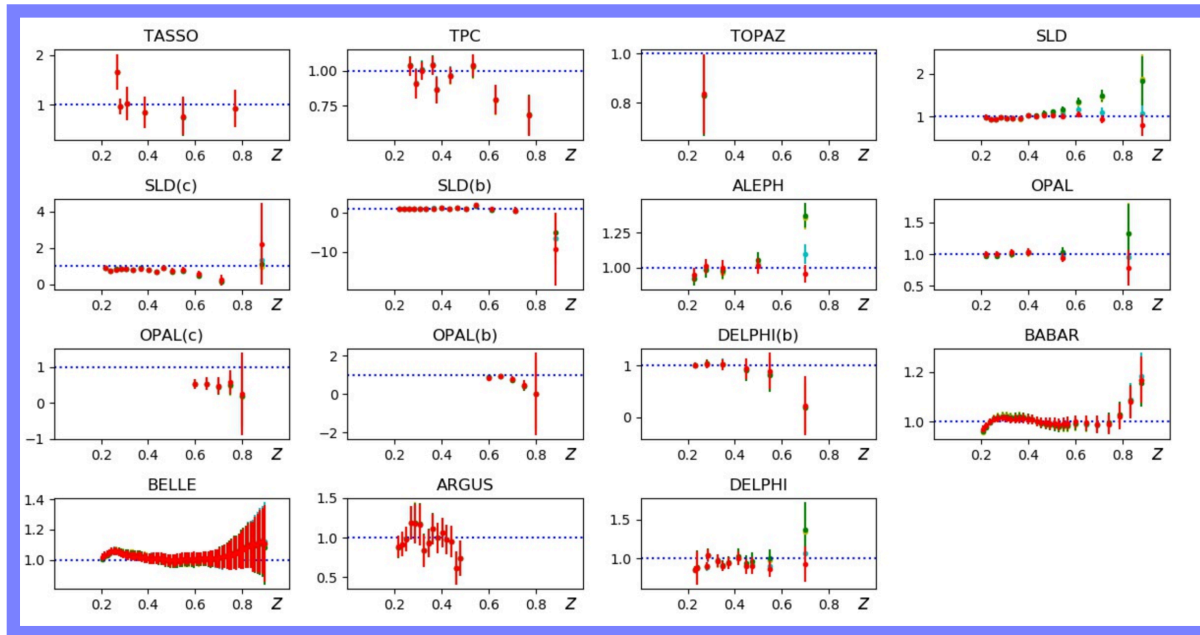
Z

Data/Theory



SIA K^+/K^- data

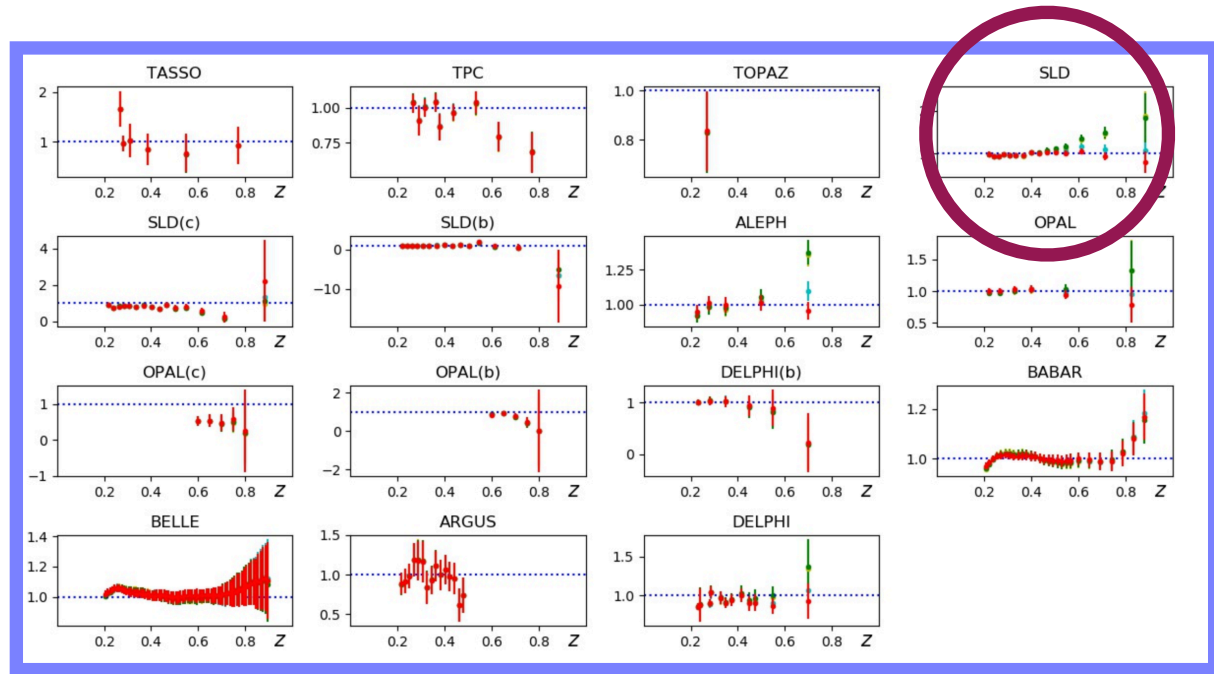
Data/Theory



Z

SIA K^+/K^- data

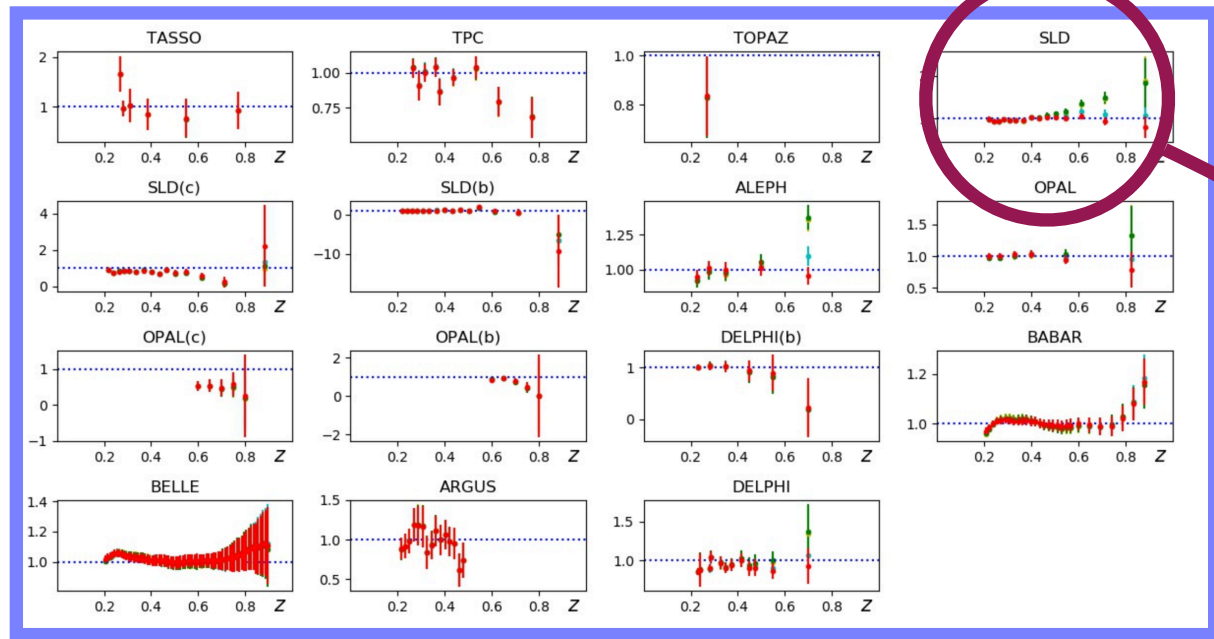
Data/Theory



Z

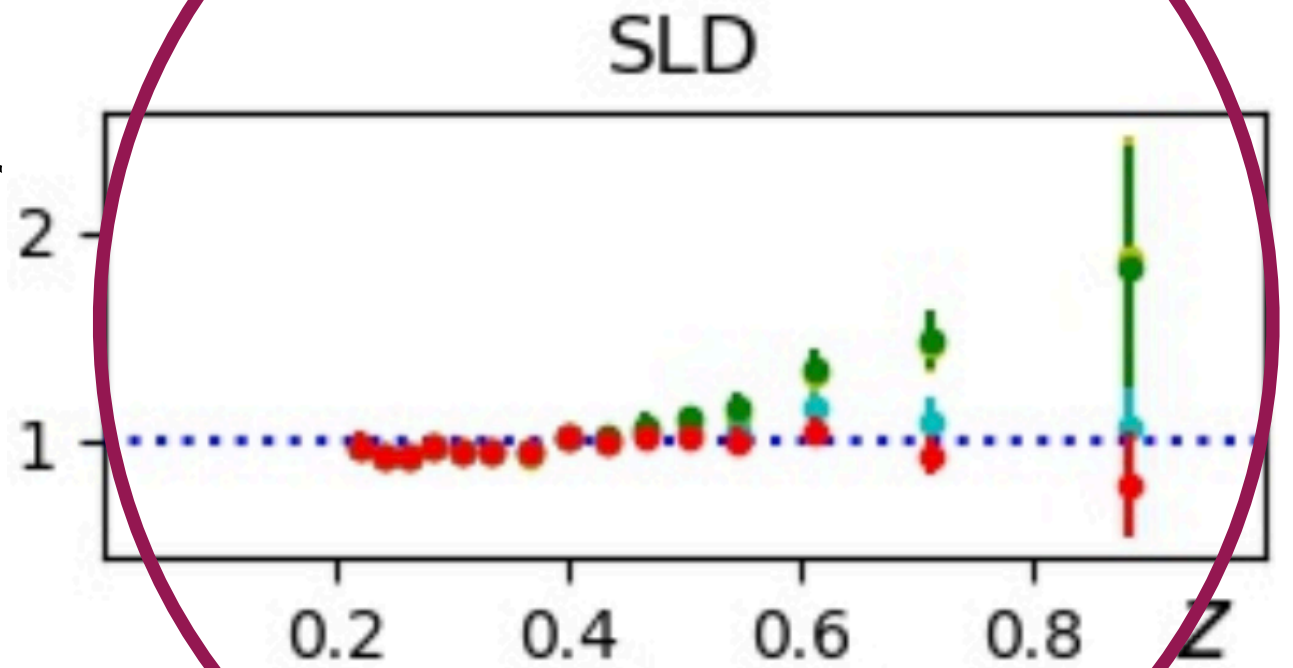
SIA K^+/K^- data

Data/Theory



Z

Data/Theory



SIDIS K-

SIA

Unfavored solutions

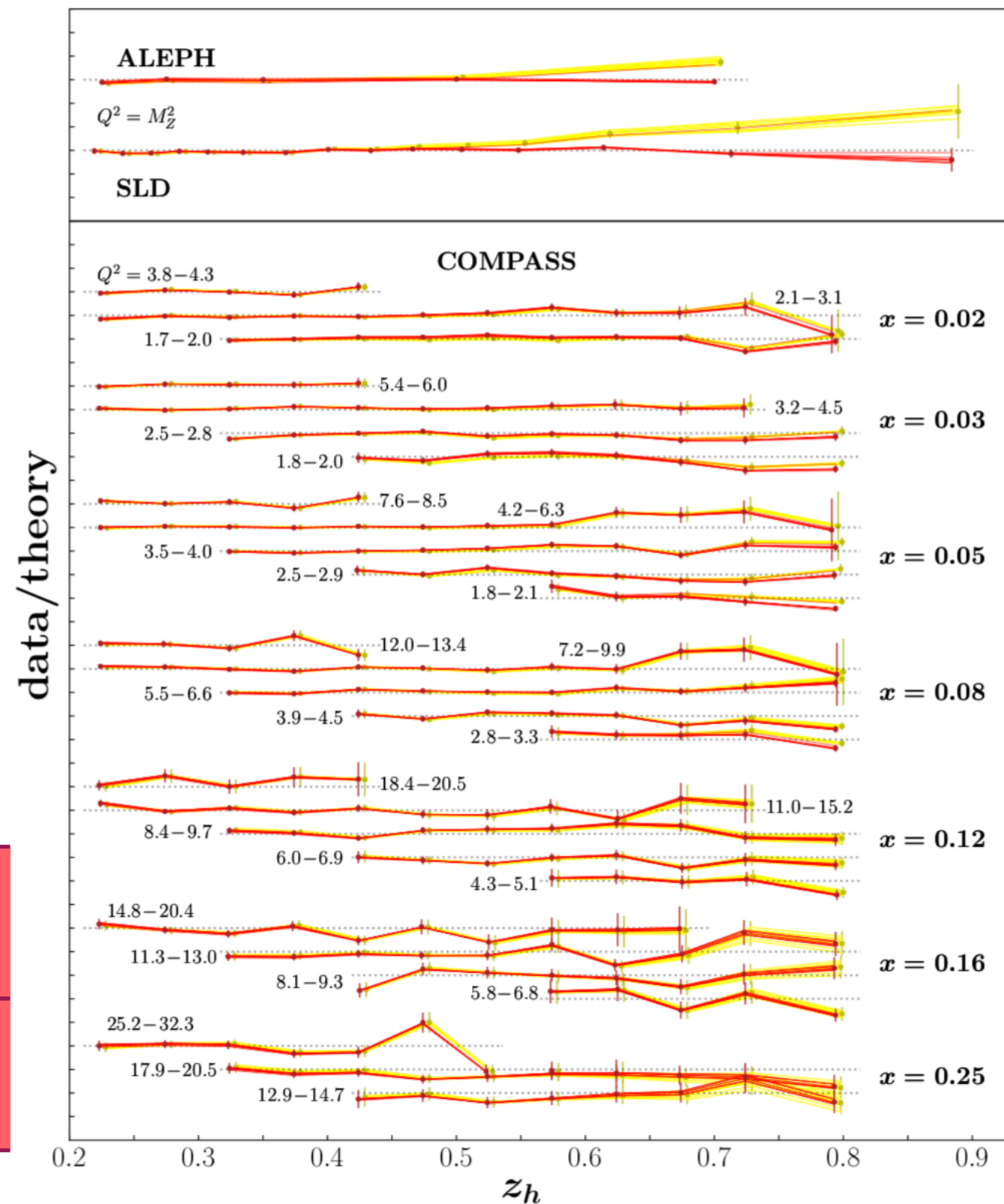
Large $s(x)$

Small $D_{s^\pm}^{K^\pm}(z)$

Favored solutions

Large $D_{s^\pm}^{K^\pm}(z)$

Small $s(x)$



SIDIS

$$\chi_{\text{SLD}}^2 = 4.10$$

$$\chi_{\text{SLD}}^2 = 1.38$$

$$\chi_{\text{ALEPH}}^2 = 4.62$$

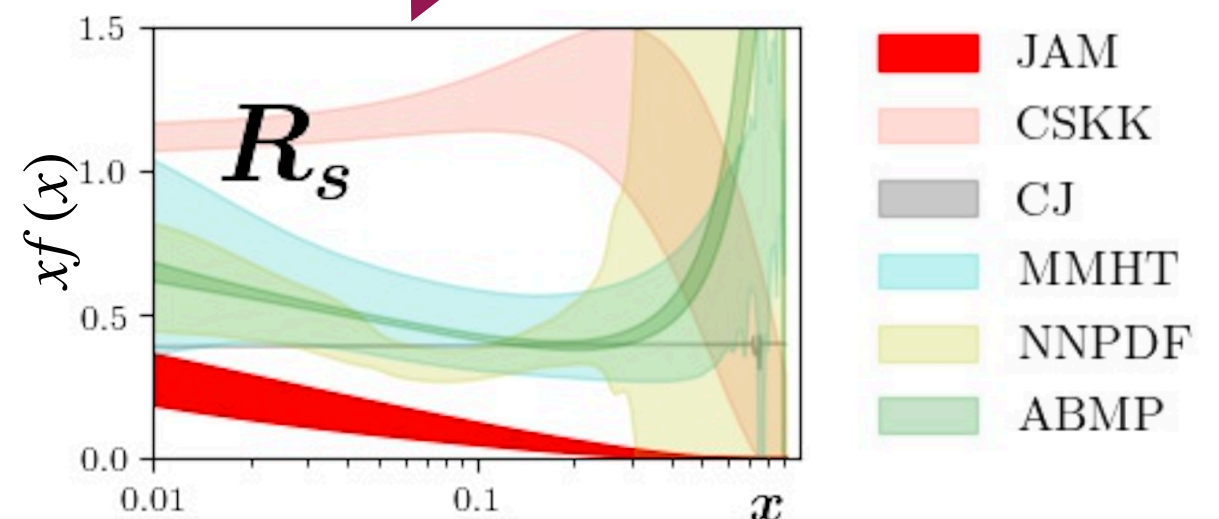
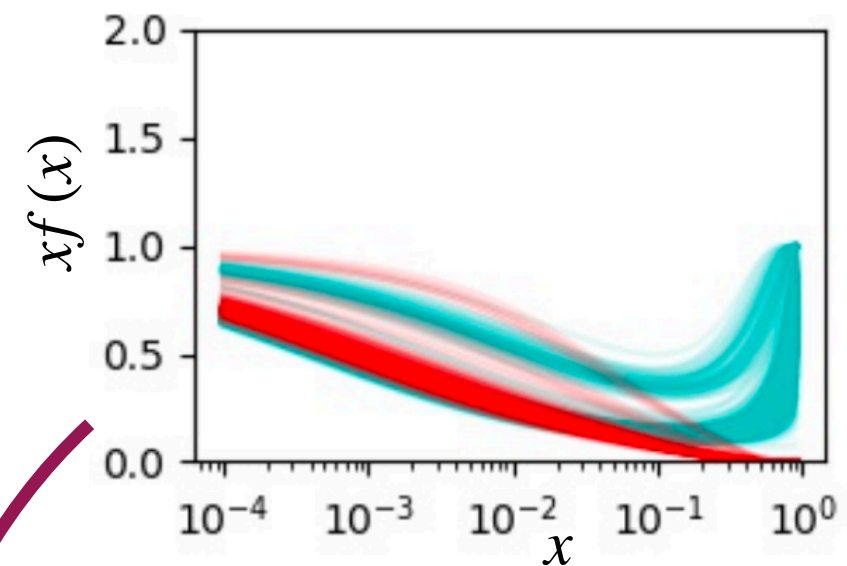
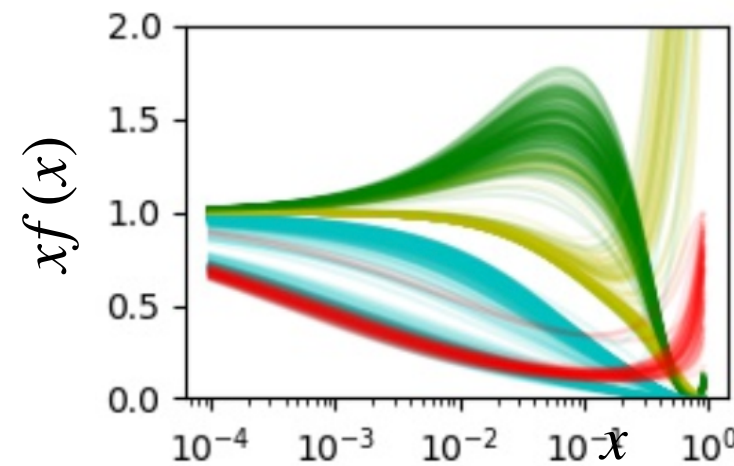
$$\chi_{\text{ALEPH}}^2 = 0.34$$

JAM19: Selection Criteria

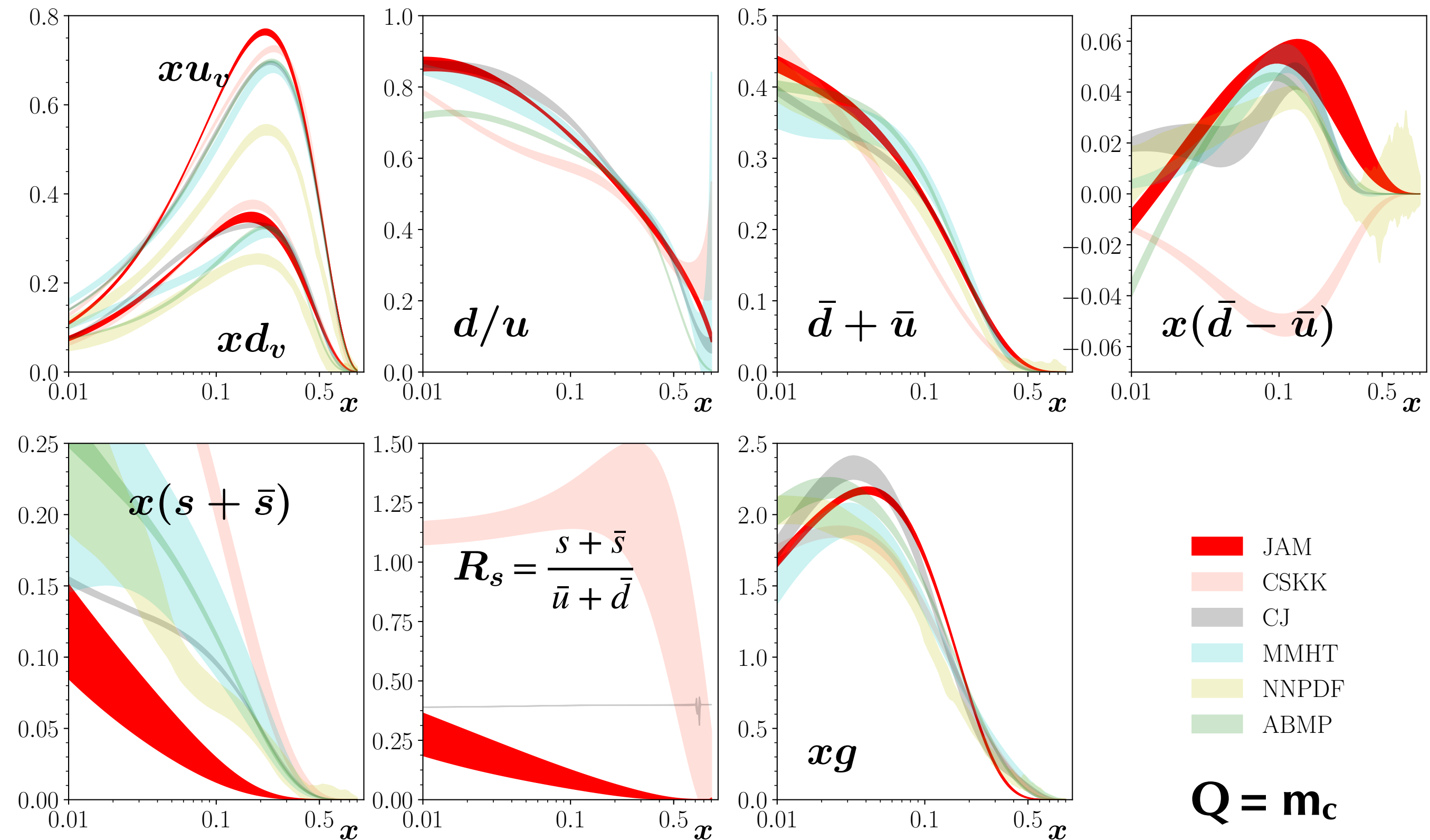
- Apply k-means clustering
- Classify clusters by increasing order in 'extended' reduced χ^2

$$\frac{\chi^2}{N_{\text{tot}}} + \sum_{\text{exp}} \frac{\chi_{\text{exp}}^2}{N_{\text{exp}}}$$

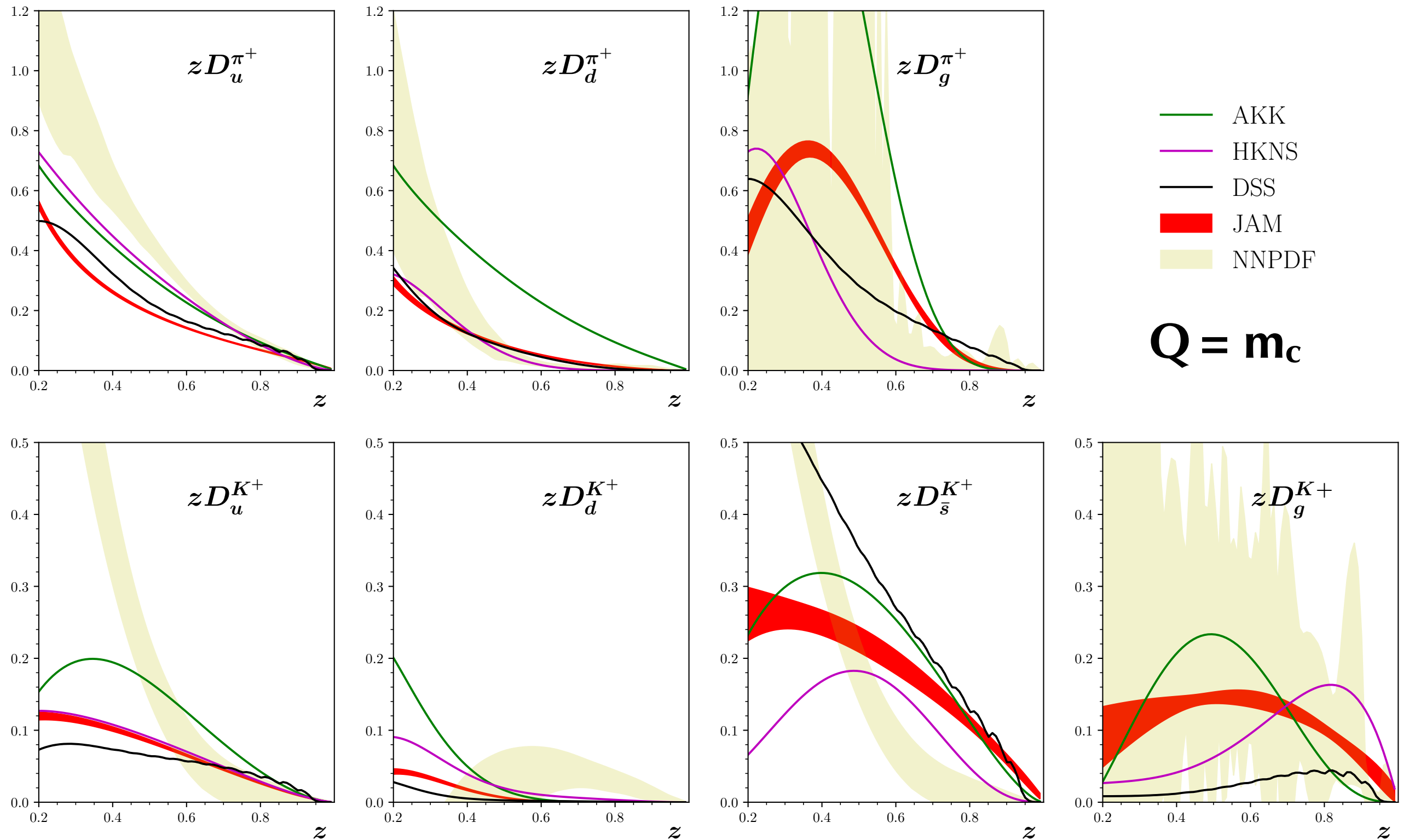
- Perform a new sampling with flat priors around the best cluster



JAM19: PDFs



JAM19: FF



Summary

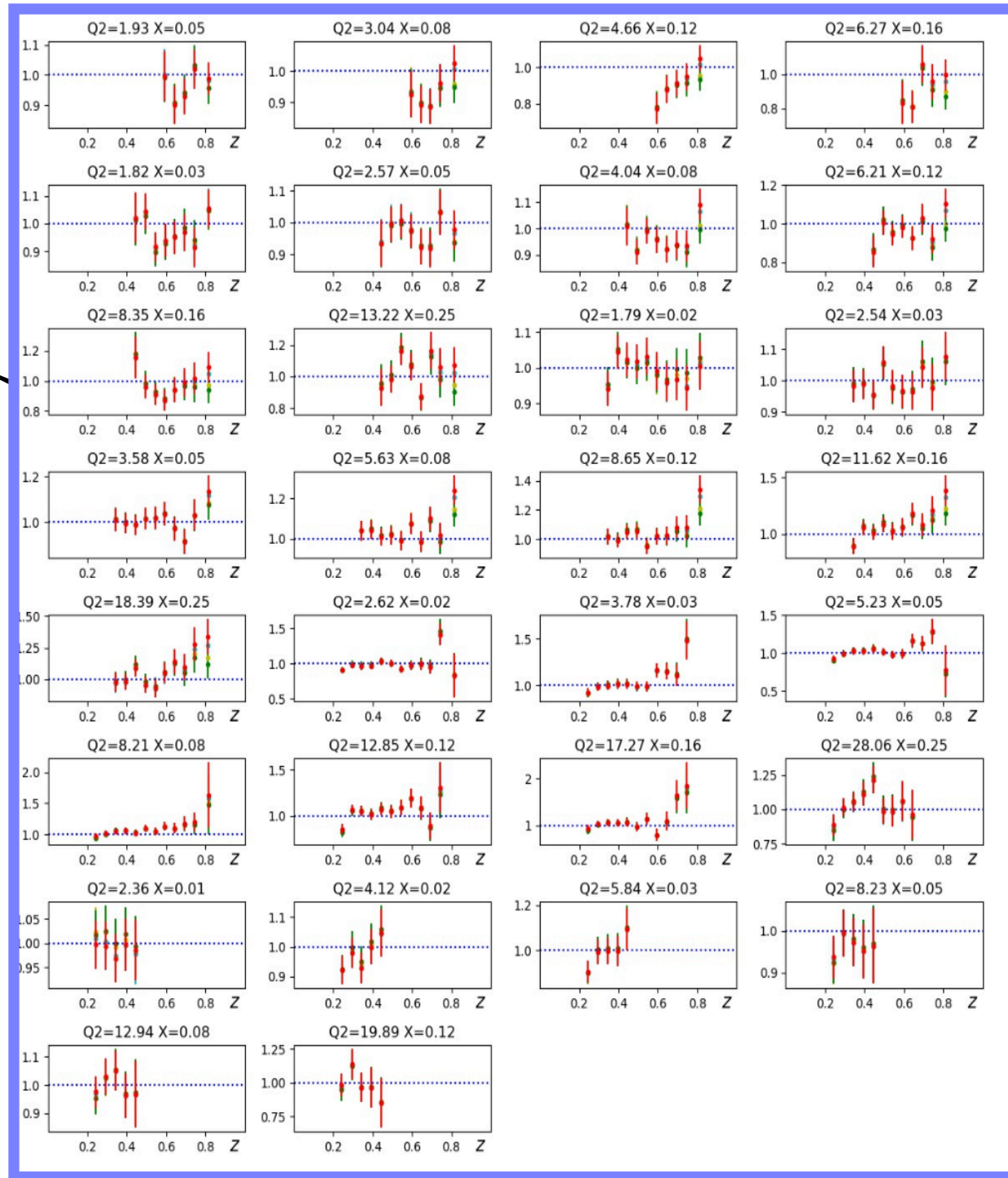
- MC statistical methods are important for a robust extraction of non-perturbative collinear distributions
 - Crucial for future Global TMDs, GPDs analysis
- First MC fit of PDFs and FFs using DIS, DY, SIDIS and SIA data
- JAM19 Methodology: MC (multi-steps), k-means clustering, 'extended' reduced χ^2
- Strange PDF strongly suppressed

Thanks

Backup

SIDIS K- data

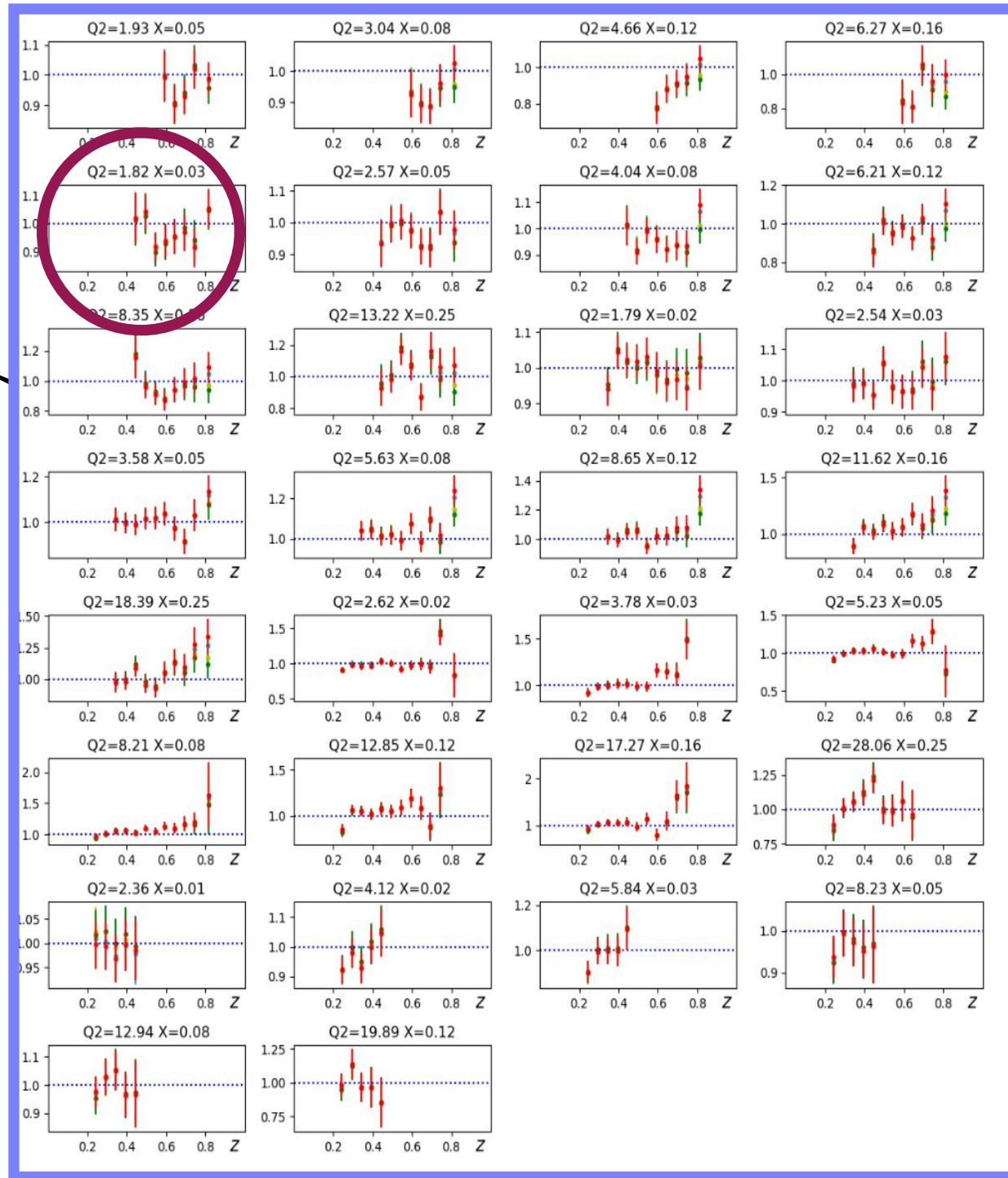
Data/Theory



Z

SIDIS K- data

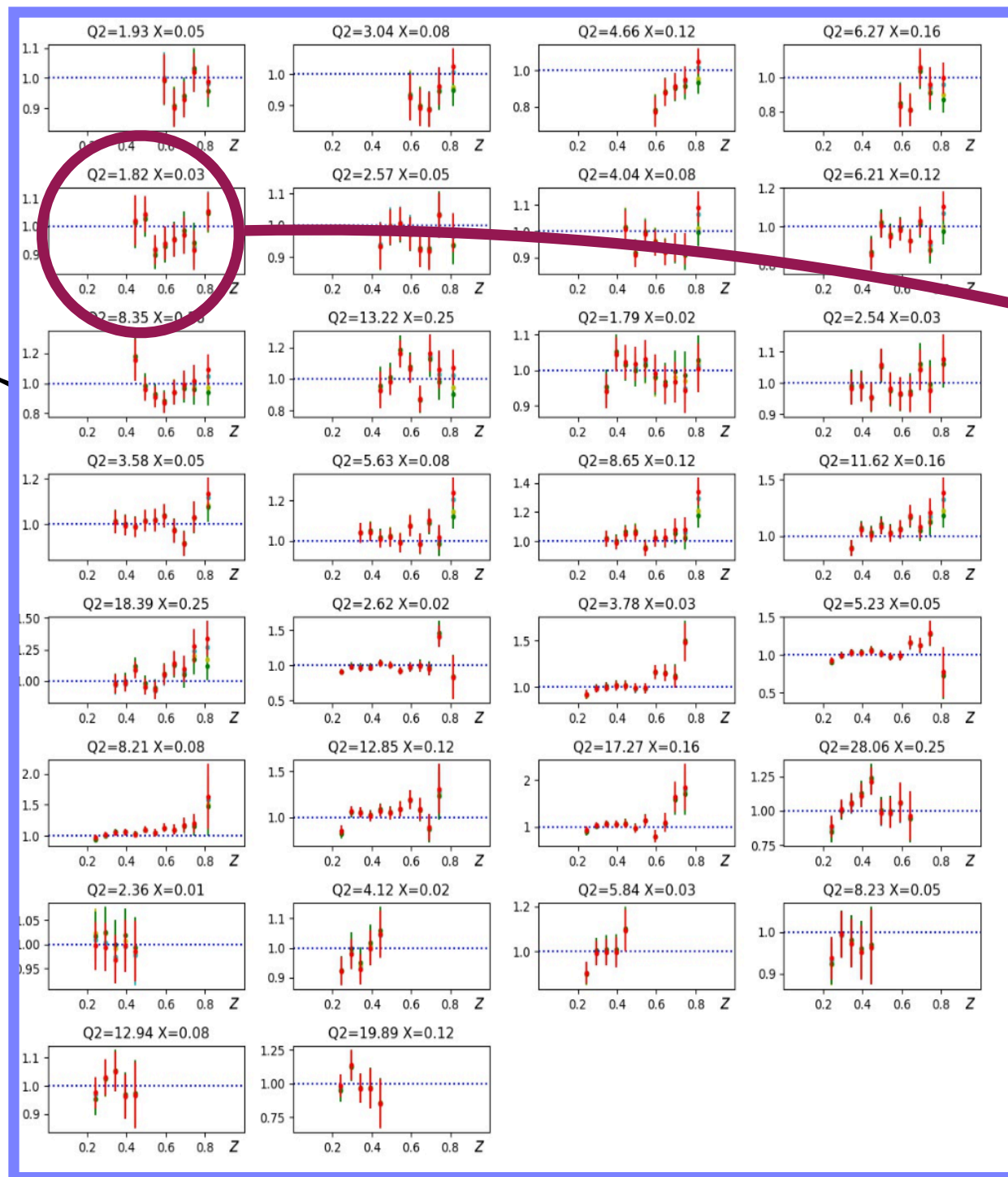
Data/Theory



Z

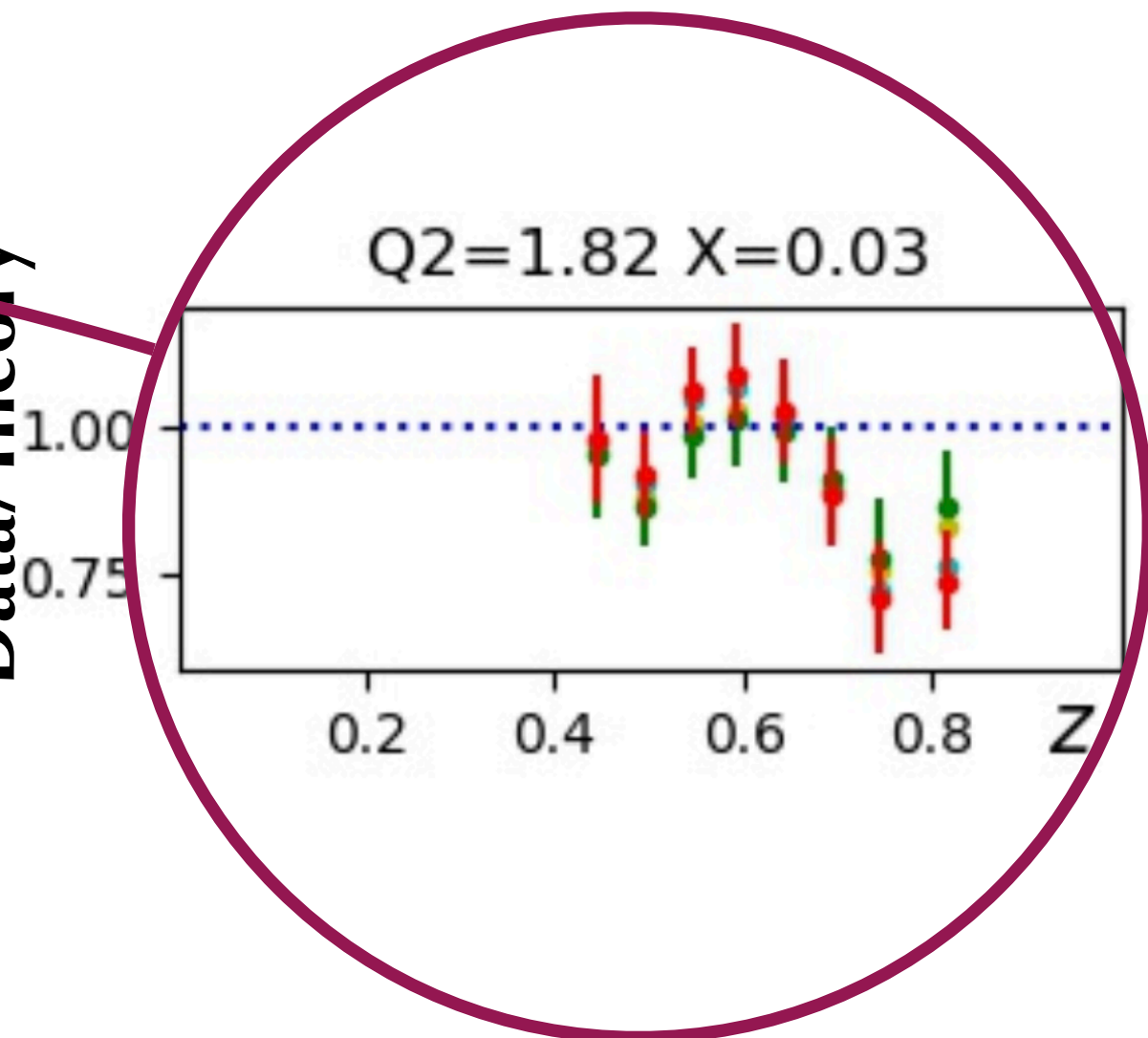
SIDIS K- data

Data/Theory



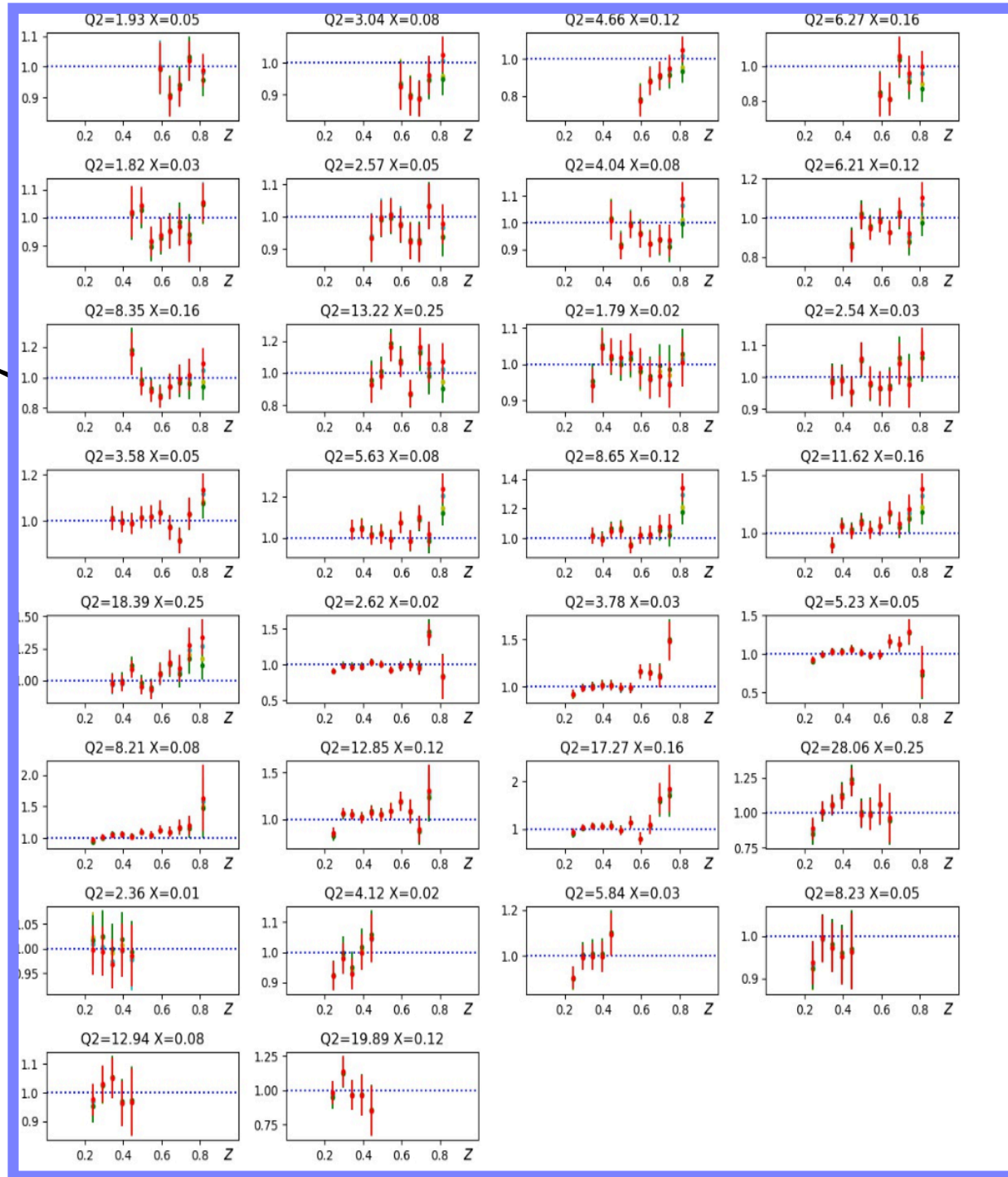
Z

Data/Theory



SIDIS K^+ data

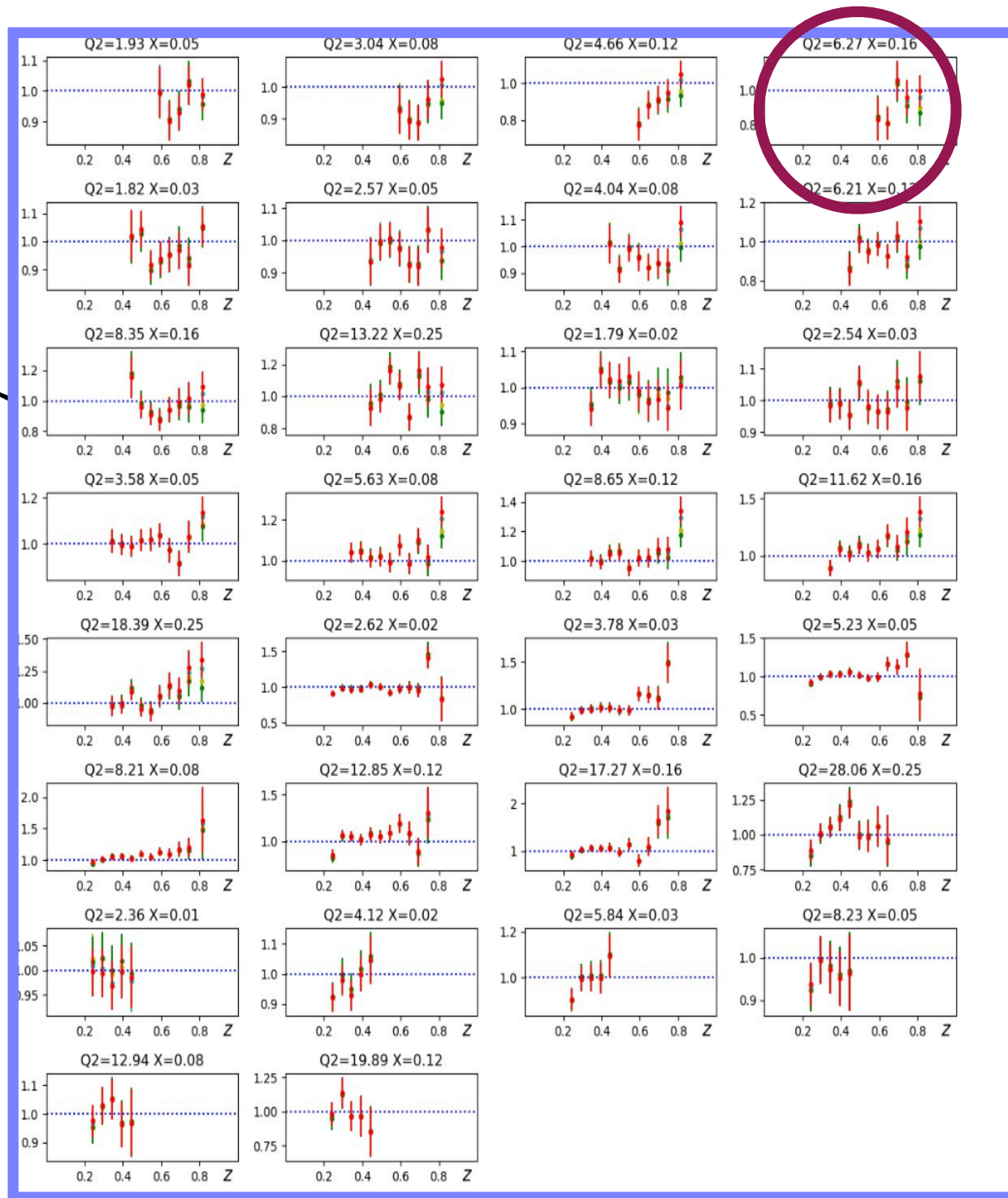
Data/Theory



Z

SIDIS K^+ data

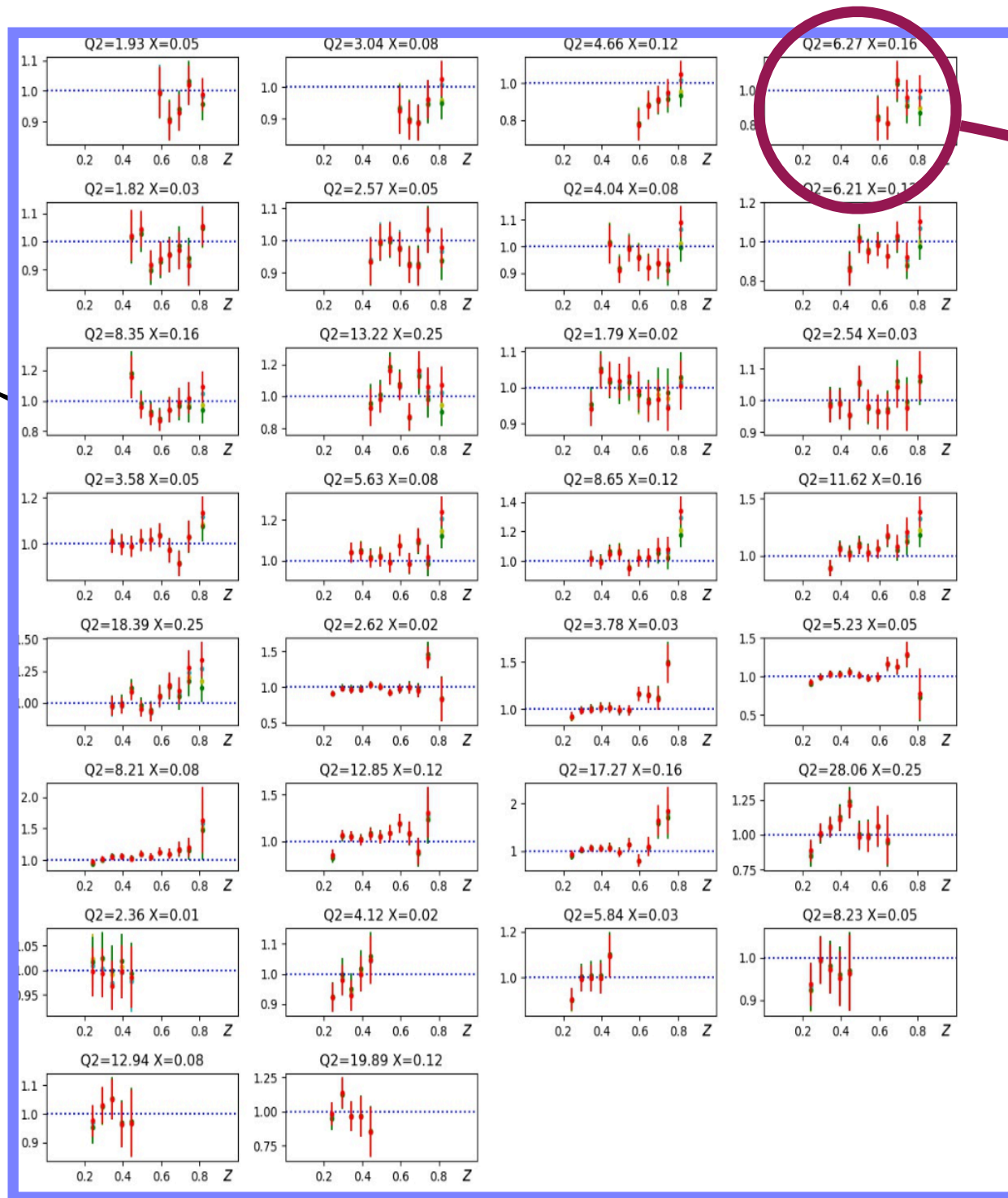
Data/Theory



Z

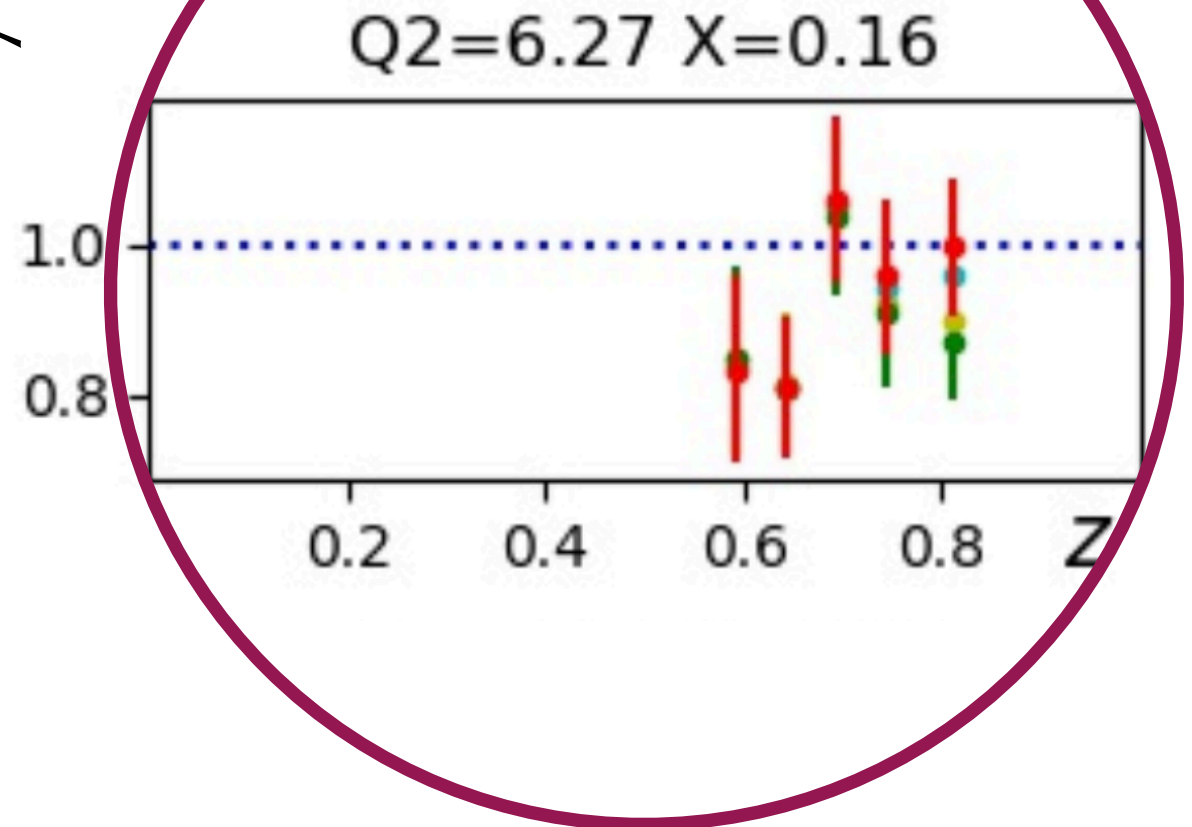
SIDIS K^+ data

Data/Theory

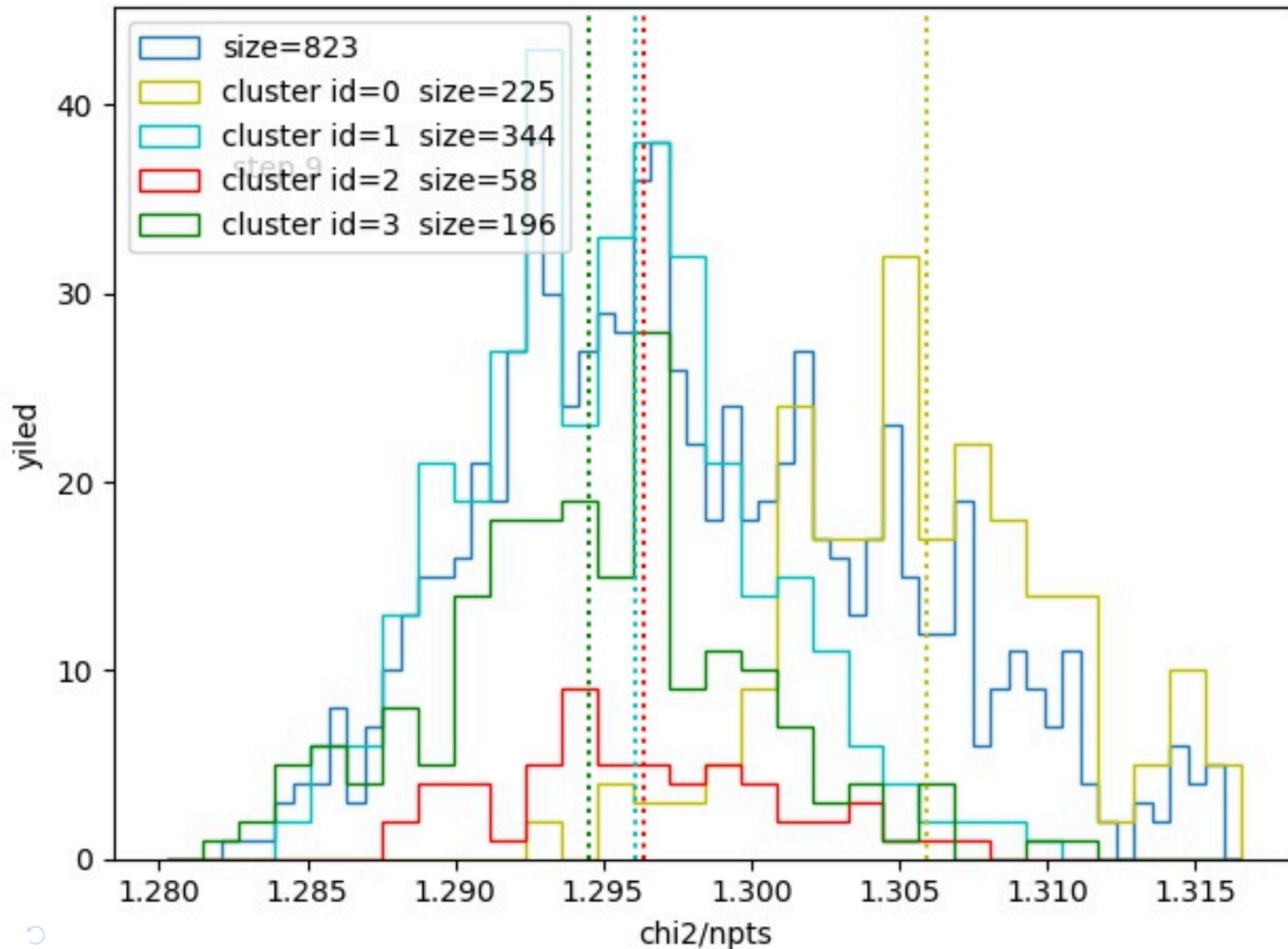


Z

Data/Theory



Chi2



Chi2

Reaction	N_{dat}	χ^2	χ^2/N_{dat}
SIDIS	992	1243.12	1.25
SIA	444	562.80	1.27
DIS	2680	3437.96	1.28
DY	250	416.29	1.67

Reaction	N_{dat}	χ^2	χ^2/N_{dat}
SIDIS ($\pi^\pm$)	498	585.48	1.18
SIDIS($K^\pm$)	494	657.64	1.33
SIA($\pi^\pm$)	231	247.27	1.07
SIA ($K^\pm$)	213	315.53	1.48

Experiment	target	hadron	N_{dat}	χ^2/N_{dat}
COMPASS	d	π^+	249	1.26
COMPASS	d	π^-	249	1.09
COMPASS	d	K^+	247	1.24
COMPASS	d	K^-	247	1.43

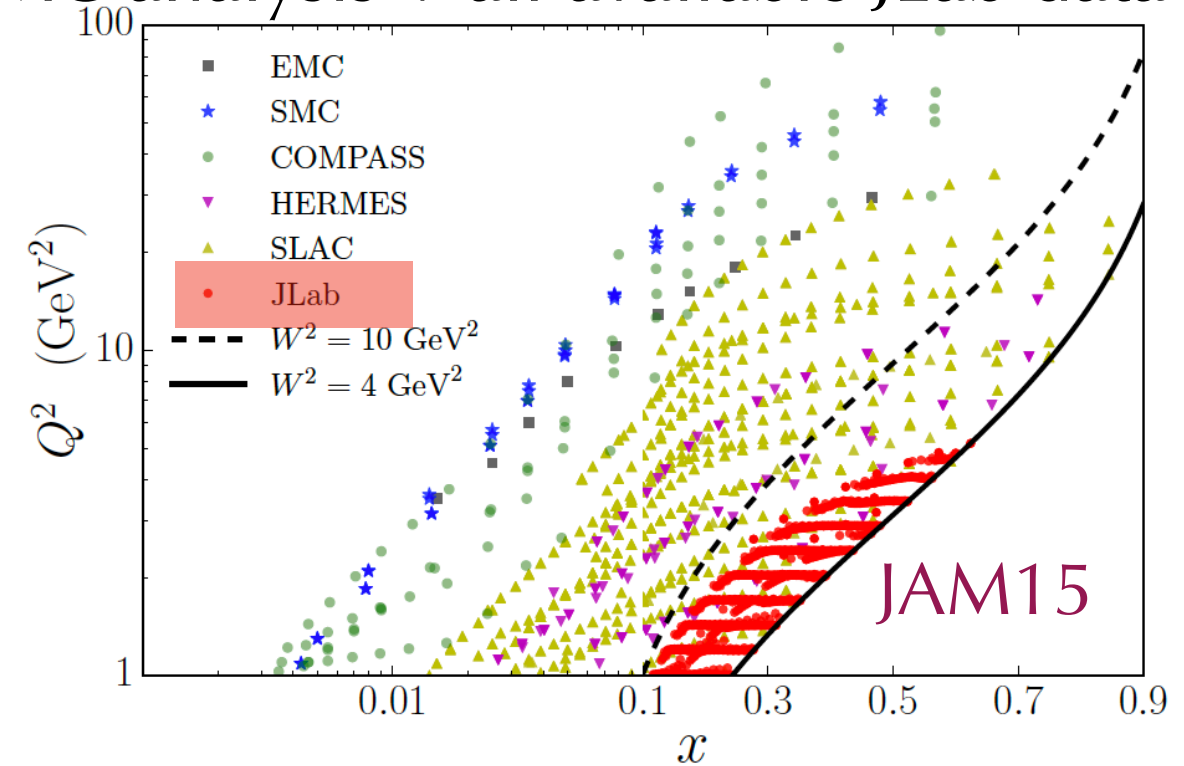
Evolution of JAM

JAM15

Iterative MC fitting technique

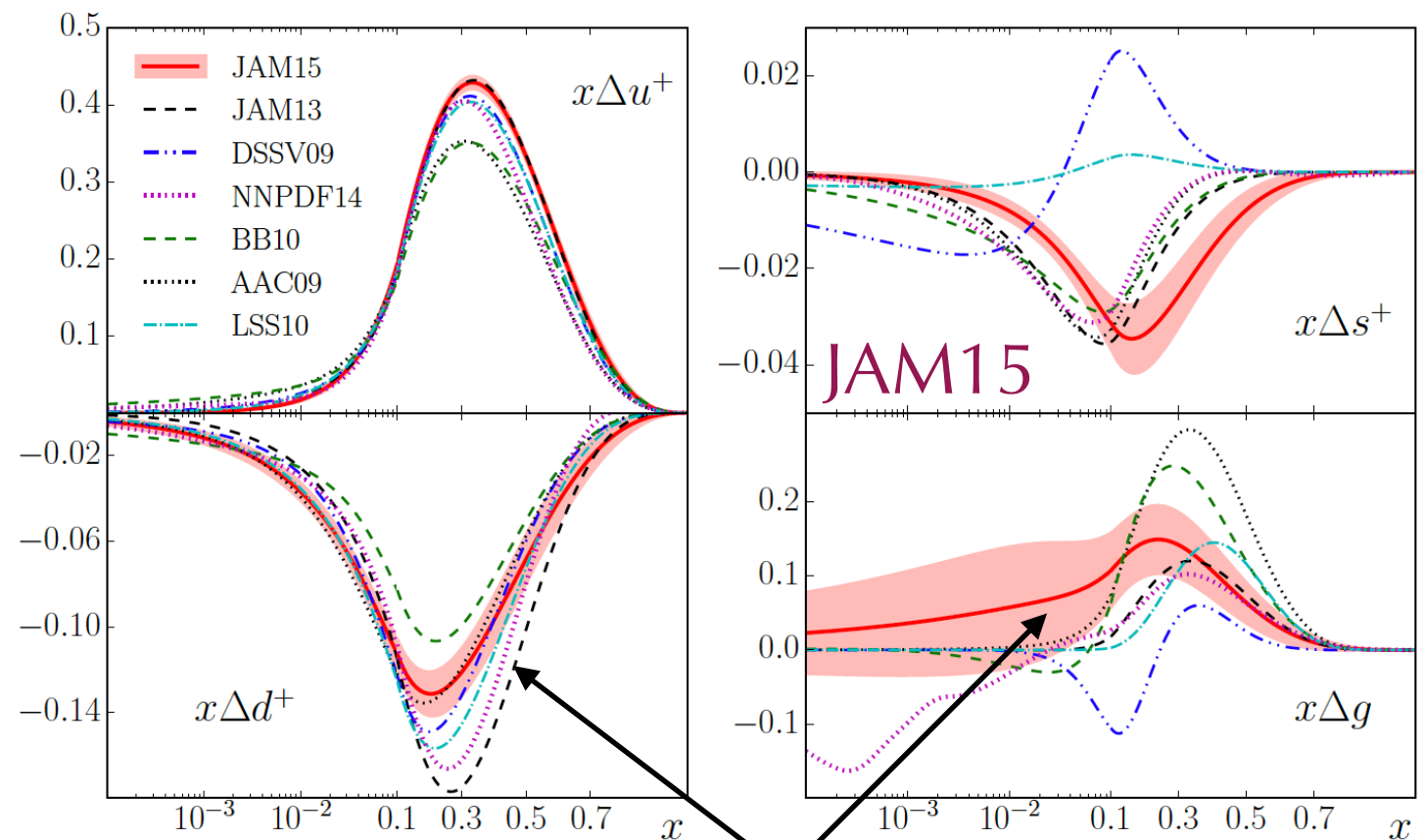
		JAM15	JAM16	JAM17	JAM18
Process	DIS	✓	✗	✓	✓
	SIA	✗	✓	✓	✓
	SIDIS	✗	✗	✓	✓
	DY	✗	✗	✗	✓
Function	f	✗	✗	✗	✓
	Δf	✓	✗	✓	✓
	D_f^h	✗	✓	✓	✓

IMC analysis + all available JLab data



Uses CJ12 NLO unpolarized PDFs

- Δu^+ and Δd^+ consistent with previous analysis
- Δs^+ slightly harder

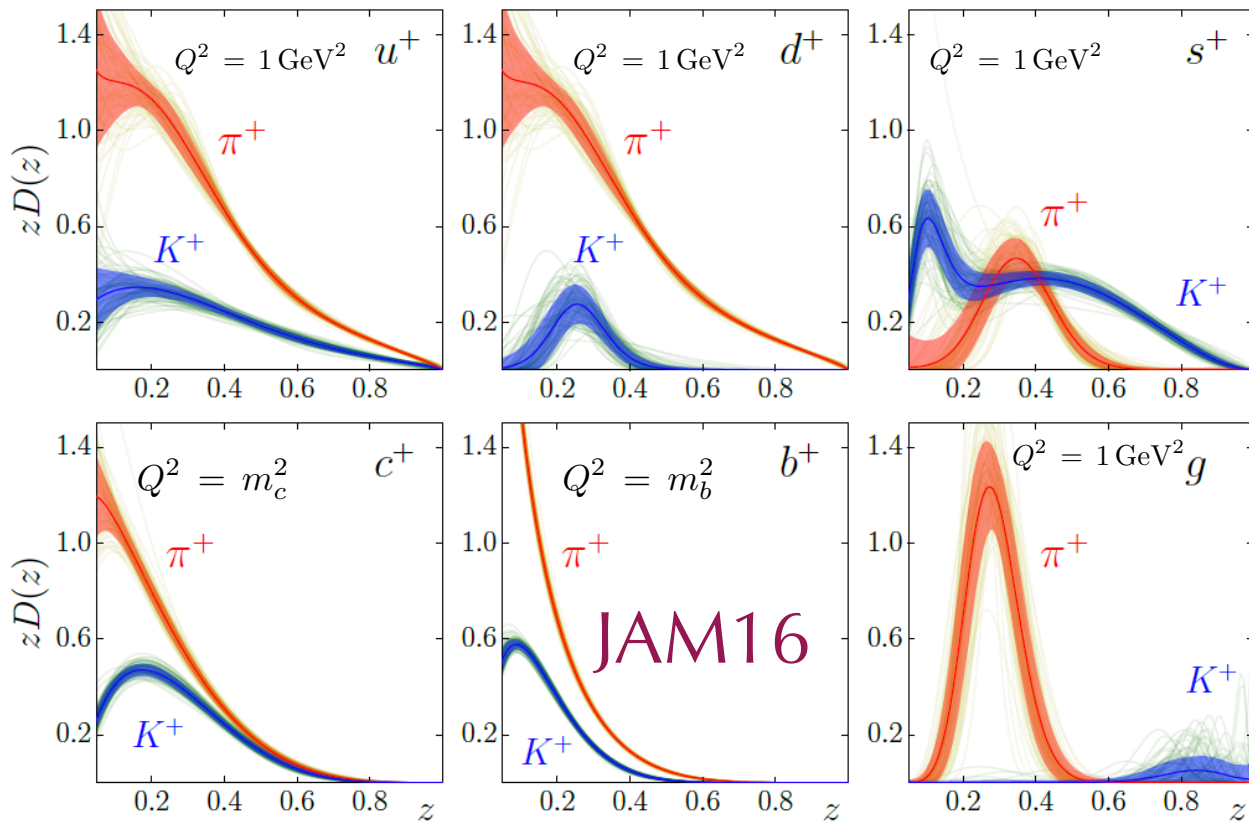


Sato, Melnitchouk, Kuhn, Ethier, Accardi
Phys. Rev. D 93, 074005 (2016)

Impact of JLab data

JAM16

- First IMC analysis of FFs
- Only SIA included



Sato, Ethier, Melnitchouk, Hirai, Kumano and Accardi
Phys. Rev. D 94, 114004 (2016)

JAM17 FFs better agreement
with other analysis

JAM17

- First (simultaneous) MC analysis of polarized PDFs and FFs
- Polarized SIDIS, polarized DIS and SIA included

