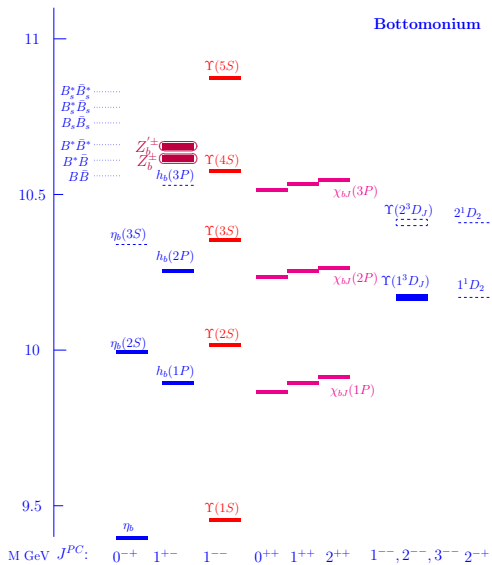


Trying to understand the $XYZ \dots P_c$

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[illegible]



The exotic menu

Exotic: not fitting the template Mesons = $(q\bar{q})$, Baryons = (qqq) .

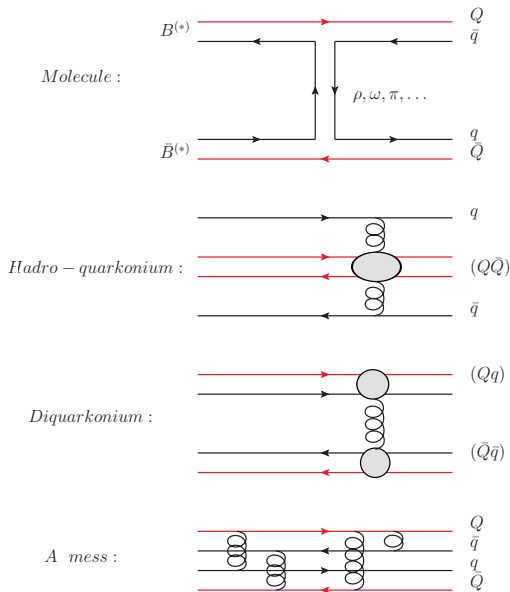
► Charmonium-like

- $X(3872)$ ($D^0 D^{*0}$), $\rightarrow J/\psi \rho$ and $J/\psi \omega$, isospin badly broken,
- $Z_c^{\pm,0}(3900)$ (DD^*), $\rightarrow J/\psi \pi$,
- $Z_c^{\pm}(4020)$, ($D^* \bar{D}^*$), $\rightarrow h_c \pi^{\pm}$,
- $Z_1^{\pm}(4050)$, $Z_2^{\pm}(4250) \rightarrow \chi_{c1} \pi^{\pm}$,
- $Z_c^{\pm}(4100) \rightarrow \eta_c \pi^{\pm}$,
- $Z_c^{\pm}(4200) \rightarrow J/\psi \pi^{\pm}$,
- $Z^{\pm}(4430)$, $\rightarrow \psi(2S) \pi^{\pm}$,
- $Y(4260)$ [4220] $\rightarrow J/\psi \pi \pi$, $h_c \pi \pi$ (almost no open charm),
- $Y(4360) \rightarrow \psi(2S) \pi \pi$, $h_c \pi \pi$ (almost no open charm),
- Pentaquark(s):
 $P_c(4380)$, $P_c(4440)$, $P_c(4457)$, $P_c(4312) \rightarrow J/\psi p$

► Bottomonium-like

- $Z_b^{\pm,0}(10610)$, (BB^*), $\rightarrow \Upsilon(nS) \pi$ ($n = 1, 2, 3$), $h_b(kP) \pi$ ($k = 1, 2$),
- $Z_b^{\pm,0}(10650)$, ($B^* \bar{B}^*$), $\rightarrow \Upsilon(nS) \pi$ ($n = 1, 2, 3$), $h_b(kP) \pi$ ($k = 1, 2$)

What is inside?



Likely all are present simultaneously.
Dominant — different in different particles.

Recall: deuteron — mostly a pn molecule, and about 5% - a mess.

Molecules

- ▶ Must be very close to the threshold. At binding/excitation energy δ , the characteristic size

$$r \sim 1/\sqrt{M\delta} \approx \begin{cases} 4.5 \text{ fm} \sqrt{\frac{1 \text{ MeV}}{\delta}} & \text{charmonium-like} \\ 2.8 \text{ fm} \sqrt{\frac{1 \text{ MeV}}{\delta}} & \text{bottomonium-like} \end{cases}$$

- ▶ A clear-cut example: $Z_b(10610) = Z_b$, $Z_b(10650) = Z'_b$

$$M(Z_b) = 10607.2 \pm 2.0 \text{ MeV} [M(BB^*) = 10604.1 \pm 0.3 \text{ MeV}],$$

$$M(Z'_b) = 10652.2 \pm 1.5 \text{ MeV} [M(B^* \bar{B}^*) = 10649.7 \pm 0.6 \text{ MeV}]$$

$$Z_b \sim \frac{B^* \bar{B} - \bar{B}^* B}{\sqrt{2}}, \quad Z'_b \sim B^* \bar{B}^*$$

- ▶ Produced in $\Upsilon(5S) \rightarrow Z_b^{(')} \pi$.

Observed in $Z_b^{(')} \rightarrow \Upsilon(1, 2, 3S) \pi$ and $Z_b^{(')} \rightarrow h_b(1, 2P) \pi$.

Also $Z_b \rightarrow B^* \bar{B} + c.c.$, $Z'_b \rightarrow B^* \bar{B}^*$.

- ▶ In charmonium-like sector: $X(3872)$, $Z_c(3900)$, $Z_c(4020)$.

Heavy Quark Spin Symmetry (HQSS) and Molecules

- ▶ HQ spin-dependent interaction of heavy Q

$$H_s = -\frac{\vec{\sigma} \cdot \vec{B}}{2M_Q} \sim \frac{\Lambda_{QCD}^2}{M_Q} \ll \Lambda_{QCD}$$

- ▶ E.g. $\Upsilon(2S) \rightarrow \Upsilon(1S)\eta$ requires $b\bar{b}$ spin rotation (Ampl. $\propto (\vec{p}_\eta \cdot [\vec{\Upsilon}_2 \times \vec{\Upsilon}_1])$):

$$\Gamma[\Upsilon(2S) \rightarrow \Upsilon(1S)\eta] \sim 10^{-3} \Gamma[\Upsilon(2S) \rightarrow \Upsilon(1S)\pi\pi]$$

- ▶ In a widely separated $B^{(*)}\bar{B}^{(*)}$ pair the spin of b is not correlated with the spin of $\bar{b}$. Rather

$$H_{spin} = \mu (\vec{s}_b \cdot \vec{s}_{\bar{q}}) + \mu (\vec{s}_{\bar{b}} \cdot \vec{s}_q), \quad \mu = M(B^*) - M(B) \approx 45 \text{ MeV}$$

- ▶ The spin of the $b\bar{b}$ pair (S_H) is mixed. In the $J^{PC} = 1^{+-}$ state:

$$B^*\bar{B} - \bar{B}^*B \sim 0_H^- \otimes 1_L^- + 1_H^- \otimes 0_L^- \quad B^*\bar{B}^* \sim 0_H^- \otimes 1_L^- - 1_H^- \otimes 0_L^-$$

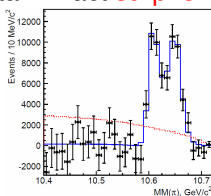
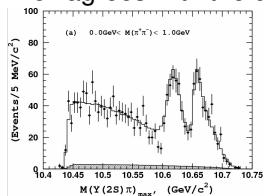
Spin structure of $Z_b^{(\prime)}$

- If the $H \otimes L$ spin composition of pairs of **free** mesons is retained in Z_b and Z_b' ,

$$Z_b \sim 0_H^- \otimes 1_L^- + 1_H^- \otimes 0_L^- \quad Z_b' \sim 0_H^- \otimes 1_L^- - 1_H^- \otimes 0_L^- ,$$

then

- $M(Z_b') - M(Z_b) \approx M(B^*) - M(B) \approx 45 \text{ MeV}$, $\Gamma(Z_b') \approx \Gamma(Z_b)$, in particular $\Gamma(Z_b') \rightarrow B^* \bar{B} + c.c.$ should be small;
- $A[Z_b' \rightarrow \Upsilon(nS) \pi] \approx -A[Z_b \rightarrow \Upsilon(nS) \pi]$, $A[Z_b' \rightarrow h_b(kP) \pi] \approx +A[Z_b \rightarrow h_b(kP) \pi]$;
- $A[\Upsilon(5S) \rightarrow Z_b' \pi] \approx -A[\Upsilon(5S) \rightarrow Z_b \pi]$;
- Definite and opposite sign of interference of Z_b and Z_b' in the $\pi\pi$ cascades from $\Upsilon(5S)$ to ortho- and para- states of $b\bar{b}$
- Well agrees with the data. In fact **surprisingly** well.

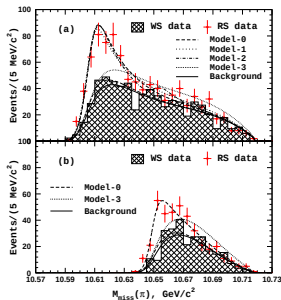


Interaction between heavy mesons in the $Z_b^{(\prime)}$

- ▶ No dependence on S_H (HQSS) — the interaction depends only on S_L .

$$V_0 = \langle 0_L^- | H | 0_L^- \rangle, \quad V_1 = \langle 1_L^- | H | 1_L^- \rangle.$$

- ▶ Exact preservation of the spin structure $\Rightarrow V_0 = V_1$. **LQSS???**
- ▶ Generally depends on the distance.
- ▶ Trivial at long distance (both vanishing).
- ▶ Surprising at short distance — interference in decays to bottomonium + pion, and



Apparent absence of decay $Z_b' \rightarrow B^* \bar{B} + c.c.$

$$V_0(q_0) \approx V_1(q_0),$$

$$q_0 = \sqrt{M_B \mu} \approx 0.5 \text{ GeV}$$

$V_0 = V_1 \Rightarrow$ All 4 other expected isovector threshold molecular states should exist

- S wave. $I^G = 1^-$ (C-even neutral component).

Other diagonal states of the Hamiltonian H_S :

$$W_{b2} : 1^-(2^+) : (1_H^- \otimes 1_L^-)|_{J=2}, \quad B^* \bar{B}^* ;$$

$$W_{b1} : 1^-(1^+) : (1_H^- \otimes 1_L^-)|_{J=1}, \quad B^* \bar{B} + \bar{B}^* B ;$$

$$W'_{b0} : 1^-(0^+) : \frac{\sqrt{3}}{2} (0_H^- \otimes 0_L^-) + \frac{1}{2} (1_H^- \otimes 1_L^-)|_{J=0}, \quad B^* \bar{B}^* ;$$

$$W_{b0} : 1^-(0^+) : \frac{1}{2} (0_H^- \otimes 0_L^-) - \frac{\sqrt{3}}{2} (1_H^- \otimes 1_L^-)|_{J=0}, \quad B \bar{B} ;$$

- Each at the corresponding meson threshold. No cross-decays.
- Not accessible in single π transitions from $\Upsilon(5, 6S)$.
- Accessible in $\Upsilon(5, 6S) \rightarrow W_b + \gamma$ — small rate.
- W_{b0} maybe accessible in $\Upsilon(6S) \rightarrow W_{b0} \pi \pi$.
- Best: $e^+ e^- \rightarrow W_b \rho$ starting at 11.4÷11.5 GeV.

$Z_c(3900)$, $Z_c(4020)$ similar to $Z_b(10610)$, $Z_b(10650)$?

- ▶ $Z_c(3900) \rightarrow \eta_c \rho$ — seen (2.1 ± 0.8) $Z_c \rightarrow J/\psi \pi \Rightarrow$ "healthy" mixing of $c\bar{c}$ spin states in a molecule
- ▶ $Z_c(4020) \rightarrow D^* \bar{D}^*$ "seen", $Z_c(4020) \rightarrow D^* \bar{D}$ "not seen"
- ▶ Questions
 - ▶ $Z_c(4020) \rightarrow \eta_c \rho$ — ?
 - ▶ $Z_c(3900) \rightarrow J/\psi \pi$ "seen", $Z_c(3900) \rightarrow h_c \pi$ "not seen"
 - ▶ $Z_c(4020) \rightarrow h_c \pi$ "seen", $Z_c(4020) \rightarrow J/\psi \pi$ "not seen"
- ▶ "Not seen" perhaps does not mean "does not exist"
- ▶ Something interesting is going on with spin symmetries in the $c\bar{c}$ sector? Another example $Y(4260)[4220] \rightarrow J/\psi \pi \pi, h_c \pi \pi$, $Y(4360) \rightarrow \psi(2S) \pi \pi, h_c \pi \pi$.

Food for thought ...

A side remark on diquarkonium $[Qq][\bar{Q}\bar{q}]$

- ▶ Driving idea: in antisymmetric $[Qq]$ attraction, in symmetric $\{Qq\}$ repulsion. Inspired by Coulomb-like one gluon exchange.
- ▶ However generally there are transitions $[Qq][\bar{Q}\bar{q}] \leftrightarrow \{Qq\}\{\bar{Q}\bar{q}\}$
- ▶ One gluon exchange in $Q(1)\bar{Q}(2)q(3)\bar{q}(4)$ in terms of $c_{ij} = \alpha_s/r_{ij}$:

$$V \left(\begin{array}{c} [Qq][\bar{Q}\bar{q}] \\ \{Qq\}\{\bar{Q}\bar{q}\} \end{array} \right) = -\frac{1}{4} \left(\begin{array}{cc} \frac{N_c^2-1}{N_c} r + \frac{N_c+1}{N_c} t & \sqrt{N_c^2-1} s \\ \sqrt{N_c^2-1} s & \frac{N_c^2-1}{N_c} r - \frac{N_c-1}{N_c} t \end{array} \right) \left(\begin{array}{c} [Qq][\bar{Q}\bar{q}] \\ \{Qq\}\{\bar{Q}\bar{q}\} \end{array} \right)$$

N_c - number of colors, $r = c_{12} + c_{34} + c_{14} + c_{23}$,

$s = c_{12} + c_{34} - c_{14} - c_{23}$, $t = 2c_{13} + 2c_{24} - c_{12} - c_{14} - c_{23} - c_{34}$

- ▶ s — attraction between the diquarks (zero overall color), t — attraction/repulsion within $[Qq]/\{Qq\}$, r — mixing $[Qq][\bar{Q}\bar{q}] \leftrightarrow \{Qq\}\{\bar{Q}\bar{q}\}$
- ▶ difference attraction - repulsion within $[Qq]/Qq \propto 2N_c/N_c = 2$; mixing term $\propto \sqrt{N_c^2-1} = O(N_c) \Rightarrow$ parametrically mixing $\gg$ difference.
- ▶ There is no parameter that would keep diquarks color antisymmetric in a $Q\bar{Q}q\bar{q}$ system!

Hadro-charmonium

No obvious nearby threshold

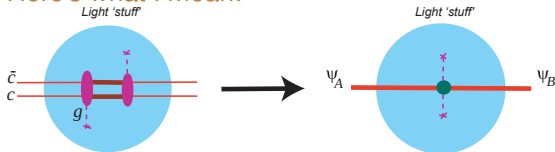
- ▶ $Z_1^\pm(4050)$, $Z_2^\pm(4250) \rightarrow \chi_{c1}\pi^\pm$ (status unclear),
- ▶ $Z_c^\pm(4100) \rightarrow \eta_c\pi^\pm$,
- ▶ $Z_c^\pm(4200) \rightarrow J/\psi\pi^\pm$,
- ▶ $Z^\pm(4430), \rightarrow \psi(2S)\pi^\pm$,
- ▶ Pentaquark(s):
 $P_c(4380)$, $P_c(4440)$, $P_c(4457)$, $P_c(4312) \rightarrow J/\psi p$

Still under discussion [$D_1\left(\frac{3}{2}^+\right)\bar{D}$ nearby threshold but S wave in e^+e^- forbidden by HQSS]:

- ▶ $Y(4260)$ [4220] $\rightarrow J/\psi\pi\pi, h_c\pi\pi$ (almost no open charm),
- ▶ $Y(4360) \rightarrow \psi(2S)\pi\pi, h_c\pi\pi$ (almost no open charm)

To me these all look like 'a charmonium stuck in a light hadron'. At least this can explain why a specific charmonium state e.g. J/ψ , or ψ' , or η_c appears in the decay.

Here's what I mean:



A van der Waals type interaction due to chromo-polarizability

$$\langle B | H_{\text{eff}} | A \rangle = -\frac{1}{2} \alpha_{AB} \vec{E}^a \cdot \vec{E}^a \quad \text{Chromo - polarizability : } \alpha_{AB}$$

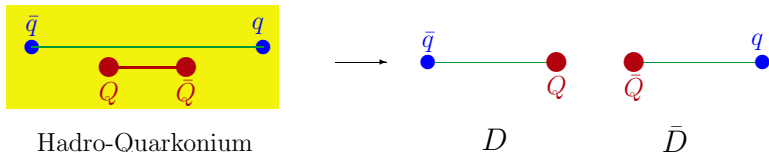
$|\alpha_{\psi' J/\psi}| \approx 2 \text{ GeV}^{-3}$ is known from $\psi' \rightarrow \pi\pi J/\psi$. Schwartz inequality
 $\alpha_{J/\psi} \alpha_{\psi'} \geq \alpha_{\psi' J/\psi}^2$.

$$\langle X | \vec{E}^a \cdot \vec{E}^a | X \rangle \geq \langle X | \vec{E}^a \cdot \vec{E}^a - \vec{B}^a \cdot \vec{B}^a | X \rangle = -\frac{1}{2} \langle X | (F_{\mu\nu}^a)^2 | X \rangle = \frac{32\pi^2}{9} M_X^2$$

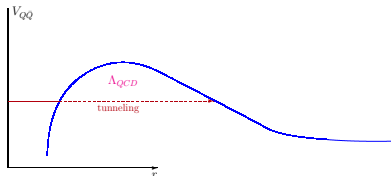
$X = (\text{Light hadron}) \Rightarrow$ strong interaction with heavier hadronic states made of light quarks and gluons.

E.g. J/ψ binding potential in heavy nuclei $V < -27 \text{ MeV}$.

Decay to open heavy flavor requires reconnection of the couplings



Born-Oppenheimer potential between heavy:



The tunneling momentum $|p_Q| = \sqrt{M_Q (V_{Q\bar{Q}} - E)} \sim \sqrt{M_Q \Lambda_{QCD}} \Rightarrow$

$$\Gamma(\rightarrow \text{open flavor}) \propto \exp(-\sqrt{M_Q/\Lambda_{QCD}})$$

If such interpretation of Y's and Z's has anything to do with reality, there should be:

- ▶ bound states of J/ψ and/or ψ' with light nuclei and with baryonic resonances, i.e. baryo-charmonium decaying to e.g. pJ/ψ (+ pions) $\Rightarrow$ pentaquarks
- ▶ resonances containing χ_{cJ} charmonium, i.e. in $\chi_{cJ} + \text{pion(s)}$
 $Z_1^\pm(4050), Z_2^\pm(4250) \rightarrow \chi_{c1} \pi^\pm$
- ▶ decays (moderately suppressed) into non-preferred charmonium states, e.g. $Y(4260) \rightarrow \pi\pi\psi'$, or $Y(4.36) \rightarrow \pi\pi J/\psi$
- ▶ Contain compact charmonium inside $\Rightarrow$ can be produced in hard processes: B decays, $p\bar{p}$, LHC, ...

$Z_c(4100)$, $Z_c(4200)$

- ▶ Belle 2014: $B^0 \rightarrow J/\psi \pi^- K^+$ resonance in $J/\psi \pi^-$ (6.2σ), $Z_c(4200)$,
 $M = 4196^{+35}_{-32}$ MeV, $\Gamma = 370^{+170}_{-150}$ MeV,
 $\mathcal{B}[B^0 \rightarrow Z_c(4200)^- K^+ \rightarrow J/\psi \pi^- K^+] \approx 2.2 \times 10^{-5}$, $J^P = 1^+$
preferred.
- ▶ LHCb 2018: $B^0 \rightarrow \eta_c \pi^- K^+$ resonance in $\eta_c \pi^-$ ($> 3\sigma$), $Z_c(4100)$,
 $M = 4096 \pm 20^{+18}_{-22}$ MeV, $\Gamma = 152 \pm 58^{+60}_{-35}$ MeV
 $\mathcal{B}[B^0 \rightarrow Z_c(4100)^- K^+ \rightarrow \eta_c \pi^- K^+] \approx 1.9 \times 10^{-5}$, $J^P = 0^+$ preferred

Strongly suggests: $Z_c(4100) = \eta_c$ embedded in S wave in an 'excited pion' $I^G(J^P) = 1^-(0^-)$, $Z_c(4200) = J/\psi$ embedded in an 'excited pion' $I^G(J^P) = 1^-(0^-)$. Expected:

- ▶ The same embeddings — HQSS partners, like η_c and $J/\psi \Rightarrow$

$$M[Z_c(4200)] - M[Z_c(4100)] \approx M(J/\psi) - M(\eta_c) = 112 \text{ MeV}$$

- ▶ $\Gamma[Z_c(4100) \rightarrow \eta_c \pi] \approx \Gamma[Z_c(4200) \rightarrow J/\psi \pi]$

▶

$$\frac{\mathcal{B}[B^0 \rightarrow Z_c(4100)^- K^+]}{\mathcal{B}[B^0 \rightarrow Z_c(4200)^- K^+]} \approx \frac{\mathcal{B}[B^0 \rightarrow \eta_c \pi^- K^+]}{\mathcal{B}[B^0 \rightarrow J/\psi \pi^- K^+]} \Big|_{M(c\bar{c}\pi) \approx M(Z_c)}$$

HQSS breaking processes

Leading HQSS breaking — M1 chromomagnetic interaction

$$H_{M1} = -\frac{1}{2m_c} (t_c^a - t_{\bar{c}}^a) (\vec{\Delta} \cdot \vec{B}^a)$$

$\vec{\Delta} = \vec{s}_1 - \vec{s}_2$ spin operator: $\langle {}^1S_0 | \Delta | {}^3S_1 \rangle = \langle {}^3S_1 | \Delta | {}^1S_0 \rangle \Rightarrow$ same coefficient C in the HQSS breaking amplitudes:

$$A[Z_c(4100) \rightarrow J/\psi \rho] = C(\vec{\psi} \cdot \vec{\rho}) ; \quad A[Z_c(4200) \rightarrow \eta_c \rho] = C(\vec{Z} \cdot \vec{\rho})$$

Implies

$$\Gamma[Z_c(4100) \rightarrow J/\psi \rho] \approx 3 \Gamma[Z_c(4200) \rightarrow \eta_c \rho]$$

HQSS breaking in charmonium $\sim 10\%$ in the rate ($\psi' \rightarrow J/\psi \eta$ vs. $\psi' \rightarrow J/\psi \pi \pi$)

Other related processes

- ▶ Same embedding — the same admixture of excited states $\eta_c(2S)$, $\psi(2S) \Rightarrow$

$$\Gamma[Z_c(4100) \rightarrow \eta_c(2S)\pi] \approx \Gamma[Z_c(4200) \rightarrow \psi(2S)\pi]$$

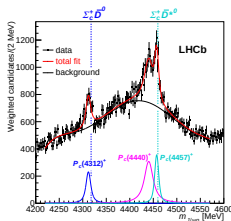
- ▶ Orbitaly excited. P and G conservation allows only $Z_c(4100) \rightarrow \chi_{c1}\pi$ and $Z_c(4200) \rightarrow h_c\pi$

$$\frac{\Gamma[Z_c(4200) \rightarrow h_c\pi]}{\Gamma[Z_c(4100) \rightarrow \chi_{c1}\pi]} \approx \left(\frac{p_2}{p_1}\right)^3 \approx 1.5$$

(P wave decays. Thus the kinematical difference is more important than in the previous.) Both processes are suppressed by both HQSS and the (orbital) excitation.

- ▶ Neutral isotopic partners of both Z_c can be S wave resonances in $\bar{p}p$ annihilation (PANDA). (The charged ones, Z_c^- , would require a deuterium target, $\bar{p}d$.)

$P_c(4312)$, $P_c(4440)$, $P_c(4457)$ — $\Sigma_c(2455)\bar{D}^{(*)}$ molecules ?



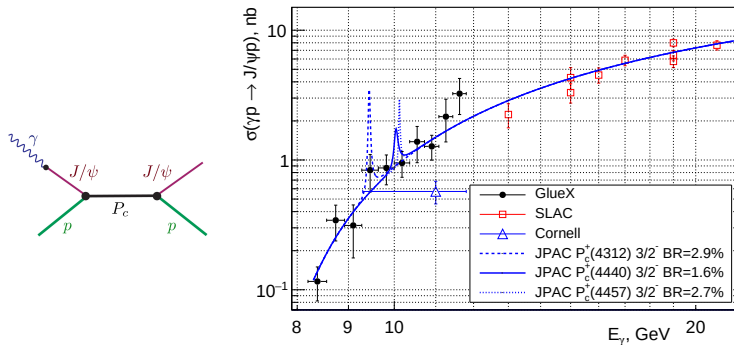
LHCb 2019: $\Lambda_b \rightarrow J/\psi p K$

- ▶ $P_c(4312) — \Sigma_c(2455)\bar{D}$, $|E_{\text{binding}}| \approx 5 - 10 \text{ MeV}$, $J^P = \frac{1}{2}^-$
- ▶ $P_c(4440) — \Sigma_c(2455)\bar{D}^*$, $J^P = \frac{1}{2}^-$
- ▶ $P_c(4457) — \Sigma_c(2455)\bar{D}^*$, $J^P = \frac{3}{2}^-$
- ▶ $P_c(4557) - P_c(4440)$ splitting due to spin-spin interaction of Σ_c and $\bar{D}^*$
- ▶ **Big** question: what about $P_c \rightarrow \Lambda_c \bar{D}^{(*)}$? Not forbidden by any law of nature.

P_c as baryocharmonium. (Charmonium embedded in an excited baryon.)

- ▶ $P_c(4312) — \chi_{c0} N$, $J^P = \frac{1}{2}^+$
- ▶ $P_c(4440), P_c(4457) — \psi(2S)N$, $J^P = \frac{1}{2}^-, \frac{3}{2}^-$

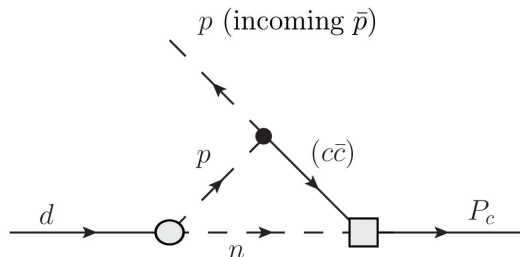
Additional sources of P_c : $\gamma + p \rightarrow P_c, \bar{p} + d \rightarrow P_c$



GlueX ArXiv: 1905.10811

The upper limit on $Br(P_c \rightarrow J/\psi + p)$ depends on the J^P of P_c . So far unclear, likely at the level of few %

Hidden-charm pentaquarks in $\bar{p} + d \rightarrow P_c$



Simultaneously for d at rest and p at rest $\bar{p} + d \rightarrow P_c$ and $\bar{p} + p \rightarrow (c\bar{c})$:
 $M_{P_c} = M_0$

$$M_0^2 = 2m_{(c\bar{c})}^2 + m_N^2$$

$M_0 = 4.48 \text{ GeV}$ for $(c\bar{c}) = J/\psi$ and $M_0 = 4.33 \text{ GeV}$ for $(c\bar{c}) = \eta_c$.
 Compare with $P_c(4450)$.

No need to consider short distance structure in deuteron.

BW max cross section: $\sigma(\bar{p} + d) \rightarrow P_c \approx Br[P_c \rightarrow \bar{p} + d] \times 2 \times 10^{-27} \text{ cm}^2$
 $Br[P_c \rightarrow \bar{p} + d] \approx 0.5 \times 10^{-6} Br[P_c \rightarrow (c\bar{c}) + n] \Gamma[(c\bar{c}) \rightarrow p\bar{p}] / (1 \text{ keV})$
 $\sim 10^{-7} Br(P_c \rightarrow J/\psi + n)$ for J/ψ , $\sim 2.5 \times 10^{-5} Br(P_c \rightarrow \eta_c + n)$ for η_c

Conclusions

- ▶ It looks like we (somewhat) understand charmonium and bottomonium below open flavor threshold. The atomic physics of quarkonium.
- ▶ What happens above the threshold — mostly puzzles.
- ▶ Molecules, hadroquarkonium, ... — Hadronic chemistry.
- ▶ Hybrids — $c\bar{c}$ plus gluonic excitations. Nowhere to be seen ...
- ▶ Some are likely molecules, some - hadroquarkonium. No 'one size fits all solution'.
- ▶ Other sources of XYZ...P
 - ▶ Additional possibilities in $\bar{p} + p \rightarrow X, Y, Z$ (neutral)
 - ▶ More possibilities (charged states) if $\bar{p}n$ could be studied using deuterium target.
 - ▶ Formation in $\gamma + p \rightarrow Pc$ ongoing at JLAB.
 - ▶ Pentaquarks can possibly be studied in $\bar{p} + d \rightarrow Pc$.